

**UNIVERSIDAD CARLOS III DE MADRID**  
**ECONOMETRICS I**  
**Academic year 2006/07**  
**FINAL EXAM**

September, 22nd, 2007

## PROBLEM TEXT

**Very important:** Notice that some results may have been omitted from the tables.

### PROBLEM 1: MONEY DEMAND

The conventional specification for money demand posits

$$\ln \left( \frac{M}{P} \right) = \alpha_1 + \alpha_2 RS + \alpha_3 \ln Y + \zeta, \quad (*)$$

where “ln” stands for natural logarithm,  $M$  = total amount of money,  $P$  = price index,  $RS$  = short run interest rate (which takes values between 0 and 1),  $Y$  = transaction volume (income).

The quantitative money theory establishes the following accounting identity:

$$MV = P Y,$$

where  $V$  = velocity of money. Taking natural logarithms, we can write such identity in additive form:

$$m + v = p + y,$$

or, equivalently,

$$-v = m - p - y,$$

where  $m = \ln M$ ,  $v = \ln V$ ,  $p = \ln P$ ,  $y = \ln Y$ .

Furthermore, the short run interest rate,  $RS$ , can be an endogenous variable. As potential instruments, we have available the long run interest rate,  $RL$ , as well as the short run interest rate two years ago,  $RS(-2)$ .

We consider two alternative specifications:

$$-v_t = \beta_1 + \beta_2 RS_t + u_t, \quad (1)$$

$$-v_t = \delta_1 + \delta_2 RS_t + \delta_3 y_t + \varepsilon_t. \quad (2)$$

The following results are based on estimating the money demand for the United Kingdom between 1874 and 1970:

**OUTPUT 1:** OLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $-v$

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.309479	0.022446	-13.78742	0.0000
$RS$	-7.005548	0.634474	-11.04150	0.0000
Mean of dependent variable	-0.525011			
S.D. of dependent variable	0.164059			
Standard error of residuals	0.109142			
$R^2$	0.562040			
Adjusted $\bar{R}^2$	0.557430			
Durbin-Watson statistic	0.327830			

**OUTPUT 2:** TSLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $-v$

Instruments:  $RL, RS(-2)$

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.324494	0.026089	-12.43802	0.0000
$RS$	-6.517483	0.767152	-8.495690	0.0000

**OUTPUT 3:** OLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $RS$

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.007971	0.003011	-2.647508	0.0095
$RL$	0.688677	0.097922	7.032898	0.0000
$RS(-2)$	0.417955	0.083551	5.002412	0.0000
Mean of dependent variable	0.030766			
S.D. of dependent variable	0.017557			
Standard error of residuals	0.009906			
Sum of squared residuals	0.009224			
$R^2$	0.688276			
Adjusted $\bar{R}^2$	0.681643			

**OUTPUT 4:** OLS estimates using the 97 observations 1874 – 1970  
 Dependent variable:  $-v$

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.324494	0.026089	-12.43802	0.0000
$RS$	-6.517483	0.767152	-8.495690	0.0000
$res3$	-1.565694	1.367535	-1.144903	0.2552
Mean of dependent variable		-0.525011		
S.D. of dependent variable		0.164059		
Standard error of residuals		0.108964		
$R^2$		0.568063		
Adjusted $\bar{R}^2$		0.558873		

(NOTE:  $res3$  are the residuals from OUTPUT 3)

**OUTPUT 5:** OLS estimates using the 95 observations 1876 – 1970  
 Dependent variable:  $e$  (Note:  $e$  are the residuals from OUTPUT 1)

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	0.000268	0.006242	0.042884	0.9659
$e(-1)$	0.850289	0.104457	8.140077	0.0000
$e(-2)$	-0.017044	0.104623	-0.162905	0.8710
Mean of dependent variable		0.000289		
S.D. of dependent variable		0.109702		
Standard error of residuals		0.108964		
$R^2$		0.699037		
Adjusted $\bar{R}^2$		0.692494		
Durbin-Watson statistic		1.983758		

