# Random-Walk-Based Segregation Measures* 

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December 22, 2012


#### Abstract

We propose an intuitive way of how to measure residential segregation in networks. Individuals are located in different nodes on a network that are interconnected through links. In this setting, we consider the process according to which, every period, an individual either moves to an adjacent node or she stops walking over the network, and define the segregation index as the probability that a randomly chosen individual meets an individual from the same social group when this random-walk terminates. It is shown that the segregation index is a natural generalization of the well-known isolation index to networks, that it has a closed-form relation to the PageRank index applied by Google, and that it is a generalization of the homophily index introduced by Currarini et al. (2009). We also show that the Spectral Segregation Index proposed by Echenique and Fryer (2007) is not continuous with respect to the network structure. Then, the segregation index is applied to Spanish census tract data and to citation data from Economics journals. Finally, we rationalize the segregation index as the equilibrium outcome of a game in which individuals have to decide how much time to invest in different cultures.


Keywords: Isolation, Homophily, Network, PageRank, Markov Chain, Segregation.
JEL-Numbers: C0, D85, Z13.

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## 1 Introduction

The objective of this study is to propose a new measure of residential segregation - the degree to which social groups live apart -, which is important in order to assess both the causes and consequences of social separation. For instance, Cutler et al. (2008) analyze how cultural factors explain the differences in segregation across ethnic groups. Also, residential segregation has a variety of effects on socioeconomic variables and its analysis is implicit in the design of integration policies. ${ }^{1}$ The most basic framework that addresses the question of how to measure residential segregation starts with some geographic space (i.e., a city) that is divided into smaller units called census tracts or neighborhoods. Also one takes the distribution of the different social groups (the population can be partitioned using observable characteristics such as ethnicity, religion, or nationality) over census tracts as given. Within this setting, the classical work of Massey and Denton (1988) introduces the following five dimensions of segregation: evenness, or the extent to which a group is distributed homogeneously over neighborhoods; exposure, or the degree of potential contact to other groups; concentration, or the amount of physical space a group occupies; centralization, or the degree to which a group resides close to the city center; and clustering, or the extent to which individuals from the same group tend to live in neighborhoods next to each other.

In a recent major contribution, Echenique and Fryer (2007) apply graph theory to derive a measure of (residential) segregation that they call the Spectral Segregation Index (SSI). The social interaction framework studied is based on the assumption that individuals divide their time among their neighbors/friends, and the more time they spend with individuals from their group, the more segregated the group as a whole is. The authors then apply the $S S I$ to the U.S. Census data from 2000 (replicating the results of Cutler and Glaeser 1997 on ghettos and uncovering a high rank correlation with measures that capture the dimensions of evenness and exposure) and to friendship networks in schools.

Our setting departs from Echenique and Fryer (2007) in several crucial aspects. First, we

[^1]allow multiple individuals to be located in the same node/neighborhood. Second, and most importantly, the segregation of a group depends in our model on the distribution of the other groups in all census tracts. The SSI, on the other hand, only considers the information that is contained in the subgraph of the considered group; that is, all individuals not belonging to the group in question are eliminated from the network. Our approach is therefore fundamentally different from the $S S I$, and, in particular, it is related to the following process: Pick any two individuals from a given group $g$ at random and suppose that the first of the two individuals moves over the network (city) in such a way that in the first period, she advances from her area of residence to some neighboring census tract. In each subsequent period, she either moves from her current position to some adjacent node (this event happens with probability $0 \leq \alpha<1$ ) or the process stops (this event happens with probability $1-\alpha$ ). Hence, the parameter $\alpha$ can be interpreted as the degree of spatial mobility. The normalized segregation index for group $g$, denoted by $\bar{\sigma}_{g}$, is then defined as the probability that the two randomly chosen individuals meet when the random-walk of the first individual terminates. ${ }^{2,3}$

After formally introducing the segregation index, we show that the measure directly incorporates three of the five dimensions introduced by Massey and Denton (1988); namely those of exposure, clustering, and centralization. First, the segregation index is a natural spatial generalization of the isolation index (see, Lieberson 1981) to networks. In fact, $\sigma_{g}$ reduces to the isolation index of group $g$ if the socio-geographical network is empty and individuals only interact in the neighborhoods they reside in (Proposition 1). Note that while $\sigma_{g}$ explicitly accounts for the intensity of interactions within group $g$, it is nevertheless directly related to the level of interaction with other groups (exposure) as well. This is because more intra-group interactions prevents the group from socializing with others.

[^2]To see that the segregation index is also related to the dimension of clustering, suppose that $\alpha=0$. In this case, the only interactions that matter are those with individuals from neighboring census tracts, and the measure becomes equal to the average proportion of all immediate neighbors that belong to the same group. Formally, Proposition 2 establishes that for $\alpha=0$, the segregation index reduces to the homophily index introduced by Currarini et al. (2009). Since social interactions with individuals who live further away become more and more feasible as $\alpha$ increases, one can regard $\sigma_{g}$ as a generalized measure of homophily/clustering that incorporates social relations beyond immediate neighbors.

Third, the segregation index also takes into account the dimension of centralization because groups that are closer to the socio-geographical center of the network are more likely to interact with individuals from the same group everything else equal. The relevance of centralization as a dimension of segregation has been reported in some countries like the U.S., where socioeconomic factors can cause some groups to move to the city center. In particular, the spatial mismatch literature emphasizes that blacks who tend to live closer to the city center have worse labor market outcomes (see, Ihlanfeldt and Sjoquist 1998 and Gobillon et al. 2007). Proposition 3 shows that the segregation index of a group $g$ is a weighted sum over the homophily indices of the nodes (the probability that a neighbor belongs to the same group), where the weight assigned to each node is assessed through the PageRank index used by Google to determine the importance of webpages in the World Wide Web. ${ }^{4}$ Thanks to this connection to PageRank, we are able to show how the segregation index can be easily implemented and efficiently calculated in regular computers, even for a large number of census tracts.

In the next step, we analyze a drawback of the $S S I$. We present an example showing that the SSI is not continuous in the strength of the social ties because in situations when two separated components of a network are merged by a new link, the SSI may change abruptly. We believe, and argue in more detail in Section 4, that continuity is a very important

[^3]property because both social and geographical networks change over time and are subject to a continuous addition and deletion of links. By considering the network structure we maintain the postulate of Echenique and Fryer (2007) that segregation is formed through social interactions, but we amend their drawback by developing a continuous measure.

In the empirical analysis, we first explore the geographical close-knitness of foreign residents in Spain in 2009. We find that the southern part of the Mediterranean coast of Almería and the autonomous community of Catalonia are the most segregated areas, while Galicia, the Basque Country and Andalusia are the least segregated ones. Also, the Pakistani and immigrants from Nigeria and Senegal are the most segregated groups, while the Latin Americans turn out to be rather integrated. Given the known detrimental effects of segregation on labor market outcomes (and therefore on income and other correlated variables), this result suggests a proactive housing policy that targets in particular immigrants from poor countries facing a language barrier. One final important feature of the model is that it allows us to uncover network/clustering effects - the change in the measure due to considering the network on top of the isolation index. These effects are strong for the Pakistani and some groups from Africa, but weak for immigrants from Western Europe.

To show that the theoretical model is flexible enough to address a wide range of different questions, we finally consider citation data for 140 leading Economics journals (that are divided into 18 different fields) from 2010 to articles published in 2005-2009. Letting $\alpha$ vary allows us again to uncover clustering in the underlying distribution. It turns out that among the smaller fields without many self citations, Accounting and Sectorial Studies show strong network effects, which suggests the existence of citation circles (journals from these fields cite journals from other fields, ..., that cite journals from the original field). This effect is not found in other fields of similar size (Human Resource Management and Social Economics).

Our final theoretical contribution is the construction of a game-theoretical model that rationalizes the segregation index. We use techniques similar to those developed in Currarini et al. (2009), where individuals are involved in a search process and utilities depend on whether they meet people who belong to the same or a different group. A network of relationships arises
as a consequence of these encounters. Ours is an essentially different search model. Individuals search through a fixed spatial network and there is no preference bias towards meetings with people from the same group. To be more concrete, individuals have to decide how much time to invest in each of the groups/cultures and then meet people from a neighboring node. We assume that there are two situations that create benefits for an individual who invests in culture $g$ : (a) her match also invests in culture $g$ and (b) her match belongs to group $g$. In the unique steady state equilibrium, the average time invested by group $g$ in its own culture is proportional to its segregation index. The fact that the benefits from the meetings are typeindependent highlights the unbiased nature of the segregation index. In particular, since the level of interaction of any individual of group $g$ with her neighbors does not depend on her group, the segregation index explains how the spatial setting alone can induce separation.

We proceed as follows. Next, we introduce the segregation index and relate it to the various dimensions of segregation. In Section 4, we discuss the discontinuity of the SSI. Section 5 presents the empirical results. In Section 6, we study the search model. Finally, we conclude. Proofs as well as some tables and numerical results are relegated to the Appendices.

## 2 The Segregation Index

Consider a set $N=\{1,2, \ldots, n\}$ of $n$ individuals. For simplicity, we will call $N$ a society. The individuals live in a city that is composed of a finite set $M=\{1,2, \ldots, m\}$ of $m$ neighborhoods or census tracts. A particular neighborhood $i \in M$ will also be referred to as a node. It is assumed that every individual lives in exactly one neighborhood, but that each neighborhood possibly inhabits multiple individuals. Also, there is a set $G$ of groups that forms a partition of the society. One can think of a group $g \in G$ as a subset of members of the society that share a particular attribute such as religion or ethnicity. Let $n_{g, i}$ be the number of individuals of group $g \in G$ that live in neighborhood $i \in M$. The number of individuals belonging to group $g \in G$ is $n_{g}=\sum_{i \in M} n_{g, i}$. Similarly, $n_{i}=\sum_{g \in G} n_{g, i}$ is the number of individuals that reside in neighborhood $i \in M$. The column vectors $\mathbf{c}_{g}=\left(n_{g, i} / n_{i}\right)_{i \in M}$ and $\mathbf{d}_{g}=\left(n_{g, i} / n_{g}\right)_{i \in M}$ are referred to as the vectors of group concentrations and group densities, respectively.

The different neighborhoods in a city are interconnected through links. Formally, A is an $m \times m$ matrix such that $a_{i, j}=1$ if there is a connection between $i$ and $j$, and $a_{i, j}=0$ otherwise. The intuition is that two neighborhoods are connected if they are geographically adjacent or if individuals from these neighborhoods directly interact with each other. ${ }^{5}$ We assume that $a_{i, i}=1$ so that individuals from the same neighborhood can directly interact with each other. Let $a_{i}=\left|\left\{j \in M: a_{i, j}=1\right\}\right|$ be the number of neighborhoods $i \in M$ is connected to. An $m \times m$ matrix $\mathbf{P}$ is said to be a row stochastic matrix associated with $\mathbf{A}$ whenever the following conditions hold: $p_{i, j}=0$ whenever $a_{i, j}=0, p_{i, j}>0$ whenever $a_{i, j}=1$, and $p_{i} \equiv \sum_{j \in M} p_{i, j}=1$. With this notation at hand, we can now formally define a city as a tuple $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$.

The advantage of working with a stochastic $\mathbf{P}$ is that it provides a natural interpretation in terms of node-to-node transition probabilities. A walk is a sequence $\omega=\left(\omega_{0}, \omega_{1}, \omega_{2}, \ldots\right)$ of at least two, possibly repeated neighborhoods with the restriction that two consecutive neighborhoods must be connected. We assume that in period $t=0$, a walk passes from the initial neighborhood $\omega_{0}$ to some adjacent neighborhood $\omega_{1}$. In every subsequent period $t=1,2,3 \ldots$, a walk continues with probability $\alpha \in[0,1)$ from the current position $\omega_{t}$ to an adjacent neighborhood $\omega_{t+1}$, and stops with probability $1-\alpha$. In case of continuation, the walk currently at neighborhood $i$ passes to $j$ with probability $p_{i, j}$. Formally, a random-walk is a random variable whose realization is a particular walk $\omega$, where the probability of a walk $\omega=\left(\omega_{0}, \omega_{1}, \ldots, \omega_{l}\right)$ of length $|\omega|=l$ conditional on the initial node being $\omega_{0}$ is

$$
\operatorname{Prob}\left(\omega \mid \omega_{0}\right)=\alpha^{(l-1)}(1-\alpha) p_{\omega_{0}, \omega_{1}} p_{\omega_{1}, \omega_{2}} \cdots p_{\omega_{l-1}, \omega_{l}} .
$$

For example, conditional on that $w_{0}=4$, the walk $\omega=(4,3,2)$ occurs with probability $p_{4,3} \cdot \alpha \cdot p_{3,2} \cdot(1-\alpha)$. Since $\alpha<1$, any realization $\omega$ of a random-walk has finite length with probability 1 . Let $\Omega$ be the set of all possible realizations of $\omega$. The expected walk length

[^4]$\mathbb{E}(l)$ is $^{6}$
$$
\mathbb{E}(l)=\sum_{l=1}^{\infty} l \sum_{\omega \in \Omega:|\omega|=l} \operatorname{Prob}\left(\omega \mid \omega_{0}\right)=\frac{1}{1-\alpha} .
$$

This equation shows that $\alpha$ is related to the expected walk length, and can thus be interpreted as the degree of spatial mobility. For instance, if $\alpha=0.85$, then $\mathbb{E}(l)=6.67$. Similarly, if $\alpha=0.99$, then $\mathbb{E}(l)=100 .{ }^{7}$

Given the transition matrix $\mathbf{P}$ and the continuation probability $\alpha \in[0,1)$, let $\mathbf{Q}$ be the $m \times m$ matrix such that $q_{i, j}$ is the probability that a walk ends in neighborhood $j$, given that it started in $i$. Our first objectives is to provide a closed-form expression of $\mathbf{Q}$ in terms of the parameters $\mathbf{P}$ and $\alpha$, yet it is already easy to see that (a) if $\mathbf{P}=\mathbf{I}$, no interaction takes place across neighborhoods, (b) if $\mathbf{P} \neq \mathbf{I}$ and $\alpha=0$, no interaction takes place beyond immediate neighbors, and (c) if $\mathbf{P} \neq \mathbf{I}$ and $\alpha$ tends to 1, the expected walk length grows arbitrarily large.

Lemma 1. $\mathbf{Q}=(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P}$.

## Proof. See Appendix A.

The intuition behind this result is as follows. In order to compute $q_{i, j}$, we have to consider all walks of the form $\omega=\left(i, \omega_{1}, \omega_{2}, \ldots, j\right)$. If $q_{i, j}^{[l]}$ denotes the probability that $j$ is reached in exactly $l$ steps from $i$, then

$$
q_{i, j}=\sum_{l=1}^{\infty} q_{i, j}^{[l]}=(1-\alpha) p_{i, j}+\alpha(1-\alpha) \sum_{\omega_{1} \in M} p_{i, \omega_{1}} p_{\omega_{1}, j}+\alpha^{2}(1-\alpha) \sum_{\omega_{1}, \omega_{2} \in M} p_{i, \omega_{1}} p_{\omega_{1}, \omega_{2}} p_{\omega_{2}, j}+\ldots
$$ or, in matrix notation,

$$
\begin{aligned}
\mathbf{Q} & =(1-\alpha) \mathbf{P}+\alpha(1-\alpha) \mathbf{P}^{2}+\alpha^{2}(1-\alpha) \mathbf{P}^{3}+\ldots \\
& =(1-\alpha)\left(\mathbf{I}+\alpha \mathbf{P}+\alpha^{2} \mathbf{P}^{2}+\ldots\right) \mathbf{P} \\
& =(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P}
\end{aligned}
$$

[^5]We can now suggest a measure of residential segregation that is related to the level of within-group interactions, taken into account through the matrix $\mathbf{Q}$. The segregation index $\sigma_{g}$ of group $g \in G$ is defined as the probability that a randomly chosen individual of group $g$ meets another individual from group $g$ in the neighborhood where her random-walk terminates.

Definition 1. Given city $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and the continuation probability $\alpha \in[0,1)$, the segregation index of group $g \in G$ is

$$
\sigma_{g}(C, \alpha)=\sum_{i \in M} d_{g, i} \sum_{j \in M} q_{i, j} c_{g, j}=\mathbf{d}_{g}^{\top} \mathbf{Q} \mathbf{c}_{g} .
$$

Since $\sigma_{g}$ is a probability, it takes values from the interval $[0,1]$. To see that the measure is increasing in the relative size $n_{g} / n$ of group $g$, take any city $C$ and consider the city $\hat{C}$ that can be obtained from $C$ by doubling the concentration of individuals of group $g$ in each neighborhood maintaining the total population in each neighborhood constant. Thus, $\hat{\mathbf{d}}_{g}=\mathbf{d}_{g}, \hat{\mathbf{c}}_{g}=2 \mathbf{c}_{g}$ and $\hat{\mathbf{Q}}=\mathbf{Q}$, which implies that $\sigma_{g}(\hat{C}, \alpha)=2 \sigma_{g}(C, \alpha)$. Consequently, the segregation of group $g$ has doubled simply because the group has grown but not because its distribution over the network has changed. The reason for this dependence is that it is only required that an individual meets any (and not a randomly chosen) individual from the same group. This effect can be accounted for with the following normalization.

Definition 2. Given city $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and the continuation probability $\alpha \in[0,1)$, the normalized segregation index of group $g \in G$ is

$$
\bar{\sigma}_{g}(C, \alpha)=\left(\frac{n_{g}}{n}\right)^{-1} \sigma_{g}(C, \alpha)=\left(\frac{n_{g}}{n}\right)^{-1} \mathbf{d}_{g}^{\top} \mathbf{P} \mathbf{c}_{g} .
$$

If group $g$ is distributed homogeneously over all neighborhoods (for all $i \in M, c_{g, i}=n_{g} / n$ ), then $\sigma_{g}(C, \alpha)=n_{g} / n$ and $\bar{\sigma}_{g}(C, \alpha)=1$. So if $\bar{\sigma}_{g}(C, \alpha)>1$, group $g$ is on average overrepresented in census tracts compared to its overall population share. The size-independence of the normalized measure becomes even more visible if it is rewritten as follows:

$$
\bar{\sigma}_{g}(C, \alpha)=n \sum_{i \in M} d_{g, i} \sum_{j \in M} n_{j}^{-1} q_{i j} d_{g, j} .
$$

According to this equation, $\bar{\sigma}_{g}$ is equal to the probability (up to the multiplicative scalar $n$ ) that a randomly chosen individual from group $g$ meets another randomly chosen individual from the same group. The fact that both individuals are chosen at random prevents this probability from depending on the representativeness of the group in the society. Finally, the segregation index of city $C$ is defined as the weighted average over the segregation indices of the groups; that is, $\sigma(C, \alpha)=\sum_{g \in G} n_{g} / n \cdot \sigma_{g}(C, \alpha)$. Intuitively, $\sigma(C, \alpha)$ is the probability that a randomly chosen individual meets an individual from the same group when her random-walk terminates. The normalized segregation index $\bar{\sigma}(C, \alpha)$ of city $C$ is defined accordingly.

## 3 Properties

### 3.1 Exposure

Isolation, the opposite of exposure, is the degree of potential contact or interaction between members of the same group. This notion is captured through the isolation index, which is defined as the likelihood that a typical individual of a group faces a member from the same group in her own neighborhood:

$$
I_{g}(C)=\sum_{i \in M} d_{g, i} c_{g, i}=\mathbf{d}_{g}^{\top} \mathbf{c}_{g}
$$

The normalized isolation index is then $\bar{I}_{g}(C)=\left(n_{g} / n\right)^{-1} I_{g}(C)$. Our first proposition directly relates the segregation to the isolation index.

Proposition 1. Given city $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and the continuation probability $\alpha \in[0,1)$, the segregation index of group $g \in G$ is

$$
\sigma_{g}(C, \alpha)=(1-\alpha) \mathbf{d}_{g}^{\top}(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P} \mathbf{c}_{g}
$$

Proof. This is a direct consequence of Lemma 1 and Definition 1.

Proposition 1 shows that the segregation index reduces to the isolation index whenever the network is empty $(\mathbf{P}=\mathbf{I})$. The measure can also be interpreted as a weighted average over the entries of the vector $\mathbf{v}_{g} \equiv \mathbf{Q} \mathbf{c}_{g}=(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P} \mathbf{c}_{g}$, where the weight of each
neighborhood $i \in M$ is equal to $d_{g, i}$. Since $\mathbf{v}_{g}$ contains the contributions of all census tracts to the segregation of group $g$, we will call it the vector of local segregations of group $g$. In particular, $v_{g, i}$ is the expected concentration of group $g$ in the neighborhood where a randomwalk that started in neighborhood $i$ terminates. We conclude with an example.

Example. Consider the city $C$ depicted in Figure 1.


Figure 1: Calculation of the segregation index.

There are two ethnic groups, blacks and whites. Two whites reside in neighborhoods 1 and 3, three whites in neighborhood 4, and one white in neighborhood 2. Moreover, three blacks live in neighborhood 3 and one black in neighborhoods 1,2 and 4 each. The transition matrix $\mathbf{P}$ in Figure 1 is such that for all $i, j \in M, p_{i, j}=a_{i, j} / a_{i}$. Since $\mathbf{d}_{\text {blacks }}^{\top}=(1 / 6,1 / 6,1 / 2,1 / 6)$, $\mathbf{d}_{\text {whites }}^{\top}=(1 / 4,1 / 8,1 / 4,3 / 8), \mathbf{c}_{\text {blacks }}^{\top}=(1 / 3,1 / 2,3 / 5,1 / 4)$, and $\mathbf{c}_{w h i t e s}^{\top}=(2 / 3,1 / 2,2 / 5,3 / 4)$, it is easy to verify that $\sigma_{\text {blacks }}(C, 0.85)=0.45$ and $\sigma_{w h i t e s}(C, 0.85)=0.55$. The normalized measures are equal to $\bar{\sigma}_{\text {blacks }}(C, 0.85)=1.05$ and $\bar{\sigma}_{\text {whites }}(C, 0.85)=0.97$, respectively.

### 3.2 Clustering

Following Massey and Denton (1988), clustering is the extent to which individuals from the same social groups live in neighborhoods next to each other. ${ }^{8}$ It is rather intuitive that the segregation index incorporates clustering in the proper definition: An individual who starts a random-walk in her area of residence is more likely to end up in a neighborhood that is

[^6]closer to her own census tract than in a neighborhood that is further away as soon $\mathbf{P} \neq \mathbf{I}$. To say it differently, two individuals are more likely to meet the closer they live to each other. Figure 2 visualizes this effect. Since for all $\alpha \in[0,1), q_{4,5}(B, \alpha)>q_{2,5}(A, \alpha)$ and $q_{5,4}(B, \alpha)>q_{5,2}(A, \alpha)$, the segregation of the blacks is higher in City B than in City A. According to Massey and Denton (1988), this is entirely due to clustering. ${ }^{9}$


Figure 2: Clustering.

From a formal point of view, we establish that the segregation index captures the dimension of clustering by showing that it naturally extends the homophily measures developed in Currarini et al. (2009). The concept of homophily in social networks reflects the propensity of individuals to be directly linked to other individuals of the same type. In particular, the homophily index $h_{g}(C)$ of group $g \in G$ in city $C$ is the expected fraction of individuals in neighboring census tracts who belong to the same group:

$$
h_{g}(C)=\sum_{i \in M} d_{g, i} \sum_{j \in M} \frac{n_{g, j} a_{i, j}}{\sum_{k \in M} n_{k} a_{i, k}}
$$

As usual, we define the normalized homophily index as $\bar{h}_{g}(C)=\left(n_{g} / n\right)^{-1} h_{g}(C)$. In the example corresponding to Figure 2, $h_{\text {blacks }}(A)=1 / 2 \cdot(1 / 3+1 / 2)=5 / 12$ and $h_{\text {blacks }}(B)=$ $1 / 2 \cdot(2 / 3+1)=5 / 6$ - the homophily index for the blacks is higher in City B. Our next

[^7]proposition shows that if $\alpha=0$ and the transition probabilities are proportional to the sizes of the neighborhoods, the segregation index coincides with the homophily index. Consequently, the segregation index can be interpreted as a generalized measure of homophily that reaches beyond immediate neighbors for strictly positive $\alpha$.

Proposition 2. If $p_{i, j}=\left(a_{i, j} n_{j}\right) /\left(\sum_{k \in M} a_{i, k} n_{k}\right)$ for all $i, j \in M$, then $\sigma_{g}(C, 0)=h_{g}(C)$. Proof. See Appendix A.

### 3.3 Centralization

Generally speaking the centrality of a node in a network captures its well-connectedness. Depending on the specific context, it can for example be assessed using the notions of degree (the number of connections a node has), betweenness (determine the shortest paths between any two nodes and calculate then, for each node, to how many of these shortest paths it belongs to), or closeness (the mean geodesic distance between a node and all nodes reachable from it). In our case, the segregation index belongs to the class of eigenvector-based centrality measures and, in particular, it is related to the PageRank index of Brin and Page (1998) that underlies Google's search engine. ${ }^{10}$

The main idea of the PageRank vector is that a webpage is more important when it is linked by other relevant pages. This idea is formalized with a finite Markov chain according to which an individual "surfs" randomly over the web. The entries of the PageRank vector are then just the stationary probabilities of this process. More formally, an individual starts at any node (webpage) and surfs the web randomly according to the (column-stochastic) matrix $\mathbf{S}$ that represents the actual links of the web. Additionally, at any point in time, the surfer is "teleported" to page $j$ (even if the current page $i$ is not directly linked with $j$ ) with probability $1-\beta$, while she continues her random-walk by crossing links normally following $\mathbf{S}^{\top}$ with probability $\beta$. In case of teleportation, the surfer is taken to page $j$ with probability $r_{j}$. The vector $\mathbf{r}=\left(r_{i}\right)_{i \in M}$ is the personalizaction vector of the PageRank index summarizing the

[^8]teleporting mechanism. This process defines a Markov chain whose stationary probabilities are gathered in the PageRank vector, the principal eigenvector of the matrix $(1-\beta) \mathbf{r} \mathbf{1}^{\top}+\beta \mathbf{S}$.

This notion of centrality can be straightforwardly adapted to our framework: An individual from group $g \in G$ randomly walks in the city according to the transition matrix $\mathbf{P}$ (that is, $\mathbf{S}=\mathbf{P}^{\boldsymbol{\top}}$ ) and is teleported to node $j$ with probability $(1-\alpha) d_{g, j}$ (that is, $\beta=\alpha$ and $\left.\mathbf{r}=\mathbf{d}_{g}\right)$.

Definition 3. Given the city $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and the continuation probability $\alpha \in[0,1)$, the PageRank vector $\mathbf{w}_{g}$ of group $g \in G$ is the principal eigenvector of the matrix $(1-\alpha) \mathbf{d}_{g} \mathbf{1}^{\top}+\alpha \mathbf{P}^{\top}$.

Note that $\mathbf{w}_{g}$ captures the centrality of the nodes for group $g$. It is group-dependent because the personalization vector $\mathbf{r}$ is set equal to the density vector $\mathbf{d}_{g}$ of group $g$. Thus, in the PageRank model, $w_{g, i}$ is the stationary probability of neighborhood $i$ when teleportation takes place according to $\mathbf{d}_{g}$, and it accounts for the reachability of neighborhood $i$ by members of group $g$. Our next proposition is the dual of Proposition 1.

Proposition 3. The segregation index of group $g$ is equal to $\sigma_{g}(C, \alpha)=\mathbf{w}_{g}^{\top} \mathbf{P} \mathbf{c}_{g}$.

Proof. See Appendix A.

Proposition 3 shows that individuals who are more central in the sense of PageRank contribute more to the overall segregation of their group because they are easier to reach by other group members. Also, if $p_{i, j}=\left(a_{i, j} n_{j}\right) /\left(\sum_{k \in M} a_{i, k} n_{k}\right)$ for all $i, j \in M$ (i.e., transition probabilities are proportional to the sizes of the neighborhoods as in Proposition 2), then $\sigma_{g}(C, \alpha)=\mathbf{w}_{g}^{\top} \mathbf{h}_{g}$, where

$$
h_{g, i}=\sum_{j \in M} \frac{n_{g, j} a_{i, j}}{\sum_{k \in M} n_{k} a_{i, k}}
$$

is the homophily index of neighborhood $i \in M$ for group $g \in G$. This equation highlights the interaction between the position of a neighborhood in the network (centrality) and its clustering (homophily): In the computation of $\sigma_{g}(C, \alpha)$, the homophily index $h_{g, i}$ of neighborhood
$i \in M$ is weighted by its PageRank index $w_{g, i}$. Note also that $\mathbf{w}_{g}=\mathbf{d}_{g}$ if the network is empty $(\mathbf{P}=\mathbf{I})$ or if there is no spatial mobility beyond one's own neighborhood $(\alpha=0)$. In the first case, $\sigma_{g}$ reduces to the isolation index (because $h_{g, i}$ is then equal to $c_{g, i}$ ). In the second case, $\sigma_{g}$ becomes equal to the homophily index. But if network effects are present $(\mathbf{P} \neq \mathbf{I}$ and $\alpha>0$ ), groups that are located more central in the network everything else equal have a higher possibility of intra-group interactions and, as a consequence, a higher segregation index. ${ }^{11}$ This is made visible with the help of the following example.

Example. Consider the city $C$ depicted in Figure 3.


Figure 3: Centrality.

There are eleven individuals belonging to three ethnic groups (blacks, whites, and squares). There is exactly one individual in each neighborhood. The particularity of the network structure is that the blacks and the whites are allocated in a very similar way. Every black is connected to two other blacks plus herself, one white, and one square. Every white is also connected to two other whites plus herself, one black, and one square. The important difference is that all blacks are connected to the same square (individual 11), while two whites are connected to square 9 and two whites to square 10 . Square 11 is thus the most central individual of her group, which implies that the blacks are relatively more central.