(Note:  $e(-1)$ ,  $e(-2)$  denote the first and second lag of the residuals in OUTPUT 1)

**OUTPUT 6:** OLS estimates using the 97 observations 1874 – 1970  
 Dependent variable:  $-v$   
 Standard deviations robust to serial correlation, lag(s) order 3

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.309479	0.040132	-7.711609	0.0000
$RS$	-7.005548	1.032501	-6.785029	0.0000
Mean of dependent variable		-0.525011		
S.D. of dependent variable		0.164059		
$R^2$		0.562040		
Adjusted $\bar{R}^2$		0.557430		
Durbin-Watson statistic		0.327830		

**OUTPUT 7:** OLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $-v$

Standard deviations robust to serial correlation, lag(s) order 3

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.652518	0.290490	-2.246268	0.0270
$RS$	-7.333019	1.114031	-6.582422	0.0000
$y$	0.042682	0.037187	1.147754	0.2540

Mean of dependent variable	-0.525011
S.D. of dependent variable	0.164059
$R^2$	0.576082
Adjusted $\bar{R}^2$	0.557230

**OUTPUT 8:** OLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $-v$

Standard deviations robust to heterokedasticity, variant HC1

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.652518	0.168034	-3.88325	0.00020
$RS$	-7.333019	0.701298	-10.45636	0.00000
$y$	0.042682	0.019122	2.23209	0.02798

**OUTPUT 9:** OLS estimates using the 97 observations 1874 – 1970

Dependent variable:  $-v$

Variable	Coefficient	Std. Error	t-statistic	p-value
$C$	-0.652518	0.168834	-3.86485	0.00020
$RS$	-7.333019	0.700075	-10.47462	0.00000
$y$	0.042682	0.019002	2.24618	0.02703
Mean of dependent variable		-0.525011		
S.D. of dependent variable		0.164059		
$R^2$		0.576082		
Adjusted $\bar{R}^2$		0.557230		

## PROBLEM 2: EFFECT OF THE ETHNIC ORIGIN ON DEATH PENALTY

Some experts believe that in the United States the probability of being condemned to death is higher, *ceteris paribus*, when the accused is black. To evaluate such hypothesis, we analyze 679 in different States where the death penalty can be applied. In this sample, the proportion of white victims is 76%. We consider the following variables:

CONDENA = binary variable that equals 1 if the accused is condemned to death and 0 otherwise;

RAZA\_ACUSADO = binary variable that equals 1 if the accused is black and 0 otherwise;

RAZA\_VICTIMA = binary variable that equals 1 if the victim is black and 0 otherwise.

We obtained the following results:

### **OUTPUT 1:** Logit estimates using the 679 observations 1 – 679

Dependent variable: CONDENAS

Variable	Coefficient	Std. Error	t-statistic	Slope*
C	-2.08	0.14	-14.86	
RAZA_ACUSADO	-0.39	0.31	-1.26	-0.0356

\*At mean

Mean of CONDENAS = 0.102

Number of 'correctly predicted' cases = 610 (89.8 percent)

McFadden's Pseudo- $R^2$  = 0.0040

$f(\beta'x)$  at mean of independent variables = 0.090

Log-likelihood = -222.25

Likelihood ratio test:  $\chi^2_1 = 1.770$

### **OUTPUT 2:** Logit estimates using the 679 observations 1 – 679

Dependent variable: CONDENAS

Variable	Coefficient	Std. Error	t-statistic	Slope*
const	-2.04	0.61	-7.26	
RAZA_ACUSADO	0.83	0.36	2.31	0.0644
RAZA_VICTIMA	-2.39	0.60	-3.98	-0.1861

\*At mean

Number of 'correctly predicted' cases = 610 (89.8 percent)

McFadden's Pseudo- $R^2$  = 0.0496

$f(\beta'x)$  at mean of independent variables = 0.078

Log-likelihood = -212.07

Likelihood ratio test:  $\chi^2_2 = 22.13$