Since $I_{\text {blacks }}(C)=I_{\text {whites }}(C)=1$ and $h_{\text {blacks }}(C)=h_{\text {whites }}(C)=3 / 5$, both groups are

[^9]equally isolated and clustered. Hence, $\sigma_{g}(C, \alpha)$ incorporates the difference between the two groups entirely through the PageRank vectors. Straightforward computations yield that $\sigma_{\text {blacks }}(C, 0.85)=0.48>0.47=\sigma_{\text {whites }}(C, 0.85) .{ }^{12}$

We complete this part of the analysis with an important comment regarding the implementability of the segregation index in real-life applications. The computation of $\sigma_{g}$ is simple and very fast, even for large matrices. One can apply first a simple iterative power method to compute the PageRank vector $\mathbf{w}_{g}$, and then Proposition 3 to compute the product $\mathbf{w}_{g}^{\top} \mathbf{P} \mathbf{c}_{g}$. To calculate $\mathbf{w}_{g}$, one departs from a randomly chosen probability vector $\mathbf{w}_{g}^{(0)}$ (that is, $w_{g, i}^{(0)} \geq 0$ for all $i \in M$ and $\left.\sum_{i \in M} w_{g, i}^{(0)}=1\right)$ and then iterates by calculating $\mathbf{w}_{g}^{(t+1)}=(1-\alpha) \mathbf{d}_{g}+\alpha \mathbf{P}^{\top} \mathbf{w}_{g}^{(t)}$ for all $t=0,1,2, \ldots$. The asymptotic convergence rate of this iterative power method is equal to $\alpha$, see Langville and Meyer (2006). For example, if $\alpha=0.85, \alpha^{50} \approx 0.00296$; that is, one expects at least $2-3$ places of accuracy after only 50 iterations. ${ }^{13}$

### 3.4 Evenness

Evenness refers to how equal the individuals of a given group are spread over the city. Formally, we say that the distribution of group $g$ is even if for all $i \in M, d_{g, i}=n_{i} / n$, or equivalently, $c_{g, i}=n_{g} / n$. In this case, $\bar{\sigma}_{g}(C, \alpha)=\left(n_{g} / n\right)^{-1} \mathbf{d}_{g}^{\top} \mathbf{P} \mathbf{c}_{g}=\mathbf{d}_{g}^{\top} \mathbf{P} \mathbf{1}=\mathbf{d}_{g}^{\top} \mathbf{1}=1$ independently of the network structure. This calculation shows that we can use a unit-normalized segregation index as a benchmark level in the sense that uneven distributions will lead to a higher or lower normalized segregation. If $\bar{\sigma}_{g}(C, \alpha)>1$, group $g$ is on average overrepresented in neighborhoods. It is underrepresented whenever $\bar{\sigma}_{g}(C, \alpha)<1$. We show next that no group can on average be underrepresented if the isolation index is applied. Hence, in this case, there

[^10]is an immediate connection between uneven distributions and a high segregation.

Proposition 4. For all cities $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$, all continuation probabilities $\alpha \in[0,1)$, and all groups $g \in G, \bar{I}_{g}(C) \geq 1$.

Proof. See Appendix A.

Since individuals can interact in several neighborhoods as soon as the network matters, it becomes possible that a group is on average underrepresented (low segregation), even if its distribution is uneven. The following example illustrates this effect.

Example. Consider the city depicted in Figure 4.


Figure 4: Evenness.

Using the node-to-node transition matrix $\mathbf{P}$ one finds that the probabilities that the random-walk terminates in a given neighborhood are equal to

$$
\mathbf{d}_{\text {blacks }}^{\top} \mathbf{Q}=\frac{1}{12+2 \alpha}(4+2 \alpha, 4,4) \quad \text { and } \quad \mathbf{d}_{w h i t e s}^{\top} \mathbf{Q}=\frac{1}{12+2 \alpha}(6,3+\alpha, 3+\alpha)
$$

We see that the black individual living in the city center is more likely to terminate her walk in her area of residence. Similarly, the black center is also more likely to absorb a walk starting from the white edges. We then obtain that

$$
\bar{\sigma}_{\text {blacks }}(C, \alpha)=\frac{12+6 \alpha}{12+2 \alpha} \geq 1 \quad \text { and } \quad \bar{\sigma}_{\text {whites }}(C, \alpha)=\frac{18+6 \alpha}{24+4 \alpha}<1
$$

We stress that the normalized segregation of the whites is lower than one even though the distribution of the group is uneven. This highlights the idea that an uneven distribution can potentially make individuals hardly accessible by members of the same group.

## 4 Discontinuity of the $S S I$

In this part of the paper, it is shown that the SSI proposed in Echenique and Fryer (2007) is not continuous in the strength of the social ties. Even though cities do not experience abrupt
changes in the short run, people may move within the city or change their pattern of social interactions, and we therefore think that a measure of segregation should behave in a stable way to these changes. Since the only difference in the primitives between Echenique and Fryer (2007) and our model is that they assume a one-to-one mapping between neighborhoods and individuals, it is assumed for the time being that $n_{i}=1$ for all $i \in M .{ }^{14}$

Given the matrix $\mathbf{P}$, the $S S I$ for group $g \in G$ is calculated by determining first the subgraph $\mathbf{P}^{g}$ of $\mathbf{P}$ that only contains interactions between members of $g$. All individuals belonging to a different group are eliminated from the network and, consequently, from the matrix $\mathbf{P}$. Such a subgraph $\mathbf{P}^{g}$ of $\mathbf{P}$ generally consists of more than one strongly connected component, so the next step is to calculate the SSI for each component separately. In particular, the SSI for group $g$ in the (strongly connected) component $\mathbf{P}^{g, \gamma}$ of $\mathbf{P}^{g}$ - denoted by $\operatorname{SSI}\left(\mathbf{P}^{g, \gamma}\right)$ - is set equal to the spectral radius of the matrix $\mathbf{P}^{g, \gamma}$, the largest absolute value of the eigenvalues of $\mathbf{P}^{g, \gamma} .{ }^{15}$ The segregation of a node (individual) $i$ in this component is denoted by $S S I_{i}\left(\mathbf{P}^{g, \gamma}\right)$, and it is the $i-$ th entry of the principal eigenvector of the matrix $\mathbf{P}^{g, \gamma}$, normalized so that the vector average is $\operatorname{SSI}\left(\mathbf{P}^{g, \gamma}\right)$. The segregation of group $g$ is a weighted average over the segregation levels of group $g$ in all components of $\mathbf{P}^{g}$. In particular,

$$
S S I\left(\mathbf{P}^{g}\right)=\sum_{\gamma} d_{g}^{\gamma} \cdot S S I\left(\mathbf{P}^{g, \gamma}\right),
$$

where $d_{g}^{\gamma}=1 / n_{g} \cdot \sum_{i \in \mathbf{P}^{g, \gamma}} n_{g, i}$ is the fraction of individuals from group $g$ that live in $\mathbf{P}^{g, \gamma} .{ }^{16}$ Alternatively, the $S S I$ of group $g$ can also be expressed as the average over the individual segregation levels:

$$
\operatorname{SSI}\left(\mathbf{P}^{g}\right)=\frac{1}{n_{g}} \sum_{\gamma} \sum_{i \in \mathbf{P}^{g, \gamma}} S S I_{i}\left(\mathbf{P}^{g, \gamma}\right) .
$$

[^11]To see how the $S S I$ is applied consider the panel on the left-hand side of Figure 5, which corresponds to the motivating example in Echenique and Fryer (2007). The society in City 1 is composed of two groups, blacks and whites. Each dot represents one individual. It is also assumed that individuals only interact with their horizontal and vertical neighbors. So, individual (A,1) spends $50 \%$ of her time with each (A,2) and (B,1) each. The subgraph $\mathbf{P}^{\text {blacks }}$ in City 1 consists therefore of two connected components $\mathbf{P}^{\text {blacks,1 }}$ and $\mathbf{P}^{\text {blacks,2 }}$.


Figure 5: Calculation of the $S S I$.

The SSI for the blacks is determined by taking a weighted average over the spectral radii of the two black connected components. The upper part of Table 1 shows that $S S I\left(\mathbf{P}^{\text {blacks,1 }}\right)=$ 0.72 and $S S I\left(\mathbf{P}^{\text {blacks }, 2}\right)=0.25$. Since $80 \%$ of the blacks reside in component 1 and $20 \%$ in component 2 , the segregation of the blacks is $S S I\left(\mathbf{P}^{\text {blacks }}\right)=0.8 \cdot 0.72+0.2 \cdot 0.25=0.63$.

| Components |  |  | Blacks | $S S I$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City 1 |  |  |  |  |  |  |  |  |
| Component 1 | $(\mathrm{~B}, 1)$ | $(\mathrm{B}, 2)$ | $(\mathrm{C}, 1)$ | $(\mathrm{C}, 2)$ | $(\mathrm{D}, 1)$ | $(\mathrm{D}, 2)$ | $(\mathrm{D}, 3)$ | $(\mathrm{D}, 4)$ |
|  | 0.87 | 0.62 | 1.26 | 0.92 | 0.93 | 0.75 | 0.29 | 0.10 |
| Component 2 | $(\mathrm{B}, 5)$ | $(\mathrm{C}, 5)$ |  |  | $\mathbf{0 . 7 2}$ |  |  |  |
|  | 0.25 | 0.25 |  |  | $\mathbf{0 . 2 5}$ |  |  |  |
| Weighted Average |  |  |  |  | $\mathbf{0 . 6 3}$ |  |  |  |

City 2

| Component | $(\mathrm{B}, 1)$ | $(\mathrm{B}, 2)$ | $(\mathrm{C}, 1)$ | $(\mathrm{C}, 2)$ | $(\mathrm{D}, 1)$ | $(\mathrm{D}, 2)$ | $(\mathrm{D}, 3)$ | $(\mathrm{D}, 4)$ | $(\mathrm{B}, 5)$ | $(\mathrm{C}, 5)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1.09 | 0.78 | 1.58 | 1.14 | 1.16 | 0.93 | 0.37 | 0.13 | 0.00 | 0.00 | $\mathbf{0 . 7 2}$ |

Table 1: Calculation of the SSI.
To see that the $S S I$ is not continuous in the entries of $\mathbf{P}^{\text {blacks }}$ suppose that the black
individuals ( $\mathrm{D}, 4$ ) and ( $\mathrm{C}, 5$ ) start communicating with each other $1 \%$ of their respective times. It is irrelevant which neighbor(s) receive now relative less attention from ( $\mathrm{D}, 4$ ) and (C,5), for the sake of the example just suppose that this extra time is taken away from the white neighbors. This small change in the network leads to City 2 on the right-hand side of Figure 5, which has now a single component. As it can be seen in the lower part of Table 1, the effect of this change on the segregation of the blacks is substantial, $S S I\left(\mathbf{P}^{\text {blacks }}\right)$ increases from 0.63 to 0.72 . In particular, the spectral radius of the integrated component converges to the larger of the two spectral radii. Finally, one also sees that the segregation levels of individuals $(B, 5)$ and $(C, 5)$ are now very close to 0 , whereas they were 0.25 in City 1 .

More formally, $S S I\left(\mathbf{P}^{g}\right)$ is discontinuous in $\mathbf{P}^{g}$, as opposed to what is stated in Proposition 5 in Echenique and Fryer (2007). This becomes evident when two connected components of $\mathbf{P}^{g}$ are merged or when one component of $\mathbf{P}^{g}$ is split up. ${ }^{17}$ The reason for the discontinuity is the component additivity attached to the measure: The $S S I$ of a connected component $\mathbf{P}^{g, \gamma}$ of $\mathbf{P}^{g}$ is defined as the spectral radius of the submatrix $\mathbf{P}^{g, \gamma}$, but the spectral radius of $\mathbf{P}^{g}$ -which is continuous in $\mathbf{P}^{g}$ - can generally not be averaged over its components. In fact,

$$
\rho\left(\mathbf{P}^{g}\right)=\max _{\gamma} \rho\left(\mathbf{P}^{g, \gamma}\right)
$$

where $\rho(\cdot)$ denotes the spectral radius. So, the property of component additivity sacrifices continuity. To restore the continuity of the $S S I$, one would therefore have to drop this component additivity. However, in this case, the segregation of group $g$ would be equal to the largest (and not the average) segregation of all components of $\mathbf{P}^{g}$, and the segregation levels in all other components of $\mathbf{P}^{g}$ would be zero. So, if additivity is dropped, one would still need to explain why this asymmetric outcome is a reasonable measure of segregation. ${ }^{18}$

There are several circumstances that can trigger the discontinuity problem of the $S S I$. The reader should observe first that the disconnectedness of a group inside a social network causes the $S S I$ to be discontinuous. Thus, even if a city or social network is connected, the

[^12]assumption that all groups within this network are connected is possibly violated. Second, if several individuals live in a node, the majority rule employed in Echenique and Fryer (2007) is a sensible choice to determine the representative individual of a census tract. However, one cannot exclude the possibility that the majority group in a node changes (even though the U.S. Census data revealed a considerable margin in most districts) and that this causes two or more smaller components to merge into one big component or vice versa. Third, even if no particular representativeness rule has to be considered because there is only a single individual in each node, it could happen that one individual changes her location in the spatial network, thus changing the network structure of her group by merging previously separated components or separating previously integrated components. Hence, the movement of a single individual can provoke a significant variation in the segregation of her group. Finally, the definition of adjacent nodes in a spatial network is also likely to become problematic if the measure is not continuous. Echenique and Fryer (2007) reasonably assume that two census tracts are connected whenever their centroids are not more than one kilometer away from each other. Yet, a small change in this distance could potentially merge or separate components of some groups, triggering an abrupt change in the segregation of these groups. Even though it turns out that the application to the U.S. Census in Echenique and Fryer (2007) is robust with respect to this kind of variation in the network, one cannot exclude the possibility that difficulties appear in future applications with different datasets.

To conclude we point out that $\sigma_{g}$ and $\bar{\sigma}_{g}$ are continuous in all their arguments. In particular, continuity with respect to $\alpha$ and $\mathbf{P}$ follows from the fact that $\mathbf{P}$ is stochastic and that $|\alpha|<1$. Moreover, our measures are quite stable in applications since we are choosing values for $\alpha$ well below 1. Finally, the next proposition provides an upper bound to the change in the segregation index when connections are modified. For that, given two cities $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and $C^{\prime}=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}^{\prime}\right\rangle$ with a common distribution of individuals over nodes, let $U$ be the subset of nodes whose connection change across the two cities; that is, $U=\left\{i \in M: p_{i, j} \neq p_{i, j}^{\prime}\right.$ for some $\left.j \in M\right\}$.

Proposition 5. The change in segregation index between $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and $C^{\prime}=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}^{\prime}\right\rangle$ is bounded above by

$$
\left|\sigma_{g}\left(C^{\prime}, \alpha\right)-\sigma_{g}(C, \alpha)\right| \leq \max _{i \in M}\left\{c_{g, i}\right\} \frac{2 \alpha}{1-\alpha} \sum_{j \in U} w_{g, j} .
$$

Proof. This follows from Theorem 6.5.1 in Langville and Meyer (2006) and Proposition 3.

## 5 Applications

### 5.1 Residential Segregation in Spain

We next apply the segregation index to the Spanish census tract data from January 2009. Among the developed countries Spain is particularly interesting to look at because the country attracted a lot of immigrants from many different parts of the world. During the boom years in the beginning of the century it was easy for the young South Americans to find a job in the construction or the (private) service sector because they were relatively cheaper to hire and had the advantage of speaking the same native language. But also immigrants from the Eastern European countries that recently entered the European Union or Africa were attracted by the vast job opportunities in the labor market. These combined effects led to the situation that more than $10 \%$ of the 45 million residents in Spain in 2009 were foreigners.

Table 3 in the Appendix B presents the population shares of 27 nationalities in Spain. ${ }^{19}$ It can be seen that the Romanians form the largest foreign group with $1.76 \%$ of the total population followed by the Moroccans who account for $1.56 \%$ of the residents. The high number Moroccans in Spain is of no surprise given their long tradition in the country. Next are Ecuador $(0.93 \%)$ and Colombia ( $0.65 \%$ ). The Nigerians form the smallest foreign group $(0.09 \%)$ for which we have data.

The Spanish territory is officially divided into 52 provinces, 47 of those are on the Iberian Peninsula. The remaining ones are the Balearic Islands in the Mediterranean Sea, the Canary

[^13]Islands in the Atlantic Ocean (2 provinces), and the autonomous cities Ceuta and Melilla in North Africa. We abstain from incorporating Ceuta and Melilla in our analysis because they are too small - each of the two cities has only about 75,000 residents, and very few of them are non-Africans. As of January 2009, the National Statistical Institute of Spain (INE) divides the 50 main provinces into a total of 35,757 census tracts. The mean number of residents per census tract is $1,268.98$, the corresponding standard deviation is 625.74. As in Echenique and Fryer (2007), we use the geographical location of the centroids of the census tracts to derive the network. In particular, we define two census tracts to be connected if the distance between their centroids is less than 400 meters. A node has then on average 4.84 connections. The corresponding standard deviation is 5.48. Also, there are 16,908 isolated nodes. ${ }^{20}$ In order to make consistent comparisons with the homophily index (see Proposition 2 ), we set the transition probabilities equal to

$$
p_{i, j}=\frac{a_{i, j} n_{j}}{\sum_{k \in M} a_{k} n_{k}},
$$

which means than the transition probability to node $j$ is proportional to the total population in census tract $j$. Observe that our results remain identical if we choose $p_{i, j}=1 / a_{i}$.

### 5.1.1 Results

We first report on the normalized segregation index $\bar{\sigma}_{g}(C, 0.85)$ for all provinces; that is, $C$ is defined by the borders of the provinces. ${ }^{21}$ Recall that only the normalized measure is invariant to the relative group sizes, which is a crucial property if one wants to compare the segregation of different nationalities.

We can see from Figure 6 that the segregation index is rather low in some parts of the

[^14]

Figure 6: Normalized segregation in Spain by provinces as of January 2009 for $\alpha=0.85$ and a neighborhood radius of 400 meters. The names of the different provinces can be identified with the help of Tables 5 in Appendix B.
autonomous communities of Galicia (provinces 15, 27, and 32), Asturias (province 33), and the Basque Country (provinces 01, 20, and 48) that are all in northern part of Spain touching the Cantabrian Sea and the Atlantic Ocean. Also, some parts of Andalusia such as Cadiz, Cordoba, Jaén, and Seville (provinces 11, 14, 23, and 41) have a segregation index that lies between 1.00 and 1.10. A substantial portion of the country has a segregation index between 1.11 and 1.20. The central region close to the capital Madrid (province 28), the second biggest city of Barcelona (province 08), the coastal sides of Alicante (province 03) and Murcia (province 30), the Balearic and the Canarian islands (provinces 07, 35, and 38), as well as Salamanca and Badajoz that touch the Portuguese border (provinces 10 and 37) have a moderate segregation index. The segregation index takes high values within other provinces of the autonomous community of Catalonia in northeastern part of the country (for example provinces 17 and 43) and Teruel (province 44). It is highest in Almería (province 04).

Figure 6 uncovers how segregated different parts of the country are, but so far we have
not analyzed which groups are causing the results we see. To say it in different words, we still have to investigate which groups are, on average, more segregated. We detail on this by calculating the normalized segregation index for each of the 27 groups in the whole country; that is, $C$ consists now of all 35,757 census tracts. Again, $\alpha=0.85$.


Figure 7: Normalized segregation in Spain by groups as of January 2009 for $\alpha=0.85$ and a neighborhood radius of 400 meters. The ordering of the different groups corresponds to that in Table 3.

It can be seen in Figure 7 that the Spanish are by far the least segregated group. Since the normalized segregation index for group $g$ takes a value of one if $c_{g, i}=n_{g} / n$ for all nodes, this finding supports the interpretation that the Spanish are very evenly distributed over all census tracts. Also, since the normalized segregation index is considerably larger than one for all other nationalities, the foreign groups show the general tendency to stick together.

The by far most segregated immigrants are the Pakistanis, $\bar{\sigma}_{P K}($ Spain, 0.85$)=23.56$, which implies that interactions within this group occur about 23 times more often than if their members were uniformly spread. Immigrants from Russia and African countries like Nigeria and Senegal have a normalized segregation index between 10-15. The immigrants of the South American countries are the most integrated ones, their segregation index ranges from 2.28 for the Colombians to 5.99 for the Uruguayans. Finally, we can also say why Almería is very segregated. In Almería, $4.3 \%$ of the population are Romanians (their segregation index in this province is 2.67 ) and $5.9 \%$ are Moroccans (their segregation index in this province is 3.94). Consequently, the segregation in Almería is high because two of the largest groups of
immigrants are overrepresented in this province.

### 5.1.2 Network Effects

One important question at this point is whether the incorporation of the network as an additional dimension adds to our understanding of segregation. To investigate this, one has to compare the normalized segregation index when $\alpha=0.85$ with the situation when $\mathbf{P}=\mathbf{I}$ and the measure reduces to the normalized isolation index. This comparison will in particular reveal which nationalities cluster in neighborhoods close to each other. To see this, imagine that the isolation index of group $g$ is 1 (no individual outside of $g$ is living in a census tract with members of $g$ ). There are now two opposite scenarios to be investigated as the network is introduced: The census tracts with inhabitants of group $g$ are spread evenly across the city or they are clustered in one particular area. If the members of $g$ live in evenly spread census tracts, new connections to neighboring census tracts will increase the interactions with members outside of $g$ and the segregation will decrease. If, on the other hand, $g$ forms a clustered group, the segregation of the group will also decrease, but the effect will now be smaller because the new interactions are more likely to be intra-group related as the neighboring nodes are populated by group $g$ as well. Hence, the decrease in segregation due to an increase in $\alpha$ is lower for clustered groups.


Figure 8: Network effects (in proportions) in Spain by groups as of January 2009 for a neighborhood radius of 400 meters. The ordering of the different groups corresponds to that in Table 3.

Figure 8 calculates the degree by which the measure decreases when the network is con-
sidered; that is, we calculate $1-\bar{\sigma}_{g}(C, 0.85) / \bar{I}_{s}(C)$. One sees that the network effect is substantial for some groups but negligible for others. The clearest effect can be identified for the Pakistanis and the Nigerians. Considering the actual network $\mathbf{P}$ with $\alpha=0.85$ reduces the normalized isolation index of these groups by $40-60 \%$. However, it is not only the relative changes that matter. For example, the Russians have the fourth highest normalized isolation index $\left(\bar{I}_{R}(C)=13.26\right)$, while they are the second most segregated group when the network matters and $\alpha=0.85$. Actually, the network effects for the Russians are rather low because the segregation index does not change much when the network is incorporated. As mentioned before, the differences in the change of the measure is due to clustering. The Russians are overrepresented in the coastal sides of Alicante (province 03), Almería (province 04), Girona (province 17), Málaga (province 29), and Tarragona (province 43), whereas the Pakistanis are spread over many cities, even though they live very concentrated within these cities. ${ }^{22}$


Figure 9: Proportion of the network effect that is due to connections beyond immediate neighbors in Spain by groups as of January 2009 for a neighborhood radius of 400 meters. The ordering of the different groups corresponds to that in Table 3.

Finally, Figure 9 analyzes which part of the network effect is due to a change from $\alpha=0$ (the normalized homophily index) to $\alpha=0.85$. In fact, the ratio between $\bar{\sigma}_{g}(C, 0)-\bar{\sigma}_{g}(C, 0.85)$ and $\bar{I}_{g}(C)-\bar{\sigma}_{g}(C, 0.85)$ shows which percentage of the clustering is due to connections beyond

[^15]immediate neighbors. The data clearly reveals that the normalized homophily index already captures most of the network effects. Nevertheless, there are several group of immigrants for which higher-order relations explain between $20 \%$ and $40 \%$ of the overall network effect (e.g., French, Moroccans, Nigerians, Chinese, and Pakistanis). We also note that almost $40 \%$ of the clustering of Spanish residents is explained by higher-order relations.

### 5.1.3 Correlation with the $S S I$

Next, we calculate the correlation between the $S S I$ and the segregation index. Recall that the basic idea behind the $S S I$ is that individuals interact with their neighbors. If one node corresponds to one individual, the set of neighbors naturally includes all nodes an individual is connected to. We allow for multiple individuals in the same neighborhoods, but the two frameworks become comparable if one defines the set of neighbors as all those individuals that can be reached within one step. The within group substochastic interaction matrix $\mathbf{P}^{g}$ for group $g$ is thus defined as

$$
p_{i, j}^{g}=\frac{a_{i, j} n_{g, j}}{\sum_{j \in M} a_{i, j} n_{j}}
$$

Hence, an individual from group $g$ living in neighborhood $i$ interacts with all $g$-members that can be reached within one step with equal probability. As before, the $S S I$ of group $g$ can then be defined as

$$
S S I\left(\mathbf{P}^{g}\right)=\sum_{\gamma} d_{g}^{\gamma} \cdot S S I\left(\mathbf{P}^{g, \gamma}\right)
$$

Since the spectral radius for each connected component can be set equal to the weighted average of the corresponding eigenvector, we obtain that

$$
S S I\left(\mathbf{P}^{g}\right)=\sum_{\gamma} d_{g}^{\gamma} \sum_{i \in \mathbf{P}^{g, \gamma}} d_{g, i}^{\gamma} \cdot S S I_{i}\left(\mathbf{P}^{g, \gamma}\right)
$$

where $d_{g, i}^{\gamma}=n_{g, i} / \sum_{j \in \mathbf{P}^{g, \gamma}} n_{g, j}$ is the fraction of individuals of group $g$ from component $\gamma$ who live in neighborhood $i$. Rewriting this equation as

$$
S S I\left(\mathbf{P}^{g}\right)=\sum_{\gamma} \sum_{i \in \mathbf{P}^{g, \gamma}} d_{g}^{\gamma} \cdot d_{g, i}^{\gamma} \cdot S S I_{i}\left(\mathbf{P}^{g, \gamma}\right)=\sum_{i \in M} d_{g, i} \cdot S S I_{i}\left(\mathbf{P}^{g, \gamma(i)}\right)
$$

shows that the $S S I$ can be envisioned as a weighted average over all neighborhoods. Since the $S S I$ is not invariant to group sizes, we have to compare it to the size dependent version of the segregation index, which according to Proposition 1 is equal to $\sigma_{g}(C, \alpha)=\sum_{i \in M} d_{g, i} v_{g, i}$. Consequently, we proceed by calculating the correlation between the vectors $\mathbf{v}_{g}=\left(v_{g, i}\right)_{i \in M}$ and $\left(S S I_{i}\left(\mathbf{P}^{g, \gamma(i)}\right)\right)_{i \in M}$ of size 35,757 corresponding to Spain as a whole.


Figure 10: Correlation between $\sigma_{g}(C, 0.85)$ and the $S S I$ in Spain by groups as of January 2009 for a neighborhood radius of 400 meters. The ordering of the different groups corresponds to that in Table 3.

Figure 10 shows a positive correlation between the $S S I$ and the segregation index for all nationalities. For several groups, the correlation ranges between 0.20 and 0.40 . The correlation is rather small for immigrants from Morocco, Chile and Bolivia. Consequently, the data reveals that the $S S I$ and the segregation are rather different in their structure even though they both relate to the probability that two members from the same group meet. This is because the measures use a different underlying network structure to determine this kind of probability (see Footnote 16).

### 5.2 Segregation in Scientific Publications

### 5.2.1 Model

Using citation data from scientific publications, we now show that the model of residential segregation can be readily applied to a wide range of socioeconomic questions. Let the set of nodes $M$ now be equal to the set of scientific journals. The set of all fields $G$ partitions $M$. The number of articles published by journal $i \in M$ constitutes the population $n_{i}$ at node $i$.

Since each journal is assumed to belong to exactly one field, $c_{g, i}=1$ if journal $i$ belongs to field $g \in G$, and $c_{g, i}=0$ otherwise. The total number of articles published by journals from field $g$ is then equal to $n_{g}=\sum_{i \in M} c_{g, i} n_{i}$. Similarly, $d_{g, i}=\left(c_{g, i} \cdot n_{i}\right) / n_{g}$ is the fraction of all articles from journals belonging to field $g \in G$ that are published by journal $i$. We can see that $d_{g, i}=0$ whenever journal $i$ does not belong to field $g$.

Let $l_{i, j}$ be the number of citations from articles in journal $i$ to articles in journal $j$. The total number of articles cited by articles in journal $i$ is denoted by $l_{i}=\sum_{j \in M} l_{i, j}$. Setting $p_{i, j}=l_{i, j} / l_{i}$ induces the stochastic matrix $\mathbf{P}$ with the following interpretation: Imagine a researcher who is currently reading an article from journal $i \in M$. The matrix $\mathbf{P}$ then indicates which journal the researcher is going to read next (following some citation from the current article). ${ }^{23}$ If the probability that the random-walk continues after the first step is $0 \leq \alpha<1$ - the interpretation of $\alpha$ is akin to that in the model of residential segregation -, the matrix $\mathbf{Q}=(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P}$ can be derived in exactly the same way as before. In particular, $p_{i, j}$ corresponds to the probability that the researcher stops at journal $j$ given that her random-walk started at journal $i$.

Given the tuple $C=\left\langle N, M, G,\left(n_{g, i}\right)_{g \in G, i \in M}, \mathbf{P}\right\rangle$ and the continuation probability $\alpha \in$ $[0,1)$, the segregation index $\sigma_{g}(C, \alpha)$ of field $g \in G$ measures the probability that a researcher who starts reading a randomly chosen article from a journal from field $g$ (that is, each journal $i$ from field $g$ is taken with probability $d_{g, i}$ ) and follows the citations therein, stops reading an article from a journal that also belongs to field $g \in G$. Formally, by Proposition 3, $\sigma_{g}(C, \alpha)=\mathbf{w}_{\mathbf{g}}^{\mathbf{\top}} \mathbf{P} \mathbf{c}_{\mathbf{g}}$, where $\mathbf{w}_{\mathbf{g}}$ is the PageRank vector of field $g$.

### 5.2.2 Results

We use citation data from the 2010 Journal Citation Reports for a five year window. It includes citations made in 2010 to articles published in 2005-2009. The set $M$ consists of 140 leading Economics journals according to the measures of Impact Factor ${ }^{\text {TM }}$ and Article

[^16]Influence ${ }^{\mathrm{TM}}$. We classify the journals in 18 fields following the CEFAFE-EU ranking from the University of Évora, Portugal. ${ }^{24}$ For each of the 18 fields, we compute both the homophily index $h_{g}(C)=\sigma_{g}(C, 0)$, which indicates the percentage of citations that stay within a field, and the segregation index $\sigma_{g}(C, 0.85)$. The results are presented in Table 2.

| Field ID | \# Journals | $n_{g} / n$ |  | $h_{g}(C)$ |  | $\sigma_{g}(C, 0.85)$ |  | $\bar{h}_{g}(C)$ |  | $\bar{\sigma}_{g}(C, 0.85)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| AccAud | 1 | 0.004 | (17) | 0.000 | (17) | 0.011 | (14) | 0.000 | (16) | 2.617 | (6) |
| AgrEnvEn | 17 | 0.120 | (2) | 0.530 | (2) | 0.163 | (5) | 4.414 | (9) | 1.358 | (14) |
| DevTrans | 11 | 0.062 | (7) | 0.341 | (7) | 0.118 | (7) | 5.468 | (7) | 1.887 | (9) |
| EconStat | 9 | 0.055 | (8) | 0.474 | (5) | 0.164 | (4) | 8.636 | (3) | 2.983 | (4) |
| FinIns | 11 | 0.094 | (3) | 0.691 | (1) | 0.351 | (2) | 7.356 | (4) | 3.742 | (3) |
| GenEcon | 33 | 0.288 | (1) | 0.479 | (4) | 0.458 | (1) | 1.662 | (14) | 1.589 | (12) |
| HistPolMet | 3 | 0.011 | (13) | 0.365 | (6) | 0.084 | (9) | 31.999 | (1) | 7.343 | (1) |
| HRM | 1 | 0.004 | (17) | 0.000 | (17) | 0.001 | (18) | 0.000 | (16) | 0.170 | (18) |
| InnovEntrSB | 2 | 0.009 | (14) | 0.036 | (13) | 0.009 | (15) | 4.097 | (11) | 1.054 | (16) |
| IO | 6 | 0.032 | (10) | 0.193 | (11) | 0.061 | (10) | 5.799 | (6) | 1.846 | (10) |
| LaborHealth | 11 | 0.079 | (4) | 0.528 | (3) | 0.207 | (3) | 6.672 | (5) | 2.622 | (5) |
| Law | 2 | 0.006 | (15) | 0.029 | (14) | 0.012 | (13) | 4.306 | (10) | 1.741 | (11) |
| Macro | 10 | 0.074 | (5) | 0.222 | (10) | 0.111 | (8) | 3.000 | (12) | 1.497 | (13) |
| PubEcon | 5 | 0.049 | (9) | 0.121 | (12) | 0.051 | (12) | 2.575 | (12) | 1.095 | (15) |
| Sector | 1 | 0.001 | (18) | 0.000 | (17) | 0.004 | (17) | 0.000 | (16) | 3.927 | (2) |
| Socio | 3 | 0.016 | (12) | 0.001 | (15) | 0.007 | (16) | 0.001 | (15) | 0.411 | (17) |
| Theory | 9 | 0.070 | (6) | 0.331 | (8) | 0.143 | (6) | 4.749 | (8) | 2.057 | (8) |
| UrbSpaReg | 5 | 0.024 | (11) | 0.264 | (9) | 0.059 | (11) | 10.982 | (2) | 2.467 | (7) |

Table 2: Field, number of journals per field, article shares, homophily index (non-normalized and normalized), and segregation index (non-normalized and normalized) for 18 different areas in Economics using the citation data from 2010 for 140 economics journals. In parentheses, we present the corresponding ordinal rankings. The abbreviations of the fields are explained in Table 4 in Appendix B.

One can see that the size dependent measures $h_{g}(C)$ and $\sigma_{g}(C, 0.85)$ yield very similar results. In fact, the set of the five most segregated fields is identical in both cases, and the corresponding rank correlation is very high (0.942). Also, these two rankings resemble very much the ranking that one obtains if the fields are simply ordered according by their relatives sizes. One should look at the normalized measures to filter out this effect.

The last two columns show that the set of the five most segregated fields is still very much the same for both indices, however there are important changes with respect to the nonnormalized measures. For the non-normalized measures, General Economic, which contains

[^17]all general interest journals and is with 33 journals by far the biggest field, is among the most segregated fields. Yet, it is far less segregated for the normalized measures, which intuitively makes sense. Similarly, Economic History is not much segregated for the size dependent measures but by far the most segregated field if the normalized measures are applied. Also note that the rank correlation between the normalized homophily index and the normalized segregation index for $\alpha=0.85$ is 0.554 . This shows that there is some clustering beyond immediate neighbors that is explained by the segregation index $\sigma$ : Even if a journal from field $g$ does not cite a journal from the same field, it may cite journals from other fields that usually cite journals from $g$.

This type of higher order clustering is exactly captured by the difference between $\bar{h}_{g}(C)$ and $\bar{\sigma}_{g}(C, 0.85)$, and it is this difference that allows us to uncover some interesting citation patterns. For example, concentrating on the four small fields with a very low normalized homophily index - AccAud, HRM, Sector, and Socio - , one sees that $\bar{\sigma}_{g}(C, 0.85)-\bar{h}_{g}(C)$ is large for Sector and AccAud but low for HRM and Socio. Hence, while neither of these four fields has many self citations, there are cycles for Sector and AccAud (these journals cite journals from other fields that then cite back) that do not occur to this large extent for HRM and Socio. Also, these are the only four fields for which the segregation raises as the expected walk length increases, which makes us conclude that these kind of cycles play only a minor/no importance in all other fields.

Among the fields that reduce their segregation when indirect citations are taken into account, General Economics (GenEcon) and Urban, Spatial, Regional, and Transport Economics (UrbSpaReg) deserve some special attention. While GenEcon does not show any network effects (the normalized fraction of field-self-citations is in both cases 1.6 times larger than that obtained from the uniform distribution), UrbSpaReg turns out to have a lot of field-self-citations (roughly 11 times more if compared to the uniform distribution), yet this fraction is reduced by $75 \%$ when indirect citations are considered as well. So, journals from other fields that are cited by UrbSpaReg do not have the tendency to cite back. This is to say that UrbSpaReg has a rather high homophily index but a normalized segregation index
when $\alpha=0.85$ that compares to that of many other fields.

## $6 \quad$ A Model of Time Investment

We now adapt the model of Currarini et al. (2009) to show that the segregation index $\sigma_{g}$ is directly related to the equilibrium outcome of a game in which individuals have to decide how to spend their time. ${ }^{25}$ We depart from the spatial network defined through the matrix $\mathbf{A}$ on the set of nodes $M=\{1,2, \ldots, m\}$. We assume that $\mathbf{A}$ is symmetric and that $a_{i}>0$. There is a set of groups/cultures $G$. At each moment in time, a continuum of individuals of mass $n_{g, i}$ of group $g \in G$ arrives (is born) in neighborhood $i \in M$. We say that an individual is an $i-$ citizen if she is born in neighborhood $i$, and an $g$-member if she belongs to group $g$.

Each individual decides how much time to invest in meeting other cultures. We consider an unbiased payoff function that does not depend on the type of the individual so that we can identify how the spatial setting alone shapes separation in equilibrium. Thus, let $t_{g, i} \geq 0$ be the time invested by an $i$-citizen in culture $g \in G$, independently of her group. The total time invested by an $i-$ citizen is $t_{i}=\sum_{g \in G} t_{g, i}$. It is the time an individual from neighborhood $i$ spends in the matching process, interacting with other citizens who also invest time. After time $t_{i}$ expires, the $i$-citizen exits the process.

Meetings between individuals are only possible if they live in neighboring census tracts. In particular, an $i$-citizen meets a $j$-citizen with probability $p_{i, j}=a_{i, j} / a_{i}$; that is, the transition probability is uniform. For all neighborhoods $i, j \in M$ and all groups $g, s, u \in G$, we write $[(i, g) \rightarrow(j, s)]^{u}$ to denote the event in which an $i$-citizen who invests in culture $g$ meets a $j$-citizen who is an $u$-member and invests in culture $s$. Note that the neighborhoods $i$ and $j$, or the groups $g, s$ and $u$ may coincide or not. A mutual-interest-based meeting of an $i-$ citizen with a $j$-citizen (I-meeting from now on) is a meeting of the form $[(i, g) \rightarrow(j, g)]^{\bullet}$; that is, an $i$-citizen meets a $j$-citizen, and they are investing in the same culture. Let $\tau_{i, j}^{g}$ be the total time an $i$-citizen spends in I-meetings related to culture $g$ with $j$-citizens. A

[^18]cultural meeting of an $i$-citizen with a $j$-citizen ( C -meeting from now on) is a meeting of the form $[(i, g) \rightarrow(j, \cdot)]^{g}$; that is, an $i$-citizen who invests in culture $g$ meets an $j$-citizen who is a $g$-member. Let $\bar{\tau}_{i, j}^{g}$ be the total time an $i$-citizen spends in C -meetings with $j$-citizens who are $g$-members. Finally, note that the meeting $[(i, g) \rightarrow(j, g)]^{g}$ is both $I$ and $C$.

We assume that individuals only benefit from meetings that are I or C. First, the $i-$ citizen gets $A_{1} \geq 0$ for each unit of time in the I-meeting $[(i, g) \rightarrow(j, g)]^{\bullet}$. Second, each unit of time in the C-meeting $[(i, g) \rightarrow(j, \cdot)]^{g}$ produces a benefit of $A_{0}>0$ for the $i-$ citizen. In case a meeting is both I and C , the $i$-citizen gets $A_{0}+A_{1}$ per unit of time in the meeting. The total benefits of an $i$-citizen are then equal to

$$
B_{i}\left(\left(t_{g, j}\right)_{g \in G, j \in M}\right)=\sum_{g \in G} \sum_{j \in M}\left(A_{0} \bar{\tau}_{i, j}^{g}+A_{1} \tau_{i, j}^{g}\right)
$$

Costs are supposed to be additively separable with respect to the time spent in the different cultures. Also, they are identical for all cultures and independent of the group:

$$
C_{i}\left(\left(t_{g, i}\right)_{g \in G}\right)=\frac{D}{2} \sum_{g \in G} t_{g, i}^{2}
$$

where $D>0$. The utility of an $i$-citizen is then

$$
U_{i}\left(\left(t_{g, j}\right)_{g \in G, j \in M}\right)=\sum_{g \in G}\left(A_{o} \sum_{j \in M} \bar{\tau}_{i, j}^{g}+A_{1} \sum_{j \in M} \tau_{i, j}^{g}\right)-\frac{D}{2} \sum_{g \in G} t_{g, i}^{2}
$$

One sees that the incentives to express interest in a particular culture $g$ are determined by three factors: The likelihood of meeting an $g$-member (the compositional effect that produces a payoff of $A_{0}$ ), the chance of finding other citizens who are also interested in culture $g$ (the complementarity effect that produces a payoff of $A_{1}$ ), and the parameter $D$ of the cost function. Next, and in order to be able to calculate the total time spent in different meetings, we have to make some assumptions on the probability that a particular meeting occurs. We follow Currarini et al. (2009) and impose an unbiased process. Formally, the probability $\rho_{i, j}^{g}$ that an $i$-citizen has an $I$-meeting related to culture $g$ with a $j$-citizen is

$$
\rho_{i, j}^{g} \equiv p_{i, j} \frac{p_{j, i}\left(n_{j} t_{g, j}\right)}{p_{j, i} \sum_{k \in G} n_{j} t_{k, j}}=p_{i, j} \frac{t_{g, j}}{t_{j}}
$$

that is, the probability is determined by the fraction of time $j$-citizens spend in culture $g$. Similarly, the probability $\bar{\rho}_{i, j}^{g}$ that an $i$-citizen has a $C$-meeting with an $g$-member from neighborhood $j$ is driven by the size of group $g$ at $j$ :

$$
\bar{\rho}_{i, j}^{g} \equiv p_{i, j} \frac{p_{j, i}\left(n_{g, j} t_{j}\right)}{p_{j, i}\left(n_{j} t_{j}\right)}=p_{i, j} \frac{n_{g, j}}{n_{j}}=p_{i, j} c_{g, j}
$$

We then find that $\tau_{i, j}^{g}=\rho_{i, j}^{g} \cdot t_{g, i}=p_{i, j} \cdot t_{g, i} \cdot t_{g, j} \cdot 1 / t_{j}$ and $\bar{\tau}_{i, j}^{g}=\bar{\rho}_{i, j}^{g} \cdot t_{g, i}=p_{i, j} \cdot t_{g, i} \cdot c_{g, j}$, respectively. Using this information, the utility function of an $i$-citizen becomes

$$
\begin{equation*}
U_{i}\left(\left(t_{g, j}\right)_{g \in G, j \in M}\right)=\sum_{g \in G}\left(A_{o} t_{g, i} \sum_{j \in M} p_{i, j} c_{g, j}+A_{1} t_{g, i} \sum_{j \in M} p_{i, j} \frac{t_{g, j}}{t_{j}}\right)-\frac{D}{2} \sum_{g \in G} t_{g, i}^{2} \tag{1}
\end{equation*}
$$

We study the simultaneous move game with utilities given by (1) and where each $i-$ citizen chooses the investment times $\left(t_{g, i}\right)_{g \in G} \geq \mathbf{0}$. Given the investment times from all individuals, the resulting meetings are balanced if the following three conditions are satisfied:

- Total balancedness: The time $i$-citizens meet $j$-citizens is equal to the time $j$-citizens meet $i$-citizens.
- I-balancedness: The time $i$-citizens have $I$-meetings related to culture $g$ with $j$-citizens is equal to the time $j$-citizens have $I$-meetings related to culture $g$ with $i$-citizens.
- $C$-balancedness: The time $i$-citizens have $C$-meetings with $g$-members from node $j$ is equal to the time that $g$-members from node $j$ spend in these meetings with $i$-citizens.

Balancedness states that every $i$-citizen who invests $t_{i}$ units of time has bilateral meetings during this time. Due to the unbiased setting, all three conditions are equivalent and reduce to $n_{i} \cdot p_{i, j} \cdot t_{i}=n_{j} \cdot p_{j, i} \cdot t_{j}$ (for details, see the proof of Theorem 1 in Appendix A). It is also important to note that balancedness can only be ensured in equilibrium if we impose some additional restrictions on the structure of the network. For this reason, we assume from now on that for all $i, j \in M, n_{i} / n_{j}=a_{i} / a_{j}$; that is, the mass of newborns in neighborhood $i \in M$ is proportional to its number of neighbors $a_{i}$. Only then meetings with all neighbors are feasible. We nevertheless point out that this condition still gives us the freedom to choose any vectors of group concentrations $\left(c_{g}\right)_{g \in G}$.

We say that $\left(t_{g, i}^{*}\right)_{i \in M, g \in G}$ is a steady state equilibrium if $\left(t_{g, i}^{*}\right)_{i \in M, g \in G}$ is a Nash equilibrium of the simultaneous move game, meetings are balanced, and the inflow and outflow of individuals are equal at any given point in time. The following result states that in the unique steady state equilibrium, the average time invested by $g$-members in their own culture, $\bar{t}^{g}$, is proportional to the segregation index of group $g$.

Theorem 1. For all groups $g \in G$,

$$
\bar{t}^{g} \equiv \frac{1}{n_{g}} \sum_{i \in M} n_{g, i} t_{g, i}^{*}=\frac{A_{0}+A_{1}}{D} \sigma_{g}\left(C, \frac{A_{1}}{A_{0}+A_{1}}\right)
$$

Proof. See Appendix A.

Observe that the relative magnitude of $A_{1} / A_{0}$ directly relates to the parameter $\alpha$. As $\alpha$ increases in the model of residential segregation, the complementarity effect in the game becomes stronger. We conclude with an example.

Example. Consider the city depicted in Figure 11.


Figure 11: Connections and arrival rates.

There are four neighborhoods and two groups. It is assumed that for all $i \in M, a_{i, i}=1$. The vectors of group concentration are equal to $\mathbf{c}_{\text {blacks }}^{\top}=(0,1,1,0)$ and $\mathbf{c}_{\text {whites }}^{\top}=(1,0,0,1)$. Since the steady state equilibrium is only balanced if the condition $n_{i} / n_{j}=a_{i} / a_{j}$ is met for all $i, j \in M$, we consider the arrival rates $n_{1}=n_{2}=3, n_{3}=4$, and $n_{4}=2$. Hence, in Figure 11 each dot indicates a continuum of individuals of mass 1 . Also, $\mathbf{d}_{\text {blacks }}^{\top}=(0,3 / 7,4 / 7,0)$ and $\mathbf{d}_{\text {whites }}^{\top}=(3 / 5,0,0,2 / 5)$. If $A_{0}=1, A_{1}=3$, and $D=2$, then $\alpha=0.75$. In this
case, the total time invested in the steady state is $t_{i}^{*}=2$ for all $i \in M$, and the average equilibrium investments are twice the segregation indices: $\bar{t}^{\text {blacks }}=2 \sigma_{\text {blacks }}(C, 0.75)=1.17$ and $\bar{t}^{\text {whites }}=2 \sigma_{\text {whites }}(C, 0.75)=0.83 .{ }^{26}$

Theorem 1 allows us to interpret the segregation index as the result of a game where individuals benefit from meetings. In the example, the blacks are more segregated because of the following game-theoretical interpretation. First, a black is more likely to meet blacks since the group is rather clustered $\left(h_{\text {blacks }}=4 / 7\right)$. Second, also a white is more likely to meet a black $\left(h_{w h i t e s}=2 / 5\right)$. This higher chance of meeting blacks for all individuals increases the compositional incentives to spend time with blacks. Third, complementarities further increase the incentives to spend time in black-related meetings. Finally, we also find that the whites spend more time in black-related than in white-related meetings (1.16 vs. 0.83 ). This is not surprising in a theoretical framework where individuals do not have any bias towards their own culture.

## 7 Conclusion

We have developed a new measure of residential segregation. In our theoretical model, the nodes of a network represent neighborhoods or census tracts, and links indicate which census tracts are adjacent in the urban space. It has also been assumed that multiple individuals from possibly different social groups can be located in the very same node. Using this information as the only primitive of our analysis, we have studied the following Markov chain: In the first period, an individual moves from her area of residence to a neighboring node. In each subsequent period, the individual advances from her current position in the network to an adjacent node with a given probability, or the process stops. The segregation index has then been defined as the probability that a randomly chosen individual from a given group meets an individual from the same social group in the node where her random-walk terminates.

We have shown in our analysis that the segregation index has several favorable aspects. First, the measure reduces to the isolation index in case the network is empty. Consequently,

[^19]the segregation index can be interpreted as a natural generalization of the isolation index to spatial networks. Second, in case the network is not empty and the exogenous probability that the random-walk stops is one, the only interactions that are taken into account are those between nodes that are direct neighbors, and the segregation index reduces to the homophily index introduced by Currarini et al. (2009). Third, the segregation index incorporates the idea that social groups that are located closer to the (relative) city center are more segregated everything else equal. In particular, the segregation index turns out to be proportional to the PageRank index applied by Google to determine the importance of webpages in the World Wide Web. Finally, the segregation index is a continuous function in the social ties. Indeed, the SSI suggested by Echenique and Fryer (2007), who have been the first to study a graphtheoretical model to develop a measure of segregation, fails to satisfy this important criterion.

In our empirical analysis, we have studied first the Spanish 2009 census tract data. The main result in this regard is that the province of Almeria on the Mediterranean coast is the most segregated area, mainly because two of the more segregated groups, the Romanians and the Morrocans, are highly overrepresented in these regions. Immigrants from Latin America, on the other hand, turn out to be very much integrated, an effect that may be related to the fact that these groups speak Spanish natively. We have also seen that clustering effects are important to understand the segregation of some of the some smaller nationalities like the Pakistanis and immigrants from African countries like Nigeria and Senegal, but not for the European communities.

Afterwards, we have indicated that our model residential segregation can be easily adapted to answer a wide range of empirical questions. To illustrate this, we have calculated the segregation of 18 different fields in Economics using citation data from 140 scientific publications. The difference between the normalized homophily index and the normalized segregation index found in the data indicates a substantial amount of higher-order clustering: Journals from field $g$ may not cite journals from the same field but journals from another field that cite journals from $g$.

Finally, in the last section of the paper, we rationalized the segregation index from a game-
theoretical point of view. We considered a model in which individuals arrive continuously at the nodes of an exogenous network and have to decide how much time to invest in the different groups/cultures (stay in the matching process). Using an unbiased utility function, we found that the equilibrium outcome of this induced game is related to the segregation index. In fact, it turned out that the average amount of time an individual from group $g$ invests in her own culture is directly proportional to segregation index.

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## Appendix A: Proofs

## Proof of Lemma 1

Consider $q_{i, j}$, which is the probability that a walk starting at node $i$ ends at node $j$. With probability $(1-\alpha)$ the walk has length one, and it will end at node $j$ with probability $p_{i, j}$. With probability $\alpha$, the walk continues following $i$ 's neighbors and it will reach node $j$ with probability $\sum_{k \in M} p_{i, k} q_{k, j}$. Thus, $q_{i, j}=(1-\alpha) p_{i, j}+\alpha \sum_{k \in M} p_{i, k} q_{k, j}$. Rewriting these equations in matrix form yields $\mathbf{Q}=(1-\alpha) \mathbf{P}+\alpha \mathbf{P} \mathbf{Q}$, which is equivalent to $\mathbf{Q}=$ $(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1} \mathbf{P}$, where the inverse $(\mathbf{I}-\alpha \mathbf{P})^{-1}$ is well-defined and non-negative because $\mathbf{P} \geq \mathbf{0}$ and $\alpha \in[0,1)$.

## Proof of Proposition 2

Note first that $\sigma_{g}(C, 0)=\mathbf{d}_{g}^{\top} \mathbf{P} c_{g}$. Hence, we show that $h_{g}(C)=\mathbf{d}_{g}^{\top} \mathbf{P} \mathbf{c}_{g}$. By definition of the homophily index,

$$
\begin{aligned}
h_{g}(C) & =\sum_{i \in M} d_{g, i} \sum_{j \in M} \frac{a_{i, j} n_{g, j}}{\sum_{k \in M}^{a_{i, k} n_{k}}} \\
& =\sum_{i \in M} d_{g, i} \sum_{j \in M} \frac{a_{i, j} n_{j}}{\sum_{k \in M} a_{i, k} n_{k}} c_{g, j} \\
& =\sum_{i \in M} d_{g, i} \sum_{j \in M} p_{i, j} c_{g, j} \\
& =\mathbf{d}_{g}^{\top} \mathbf{P} \mathbf{c}_{g} .
\end{aligned}
$$

This concludes the proof of the proposition.

## Proof of Proposition 3

By Lemma 1 and Proposition $1, \sigma_{g}(C, \alpha)=\left(\mathbf{d}_{g}^{\top} \mathbf{M}\right) \mathbf{P c}_{g}$, where $\mathbf{M}=(1-\alpha)(\mathbf{I}-\alpha \mathbf{P})^{-1}$. Hence, it only remains to be shown that $\mathbf{w}_{g}=\mathbf{M}^{\top} \mathbf{d}_{g}=(1-\alpha)\left(\mathbf{I}-\alpha \mathbf{P}^{\top}\right)^{-1} \mathbf{d}_{g}$. By definition, $\mathbf{w}_{g}$ is equal to the principal eigenvector of the matrix $\mathbf{S}=(1-\alpha) \mathbf{d}_{g} \mathbf{1}^{\top}+\alpha \mathbf{P}^{\top}$. Since $\mathbf{S}$ is column stochastic, its spectral radius is 1 and the principal eigenvector $\mathbf{w}_{g}$ satisfies the equation $\mathbf{S} \mathbf{w}_{g}=\mathbf{w}_{g}$. Taking a $\mathbf{w}_{g}$ whose coordinates sum up to 1 , we get that $(1-\alpha) \mathbf{d}_{g}+\alpha \mathbf{P}^{\top} \mathbf{w}_{g}=\mathbf{w}_{g}$. Solving this equation we get that $\mathbf{w}_{g}=(1-\alpha)\left(\mathbf{I}-\alpha \mathbf{P}^{\boldsymbol{\top}}\right)^{-1} \mathbf{d}_{g}$.

## Proof of Proposition 4

Since $\mathbf{P}=\mathbf{I}$,

$$
\bar{\sigma}_{g}(C, \alpha)=\left(n_{g} / n\right)^{-1} I_{g}(C)=\left(n_{g} / n\right)^{-1} \sum_{i \in M} d_{g, i} c_{g, i}=n \sum_{i \in M} \frac{1}{n_{i}} d_{g, i}^{2} .
$$

The sum of squares is minimized if $d_{g, i}=n_{i} / n$ for all $i \in M$. Thus,

$$
\bar{\sigma}_{g}(C, \alpha) \geq n \sum_{i \in M} \frac{1}{n_{i}} \frac{n_{i}^{2}}{n^{2}}=\frac{1}{n} \sum_{i \in M} n_{i}=1 .
$$

This concludes the proof of the proposition.

## Proof of Theorem 1

The proof is organized as follows. First, we show existence of a steady state equilibrium and relate it to the segregation index. Afterwards, we establish the uniqueness of the equilibrium. Finally, we prove matching balancedness.

## 1) Existence

Take any time investments $\left(t_{g, i}\right)_{i \in M, g \in G}$. Using the utility function (1), one sees that the marginal utility of the time investment $t_{g, i}$ in culture $g$ of an individual born in neighborhood $i$ equals

$$
\begin{equation*}
\frac{\partial U_{i}}{\partial t_{g, i}}=A_{0} \sum_{j \in M} p_{i, j} c_{g, j}+A_{1} \sum_{j \in M} p_{i, j} \frac{t_{g, j}}{t_{j}}-D t_{g, i} . \tag{2}
\end{equation*}
$$

In order to prove existence, we derive an equilibrium where $\partial U_{i} / \partial t_{g, i}=0$. We will show first that the total time efforts are equal for all individuals; that is, in this equilibrium, individuals will only differ in the way they distribute their time over all cultures. Summing over all groups and recalling that $\sum_{g \in G} c_{g, j}=1$ for all $j \in M$ and $\sum_{j \in M} p_{i, j}=1$, we have that $A_{0}+A_{1}-D t_{i}=0$. It follows then that for all $i \in M$,

$$
\begin{equation*}
t_{i}^{*}=\frac{A_{0}+A_{1}}{D} \tag{3}
\end{equation*}
$$

Now, we are going to determine the time spent in $g$-related meetings. Let $\mathbf{t}_{g}=\left(t_{g, i}\right)_{i \in M}$ be the vector of times spent in culture $g \in G$. Using equation (3), the first order conditions can be rewritten in matrix form as

$$
\frac{A_{0}}{D} \mathbf{P} \mathbf{c}_{g}+\frac{A_{1}}{A_{0}+A_{1}} \mathbf{P} \mathbf{t}_{g}-\mathbf{t}_{g}=\mathbf{0}
$$

It follows that

$$
\mathbf{t}_{g}^{*}=\frac{A_{0}}{D}\left(\mathbf{I}-\frac{A_{1}}{A_{0}+A_{1}} \mathbf{P}\right)^{-1} \mathbf{P} \mathbf{c}_{g} \geq \mathbf{0}
$$

The non-negativity of $\mathbf{t}_{g}^{*}$ follows from the fact that the inverse exists and that it is nonnegative (remember that $\mathbf{P}$ is stochastic and that $\left.0 \leq A_{1} /\left(A_{0}+A_{1}\right)<1\right)$. Hence, $\mathbf{t}_{g}^{*}$ is the unique equilibrium satisfying $\partial U_{i} / \partial t_{g, i}=0$ for all $i \in M$ and $g \in G$.

Next, we will will relate the equilibrium time investments to the segregation index. Recall that the vector of local segregations $\mathbf{v}_{g}$ for the continuation probability $\alpha=A_{1} /\left(A_{0}+A_{1}\right)$ is defined as

$$
\mathbf{v}_{g}=\frac{A_{0}}{A_{0}+A_{1}}\left(\mathbf{I}-\frac{A_{1}}{A_{0}+A_{1}} \mathbf{P}\right)^{-1} \mathbf{P} \mathbf{c}_{g}
$$

Consequently,

$$
\mathbf{t}_{g}^{*}=\frac{A_{0}+A_{1}}{D} \mathbf{v}_{g}
$$

Finally, the average time investment in culture $g$ by members of group $g$ is

$$
\bar{t}^{g} \equiv \frac{1}{n_{g}} \sum_{i \in M} n_{g, i} t_{g, i}^{*}=\sum_{i \in M} d_{g, i} t_{g, i}^{*}=\frac{A_{0}+A_{1}}{D} \sum_{i \in M} d_{g, i} v_{g, i}=\frac{A_{0}+A_{1}}{D} \sigma_{g}\left(C, \frac{A_{1}}{A_{0}+A_{1}}\right)
$$

This concludes the first part of the proof.

## 2) Uniqueness

In any equilibrium, $\partial U_{i} / \partial t_{g, i} \leq 0$ for all $i \in M$ and $g \in G$, with strict inequality only if $t_{g, i}^{*}=0$. We show that $\partial U_{i} / \partial t_{g, i}=0$. Suppose, by contradiction, that $\partial U_{i} / \partial t_{g, i}<0$ for some $i \in M$ and $g \in G$. Then, $t_{g, i}^{*}=0$ and it follows from equation (2) that

$$
A_{0} \sum_{j \in M} p_{i, j} c_{g, j}+A_{1} \sum_{j \in M} p_{i, j} \frac{t_{g, j}}{t_{j}}<0
$$

However, this cannot be because all values in the equation are non-negative by definition. Hence, $\partial U_{i} / \partial t_{g, i}=0$, and the unique equilibrium is the one calculated in the first part of the proof. This concludes the second part of the proof.

## 3) Balancedness

The balancedness conditions can be written formally as:

- Total balancedness. For all $i, j \in M, n_{i} \cdot t_{i} \cdot p_{i, j}=n_{j} \cdot t_{j} \cdot p_{j, i}$.
- I-balancedness. For all $i, j \in M$ and $g \in G, n_{i} \cdot p_{i, j} \cdot t_{g, i} \cdot t_{g, j} \cdot 1 / t_{j}=n_{j} \cdot p_{j, i} \cdot t_{g, j} \cdot t_{g, i} \cdot 1 / t_{i}$, which is equivalent to $n_{i} \cdot t_{i} \cdot p_{i, j}=n_{j} \cdot t_{j} \cdot p_{j, i}$.
- C-balancedness. For all $i, j \in M$ and $g \in G, n_{i} \cdot p_{i, j} \cdot t_{g, i} \cdot c_{g, j}=n_{g, j} \cdot t_{j} \cdot p_{j, i} \cdot t_{g, i} \cdot 1 / t_{i}$, which is equivalent to $n_{i} \cdot t_{i} \cdot{ }^{i}, j=n_{j} \cdot t_{j} \cdot p_{j, i}$.

The three conditions are therefore equivalent, and we only have to show that $n_{i} t_{i}^{*} p_{i, j}=$ $n_{j} t_{j}^{*} p_{j, i}$. Using that $a_{i} / a_{j}=n_{i} / n_{j}$ by assumption, $t_{i}^{*}=t_{j}^{*}$, and $p_{i j}=1 / a_{i}$, we obtain that

$$
\frac{p_{i, j}}{p_{j, i}}=\frac{1 / a_{i}}{1 / a_{j}}=\frac{a_{j}}{a_{i}}=\frac{n_{j}}{n_{i}}=\frac{n_{j}}{n_{i}} \frac{t_{j}^{*}}{t_{i}^{*}} .
$$

This concludes the proof of the Theorem.

## Appendix B: Tables and Figures

| Nationality | ID | Number of Residents | Share |
| :--- | :--- | :---: | :---: |
| Spain | E | $40,956,149$ | $90.26 \%$ |
| Europe |  |  |  |
| Bulgaria | BU | 164,716 | $0.36 \%$ |
| France | F | 120,262 | $0.27 \%$ |
| Italy | I | 175,232 | $0.39 \%$ |
| Poland | PO | 85,007 | $0.19 \%$ |
| Portugal | P | 140,801 | $0.31 \%$ |
| Romania | RU | 798,869 | $1.76 \%$ |
| Russia | R | 47,428 | $0.10 \%$ |
| Ukraine | UC | 82,263 | $0.18 \%$ |

## Africa

| Algeria | AR | 56,194 | $0.12 \%$ |
| :--- | :--- | :---: | :---: |
| Morocco | MA | 708,939 | $1.56 \%$ |
| Nigeria | NI | 42,322 | $0.09 \%$ |
| Senegal | SE | 56,589 | $0.12 \%$ |

South America

| Argentina | A | 142,239 | $0.31 \%$ |
| :--- | :--- | :---: | :---: |
| Bolivia | BO | 230,693 | $0.51 \%$ |
| Brazil | B | 126,172 | $0.28 \%$ |
| Colombia | CO | 296,619 | $0.65 \%$ |
| Cuba | CU | 54,598 | $0.12 \%$ |
| Chile | CH | 51,032 | $0.10 \%$ |
| Ecuador | EC | 421,385 | $0.93 \%$ |
| Paraguay | PA | 81,549 | $0.18 \%$ |
| Peru | PE | 139,167 | $0.31 \%$ |
| Dominican Republic | RD | 88,102 | $0.19 \%$ |
| Uruguay | UR | 50,422 | $0.11 \%$ |
| Venezuela | VE | 61,448 | $0.14 \%$ |

## Asia

| China | C | 147,373 | $0.32 \%$ |
| :--- | :--- | :--- | :--- |
| Pakistan | PK | 54,100 | $0.12 \%$ |

Table 3: Residents in Spain as of January 2009 according to the country of origin (nationality). The data is made available by the National Statistical Institute (INE) of Spain. Only 39,915 of the Romanians living in Spain were also born in Spain.

| Field ID | Full Name |
| :--- | :--- |
| AccAud | Accounting and Auditing |
| AgrEnvEn | Agricultural, Environmental and Energy Economics |
| DevTrans | Development and Transition Economics |
| EconStat | Econometrics and Statistics Applied to Economics |
| FinIns | Finance and Insurance |
| GenEcon | General Economics |
| HistPolMet | History of Economic Thought, Political Economy, Methodology |
| HRM | Human Resource Management and Industrial Relations |
| InnovEntrSB | Innovation, Entrepreneurship, Small Business |
| IO | Industrial Organization, Productivity Analysis |
| LaborHealth | Labor, Education, Population and Health Economics |
| Law | Law and Economics |
| Macro | Macroeconomics, International and Monetary Economics |
| PubEcon | Public Economics, Public Choice |
| Sector | Sectorial Studies |
| Socio | Social Economics, Political Science, Philosophy, Sociology, International Relations |
| Theory | Economic Theory, Game and Decision Theory |
| UrbSpaReg | Urban, Spatial, Regional and Transport Economics |

Table 4: Field abbreviations in the citation model using the CEFAGE-EU ranking from the University of Évora, Portugal.

| ce | E | BU | F | I | PO | P | RU | R | C | AR | MA | NI | SE | A | BO | B | CO | CU | CH | EC | PA | PE | RD | UR | VE | C | PA | $\bar{I}(C)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 A | 1.0 | 9.58 | 3.02 | 2.86 | 5.5 | 2.22 | 2.2 | 7.81 | 4.86 | 2.11 | 2.30 | 4.75 | 7.70 | 2.71 | 3.14 | 1.80 | 1.63 | 3.08 | 5.55 | 2.15 | 2.55 | 3.98 | 3.63 | 4.49 | . 6 | 4.61 | 4.64 | 1.13 |
| 02 | 1.00 | 3.37 | 3.19 | 3.05 | 8.85 | 6.11 | 2.68 | 5.77 | 8.39 | 5.17 | 3.64 | 20.36 | 8.70 | 3.47 | 3.75 | 3.74 | 1.89 | 23 | 86 | 3.36 | 2.07 | 5.14 | 4.22 | 7.88 | 5.37 | 8.15 | . 90 | 21 |
| 03 | 1.01 | 3.94 | 4.23 | 2.53 | 3.89 | 3.26 | 2.52 | 7.25 | 4.19 | 4.19 | 3.18 | 17.76 | 12.79 | 2.16 | 5.19 | . 54 | 2.13 | 2.93 | 4.95 | 2.40 | 5.06 | 3.96 | 5.15 | 3.00 | 4.43 | 4.41 | 18.93 | 1.36 |
| 04 A | 1.03 | 3.93 | 4.18 | 3.71 | 4.58 | 3.5 | . 72 | 3.02 | 4.19 | 7.27 | 4.23 | 17.00 | 8.65 | 1.9 | 7.88 | . 5 | 2.39 | 4.4 | 6.14 | 4.3 | 14.84 | 5.28 | 6.75 | 7.51 | 5.29 | 5.02 | 12.95 | 1.53 |
| 05 Avila | 1.00 | 7.69 | 5.59 | 4.91 | 4.05 | 3.86 | 2.17 | 17.25 | 6.76 | 9.39 | 3.63 | 10.77 | 65.85 | 6.14 | 7.00 | 3.18 | 2.39 | 6.76 | 10.72 | 2.89 | 18.05 | 4.36 | 2.77 | 7.13 | 10.73 | 4.63 | 84.63 | 1.22 |
| 06 Badajoz | 1.00 | 20.14 | 6.35 | 5.55 | 16.03 | 4.16 | 5.81 | 76 | 10.17 | 10.04 | 23 | 23.77 | 26.51 | 5.64 | 7.42 | . 0 | 3.3 | 7.9 | 19.68 | 5.2 | 12.44 | 8.7 | 7.9 | 21.53 | 13.35 | 7.08 | 42.30 | 15 |
| 07 | 1.01 | 2.95 | 2.77 | 1.87 | 3.12 | 2.98 | 2.64 | 3.92 | 3.65 | 3.74 | 2.88 | 19.83 | 7.84 | 1.53 | 4.52 | 2.12 | 1.81 | 1.93 | 2.45 | 2.28 | 4.62 | 2.44 | 2.59 | 2.41 | 2.64 | 5.14 | 21.25 | 1.34 |
| 08 | 1.01 | 5.94 | 4.02 | 2.63 | 5.13 | 3.34 | 2.86 | 3.42 | 4.41 | 7.79 | 3.52 | 17.26 | 13.51 | 1.98 | 3.75 | 3.33 | 1.82 | 2.52 | 2.83 | 2.85 | 6.55 | 2.71 | 4.36 | 3.52 | 2.81 | 5.50 | 16.57 | 1.41 |
| 09 Burgos | 1.00 | 3.63 | 3.63 | 4.48 | 5.63 | 4.26 | 2.09 | 8.82 | 8.61 | 4.21 | 2.63 | 11.72 | 10.02 | 4.27 | 5.53 | 2.64 | 2.2 | 5.26 | 10.00 | 2.4 | 4.88 | 4.4 | 3.1 | 23.20 | 4.12 | 6.65 | 8.75 | 1.22 |
| 10 Caceres | 1.00 | 26.13 | 9.99 | 9.47 | 13.12 | 6.75 | 5.13 | 14.57 | 21.61 | 11.74 | 10.92 | 60.79 | 15.10 | 5.91 | 8.46 | 3.55 | 3.61 | 9.05 | 17.61 | 5.36 | 13.04 | 6.02 | 9.10 | 22.88 | 9.46 | 9.08 | 101.07 | 1.26 |
| 11 | 1.00 | 19.67 | 4.44 | 4.82 | 7.40 | 6.33 | 64 | 9.10 | 8.66 | 15.2 | 5.57 | 18.63 | 22.39 | 5.29 | 6.9 | 29 | 3.3 | 5.0 | 12.09 | 5.91 | 12.2 | 5.92 | 5.7 | 15.3 | 6.31 | 6.58 | 85.18 | 1.16 |
| 12 C | 1.01 | 6.58 | 4.59 | 2.85 | 4.33 | 3.50 | 1.48 | 7.15 | 4.82 | 2.90 | 2.33 | 7.39 | 10.47 | 2.17 | 17.47 | 5.21 | 1.76 | 2.66 | 5.01 | 4.77 | 7.67 | 3.73 | 5.41 | 6.29 | 3.76 | 3.29 | 8.57 | 24 |
| 13 Ciudad R | 1.00 | 7.38 | 4.88 | 4.82 | 6.64 | 6.09 | 2.18 | 4.72 | 4.62 | 8.01 | . 41 | 39.28 | 5.9 | 5.34 | 4.06 | 4.83 | 2.6 | 6.68 | 16.42 | 4.2 | . 72 | 6.74 | 5.3 | 19.1 | 6.52 | 6.06 | 5.61 | 1.19 |
| 14 Cordoba | 1.00 | 24.10 | 5.13 | 4.28 | 16.16 | 6.30 | 3.58 | 8.03 | 8.80 | 11.32 | 3.03 | 25.21 | 34.05 | 6.26 | 10.76 | 5.34 | 3.4 | 8.42 | 15.05 | 6.25 | 7.50 | 12.96 | 11.65 | 25.29 | 8.40 | 8.08 | 17.46 | 1.13 |
| 15 | 1.00 | 17.97 | 3.85 | 2.58 | 10.2 | 2.87 | . 01 | 77 | 13.84 | 29.83 | 10.78 | 15.7 | 22.8 | 3.07 | 17.53 | 3.58 | 2.68 | 3.60 | 9.77 | 7.25 | 10.55 | 5.30 | 5.80 | 4.54 | 3.10 | 8.24 | 45.1 | 1.14 |
| 16 | 1.01 | 7.88 | 6.24 | 5.1 | 5.97 | 8.20 | 1.66 | 8.20 | 3.24 | 6.88 | 2.52 | 29.69 | . 1 | 4.13 | 10.6 | 8.41 | 2.70 | 9.73 | 12.1 | 3.40 | 3.47 | 3.88 | 4.88 | 56.18 | 0.35 | 1.6 | 47.83 | 28 |
| 17 | 1.02 | 6.38 | 5.96 | 2.33 | 3.49 | 3.53 | 1.99 | . 18 | 2.62 | 5.63 | 2.33 | 21.51 | 6.13 | 2.48 | 7.33 | 3.17 | 2.08 | 2.65 | . 57 | 2.80 | .95 | 3.51 | 3.70 | 3.70 | 3.02 | 5.19 | 6.33 | 42 |
| 18 G | 1.00 | 17.98 | 3.45 | 3.30 | 7.58 | 4.85 | 5.27 | 3.26 | 6.39 | 6.70 | 4.29 | 47.14 | 8.95 | 2.41 | 7.13 | 3.29 | 2.9 | 4.08 | 6.44 | 5.22 | 9.86 | 6.77 | 6.40 | 9.87 | 5.06 | 7.12 | 24.27 | . 23 |
| 19 Guadalajar | 1.01 | 7.49 | 52 | 2.27 | 17 | 47 | 57 | 07 | 97 | 98 | 2.21 | . 77 | 16.84 | 2.36 | 6.0 | 4.01 | 1.58 | 2.94 | 4.24 | 2.28 | . 65 | 1.90 | 2.67 | 5.26 | 3.21 | 5.31 | 9.5 | 27 |
| 20 Guipuzca | 1.00 | 8.57 | 2.95 | 2.83 | 6.74 | 2.45 | 5.65 | 5.05 | 3.70 | 4.16 | 2.8 | 19.51 | 5.5 | 2.58 | 4.2 | 2.68 | 2.2 | 2.4 | 5.28 | 2.27 | 7.84 | 3.8 | 3.04 | 9.08 | 4.02 | 7.1 | 10.5 | 1.14 |
| 21 Huelva | 1.01 | 5.94 | 3.94 | 3.75 | 6.14 | 5.32 | 2.74 | 8.53 | 3.77 | 6.38 | 3.93 | 21.92 | 10.21 | 5.02 | 6.2 | 4.16 | 3.27 | . 12 | 16.1 | 6.2 | 17.21 | 8.09 | 11.19 | 17.2 | 7.50 | . 19 | 40.06 | 25 |
| 22 | 1.01 | 6.03 | 5.22 | 3.27 | 4.85 | 4.09 | 1.85 | 4.04 | 3.11 | 4.88 | 2.86 | 20.76 | 6.94 | 3.26 | 14.46 | 5.30 | 3.26 | 4.61 | 8.27 | 3.07 | 8.72 | 4.23 | 3.12 | 5.37 | 4.43 | 20.32 | 17.26 | 30 |
| 23 | 1.00 | 16.97 | 5.33 | 5.83 | 18.50 | 6.35 | 2.63 | 5.87 | 12.51 | 4.41 | 4.84 | 31.05 | 16.92 | 4.78 | 6.35 | 6.14 | 4.6 | 8.72 | 22.43 | 4.29 | 10.65 | 7.96 | 7.09 | 31.15 | 12.8 | 7.23 | 24.75 | 13 |
| 24 L | 1.00 | 5.61 | 3.59 | 3.96 | 10.5 | 4.13 | 5.20 | 99 | 12.11 | 14.21 | 4.08 | 23.05 | 26.48 | 3.23 | 9.58 | 2.48 | 2.65 | 4.12 | 17.62 | 5.0 | 6.96 | 5.28 | 3.83 | 13.36 | 3.72 | 8.37 | 29.48 | 20 |
| 25 L | 1.01 | 4.67 | 7.94 | 2.47 | 3.69 | 7.36 | 1.62 | 22 | 10.40 | 3.30 | 2.06 | 5.8 | 3.59 | 2.46 | 5.0 | 3.99 | 2.00 | 3.64 | 6.65 | 3.34 | 7.78 | 3.62 | 3.04 | 4.83 | 5.68 | 4.88 | 8.95 | . 36 |
| 26 | 1.01 | 3.45 | 2.82 | 2.44 | 10.07 | 6.09 | 1.96 | 4.30 | 6.36 | 4.35 | 3.00 | 6.51 | 10.30 | 2.33 | 2.70 | 2.84 | 2.18 | 2.47 | 22.39 | 2.54 | 8.59 | 8.24 | 3.84 | 9.04 | 3.67 | 4.41 | 4.93 | 3 |
| 27 L | 1.00 | 34.91 | 4.66 | 3.41 | 40.72 | 1.87 | 3.75 | 16.97 | 15.04 | 26.26 | 4.87 | 18.23 | 27.57 | 3.55 | 12. | 2.95 | 2.85 | 3.91 | 15.47 | 8.96 | 8.38 | 10.0 | 3.65 | 5.97 | 3.83 | 9.97 | 30.11 | 4 |
| 28 Madrid | 1.0 | 3.78 | 8.00 | 2.28 | 3.07 | 2.28 | 2.93 | 4.15 | 3.43 | 8.71 | . 31 | 13 | . 0 | 1.92 | 3.28 | 2.86 | 1.7 | 2.5 | 3.66 | 2.3 | 2.97 | 1.88 | 3.27 | 4.89 | 2.79 | 5.03 | 27.91 | 1.34 |
| 29 M | 1.01 | 3.75 | 3.42 | 61 | 4.78 | 3.32 | 2.84 | 5.16 | 2.88 | 7.04 | 2.18 | 7.64 | 10.3 | 1.95 | 4.8 | 2.9 | 2.22 | 3.43 | 3.7 | 6.2 | 2.76 | 3.9 | 4.8 | 3.17 | 2.95 | 4.19 | 14.5 | 1.22 |
| 30 | 1.01 | 5.62 | 4.26 | 2.97 | 7.21 | 5.47 | 2.92 | 4.51 | 4.65 | 7.13 | 3.06 | 12.18 | 13.81 | 2.81 | 2.59 | 3.33 | 2.39 | 4.10 | 7.29 | 2.07 | 5.6 | 6.67 | 5.28 | 7.64 | 5.36 | 4.44 | 47.94 | 1.37 |
| 31 | 1.00 | 2.88 | 6.47 | 2.35 | 4.04 | 2.54 | 2.30 | 4.06 | 3.52 | 5.87 | 4.49 | 6.53 | 5.21 | 2.49 | 3.84 | 2.46 | 1.91 | 3.03 | 4.39 | 2.17 | 7.88 | 2.80 | 2.96 | 8.13 | 3.41 | 5.07 | 17.15 | 24 |
| 32 O | 1.00 | 12.95 | 5.39 | 3.11 | 11.75 | 3.05 | 3.99 | . 68 | 10.67 | 6.7 | 9.88 | 18.34 | 11.50 | 2.64 | 8.37 | 2.99 | 2.82 | 3.96 | 14.2 | 8.12 | 7.35 | 8.10 | 3.77 | 3.55 | 2.55 | 8. 34 | 43.72 | 1.14 |
| 33 A | 1.00 | 8.64 | 3.29 | 3.07 | . 31 | 3.14 | 2.77 | 6.99 | 5.76 | 9.05 | 4.01 | 12.56 | 11.99 | 2.64 | 8.81 | 2.25 | 2.89 | 3.03 | 7.95 | 5.47 | 4.51 | 5.59 | 3.87 | 6.90 | 3.24 | 5.45 | 56.2 | 1.14 |
| 34 P | 1.00 | 2.79 | 3.51 | 3.40 | 5.99 | . 59 | 3.69 | 10.45 | 17.59 | 20.17 | 4.36 | 119.34 | 5.3 | 4.16 | 11.56 | 3.10 | 2.84 | 7.82 | 19.05 | 3.45 | 89 | 3.73 | 9.95 | 49.58 | 9.15 | 5.58 | 57.1 | 16 |
| 35 | 1.01 | 7.50 | 3.96 | 4.11 | 4.77 | 4.68 | 9.07 | 4.78 | 6.68 | 6.95 | 4.91 | 7.02 | 9.69 | 2.48 | 6.11 | 3.20 | 3.13 | 2.45 | 4.19 | 3.7 | 9.35 | 3.55 | 6.82 | 4.17 | 2.21 | 6.50 | 40. | 1.32 |
| 36 Pontevedra | 1.0 | 34.31 | 3.56 | 2.53 | 25.44 | 2.24 | 6.97 | 7.65 | 75 | 48.87 | 7.06 | 20.43 | 18.74 | 2.49 | 24.91 | 3.39 | 2.8 | 4.60 | 11.50 | 11. | 8.29 | 6.05 | 6.3 | 3.53 | 2.88 | 10.24 | 105.68 | 18 |
| 37 Salamanca | 1.0 | 38 | 4.69 | 3.72 | . 36 | 11.36 | 4.50 | 6.33 | 6.49 | 30.26 | 2.85 | 8.75 | 30.32 | 4.80 | 4.75 | 3.21 | 2.94 | 5.44 | 7.39 | 7.8 | 9.10 | 4.46 | 24.62 | 12.35 | 5.70 | 4.96 | 78.69 | 1.26 |
| 38 SantaCruz | 1.01 | 7.59 | 7.02 | 4.67 | 6.34 | 3.82 | 5.17 | 12.50 | 10.58 | 8.14 | 7.40 | 8.23 | 18.94 | 2.96 | 7.56 | 4.17 | 3.94 | 2.70 | 4.99 | 5.80 | 9.77 | 3.34 | 4.58 | 4.33 | 1.76 | 19.33 | 69.67 | 1.40 |
| 39 Cantabria | 1.0 | 15.81 | 2.44 | 2.32 | 21.61 | 4.18 | 2.10 | 4.19 | 93 | 10.6 | 4.12 | 10.8 | 10.3 | 2.61 | 12.17 | 2.40 | 2.06 | 3.04 | 5.80 | 3.92 | 3.66 | 3.17 | 3.11 | 7.3 | 3.1 | 5.80 | 11.03 | 1.17 |
| 40 Segovia | 1.01 | 1.76 | 5.83 | 6.57 | 2.69 | 13.12 | 4.01 | 18.04 | 29 | 11.1 | 2.36 | . 15 | 31.1 | 6.37 | . 7 | 3.52 | 1.98 | 7.56 | 7.95 | 2.77 | 13.52 | 2.4 | 3.18 | 8.08 | 7.66 | 7.6 | 51.74 | 1.27 |
| 41 Sevilla | 1.0 | 16.18 | 4.39 | 3.86 | 7.83 | 5.27 | 4.50 | 12 | 5.73 | 10.2 | 2.89 | 3.61 | 26.6 | 3.6 | . 8 | . 4 | 2.9 | . | 11.5 | 9.7 | 8.27 | 5. | 19.91 | 11.7 |  | . 8 | 8. | 1.17 |
| 42 Soria | 1.00 | 2.42 | 5.3 | 4.52 | 5.74 | 3.51 | 2.51 | 8.95 | 8.48 | 4.87 | 2.71 | 11.54 | 8.60 | 2.74 | 2.83 | 2.32 | 2.97 | 3.00 | 17.97 | 2.06 | 7.08 | 2.68 | 3.03 | 21.01 | 3.63 | 4.24 | 28.83 | 1.18 |
| 43 Tarragona | 1.0 | 4.05 | 3.80 | 2.33 | . 61 | 2.87 | 2.26 | 4.27 | 3.52 | 3.49 | 2.12 | 20.77 | 17.72 | 2.33 | 5.13 | 3.14 | 1.96 | 2.71 | 3.33 | 2.78 | 4.77 | 2.56 | 8.14 | 4.10 | 3.18 | 3.22 | 9.06 | 1.3 |
| 44 Teruel | 1.01 | 14.77 | 5.75 | 5.31 | 10.59 | 5.33 | 1.70 | 81.03 | 6.38 | . 69 | 2.12 | 64.03 | 29.52 | 9.43 | 24.61 | 4.91 | 4.19 | 7.71 | 27.43 | 5.30 | 20.36 | 3.21 | 4.72 | 44.55 | 17.98 | 7.85 | 13.11 | 1.42 |
| 45 Toledo | 1.0 | 3.64 | 3.81 | 3.03 | 3.76 | 3.81 | 1.84 | 10.26 | 5.50 | . 93 | 2.17 | 10.9 | 32.0 | 2.98 | 6.78 | . 63 | 2.1 | 3.88 | 5.37 | 2.1 | 7.86 | 3.63 | 3.23 | 13.39 | 4.85 | 5.56 | 31.6 | 1.22 |
| 46 V | 1.01 | 5.77 | 2.74 | 2.19 | 4.20 | 4.6 | 2.20 | 3.68 | 3.14 | 3.31 | 3.03 | 6.92 | 8.93 | 2.07 | . 3 | 2.9 | 2.0 | 2.73 | 6.18 | 3.1 | 5.21 | 3.9 | 5.3 | . 60 | 3.35 | 3.9 | 8. 7 | 1.26 |
| 47 Valladolid | 1.00 | 66 | 4.12 | 4.40 | . 8 | 3.8 | 3.1 | 36 | 10.54 | 18.38 | 4.9 | 32.28 | 20.9 | 4.16 | 5.84 | 2.49 | 2.36 | 3.95 | 16.18 | 4.62 | 9.42 | 4.97 | 3.97 | 55.79 | 5.16 | 5.63 | 30.72 | 1.19 |
| 48 Vizcaya | 1.00 | 16.47 | 4.39 | 3.51 | 14.31 | 4.05 | 2.93 | 9.40 | 9.46 | 6.16 | 3.72 | 13.24 | 18.84 | 3.16 | 2.58 | 2.40 | 2.09 | 3.26 | 7.04 | 3.54 | 2.72 | 3.75 | 6.38 | 10.71 | 3.90 | 7.32 | 18.96 | 1.16 |
| 49 Zamora | 1.0 | 2.79 | 5.01 | 12.26 | 62.33 | 3.78 | 5.41 | 19.35 | 13.00 | 14.00 | 7.26 | 82.57 | 188.74 | 5.62 | 9.70 | 3.93 | 3.78 | 6.65 | 15.41 | 11.38 | 9.22 | 6.01 | 4.37 | 12.47 | 8.70 | 9.83 | 65.38 | 1.18 |
| 50 Zaragoza | 1.01 | 10.48 | . 93 | . 31 | 10.20 | . 23 | . 91 | .13 | . 63 | . 55 | . 83 | 6.29 | 5.37 | 3.27 | 5.89 | 2.67 | 1.98 | 3.52 | 6.04 | 2.51 | 13.72 | 3.55 | 3.31 | 7.56 | 3.43 | 4.13 | 39.62 | 1.2 |
| Spain | 1.01 | 8.78 | 7. | 5.76 | 7.41 | 6.81 | 4.22 | 13.26 | 7.21 | 9.99 | 5.2 | 61 | 18.82 | 3.2 | 5.59 | 3.70 | 2.66 | 4.9 | 5.68 | 4.37 | .7 | 4.7 | 6.60 | 7.1 | 4.9 | 7.8 | 0. | 1.52 |

Table 5: Normalized segregation index in Spain as of January 2009 for $\mathbf{G}=\mathbf{I}$ (normalized isolation index) and a neighborhood radius of 400 meters.

| Province | E | BU | F | I | PO | P | RU | R | UC | AR | MA | NI | SE | A | BO | B | CO | CU | CH | EC | PA | PE | RD | UR | VE | C | PA | $\bar{h}(C)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 Alava | 1.00 | 76 | 1.96 | 1.93 | 3.40 | 1.97 | . 77 | 2.06 | 15 | 61 | 78 | 2.43 | 2.83 | 1.70 | 1.76 | 1.34 | 1.37 | 13 | 25 | 1.50 | 77 | 3.19 | 32 | . 52 | 80 | 32 | 34 | 1.06 |
| 02 | 1.00 | 3.03 | 2.74 | 2.17 | 7.75 | 4.92 | 2.60 | 3.38 | 8.02 | 3.25 | 3.42 | 9.38 | 4.83 | 2.36 | 3.45 | 2.22 | 1.63 | 2.87 | 5.19 | 3.09 | 1.68 | 3.19 | 2.54 | 3.76 | 3.43 | 4.85 | 6.68 | 1.16 |
| 03 Alicante | 1.01 | 67 | 12 | 2.36 | 3.56 | 2.81 | 2.27 | 7.03 | 3.80 | . 06 | 2.78 | 13.47 | . 68 | . 97 | . 46 | 3.9 | 1.92 | 2.44 | . 03 | 2.08 | 3.20 | 2.5 | 3.3 | 2.50 | 3.69 | 3.6 | 11.74 | 29 |
| 04 Almeria | 1.02 | 3.68 | 4.13 | 3.56 | 4.41 | 3.25 | 2.69 | 2.89 | 4.04 | 6.94 | 4.01 | 16.54 | 8.25 | 1.80 | 7.69 | 3.19 | 2.23 | 3.85 | 5.50 | 4.25 | 14.54 | 5.10 | 5.88 | 6.88 | 3.68 | 4.24 | 12.04 | 1.50 |
| 05 A | 1.00 | 7.64 | 5.27 | 4.7 | 3.61 | 3.74 | 2.08 | 16.01 | 6.23 | 6.06 | 3.59 | 5.00 | 57.50 | 6.09 | . 96 | 3.07 | 2.29 | 6.58 | 10.24 | 2.73 | 18.03 | 4.16 | 2.5 | 6.83 | 10.39 | 3.6 | 84.63 | 1.21 |
| 06 Badajoz | 1.00 | 18.94 | 5.54 | 4.75 | 13.43 | 4.02 | 5.27 | 13.17 | 8.00 | 6.94 | 2.72 | 12.1 | 20.05 | 4.38 | 5.81 | 2.52 | 2.76 | 5.34 | 16.4 | 3.75 | 9.37 | 7.0 | 6.0 | 16.74 | 10.8 | 4.75 | 21.74 | 1.12 |
| 07 Baleares | 1.01 | 2.69 | 2.70 | 1.80 | 2.94 | 2.66 | 2.44 | 3.44 | 2.74 | 2.62 | 2.74 | 13.12 | 6.83 | 1.44 | 3.80 | 1.94 | 1.68 | 1.72 | 2.08 | 2.12 | 3.70 | 2.06 | 2.00 | 2.24 | 2.05 | 3.57 | 16.49 | 27 |
| 08 Barcelona | 1.01 | 3.87 | 3.61 | 2.34 | 4.12 | 2.09 | . 31 | 2.00 | 2.86 | 3.26 | 2.89 | 11.64 | 94 | . 65 | 2.67 | 2.05 | . 41 | 1.63 | 1.91 | . 39 | 4.8 | 2.11 | 2.9 | 2.68 | 1.72 | 3.8 | . 15 | . 26 |
| 09 Burgos | 1.00 | 3.30 | 2.95 | 95 | 3.91 | 69 | 1.93 | 5.85 | 6.84 | 2.44 | 2.25 | 4.13 | 5.10 | 3.24 | 3.71 | 1.95 | 2.04 | 3.60 | 5.23 | 1.90 | 3.37 | 3.06 | 2.40 | 19.93 | 2.45 | 3.14 | 5.82 | 1.16 |
| 10 Caceres | 1.00 | 20.59 | 77 | 8.37 | 11.32 | 6.68 | 4.97 | 11.59 | 15.45 | 9.67 | 10.83 | 59.24 | 12.35 | 5.28 | 5.98 | 3.14 | 2.76 | 6.56 | 15.40 | 3.90 | 6.89 | 5.18 | 7.54 | 19.93 | 6.95 | 4.60 | 68.95 | 1.24 |
| 11 | 1.00 | 14.91 | 3.66 | 4.05 | 5.23 | 5.51 | 12.98 | 6.49 | 5.07 | 6.80 | 4.47 | 10.80 | 10.70 | 4.19 | 4.72 | 3.50 | 2.62 | 3.27 | 6.26 | 3.93 | 7.33 | 3.70 | 3.32 | 12.32 | 3.77 | 3.63 | 35.81 | 1.11 |
| 12 Castello | 1.01 | 6.06 | 4.53 | 2.73 | 3.90 | 3.20 | 1.37 | 6.41 | 4.31 | 2.25 | 2.08 | 3.93 | 15 | 1.87 | 6.28 | 5.01 | 1.53 | . 05 | 3.70 | 4.44 | 4.81 | 2.70 | 3.15 | 5.92 | 2.88 | 2.34 | 4.55 | 19 |
| 13 Ciudad Rea | . 0 | 7.25 | 4.51 | 3.62 | 6.16 | 4.67 | 2.15 | 11.92 | 3.73 | 6.16 | 2.33 | . 18 | 2.61 | 4.27 | 3.84 | 3.74 | 37 | 5.68 | 0.2 | . 7 | 3.1 | 3.88 | 3.9 | 12.31 | 5.2 | 3.9 | 27.20 | 17 |
| 14 Cordoba | 1.00 | 18.49 | 3.81 | 2.62 | 10.84 | 55 | 17 | 27 | . 5 | 90 | 34 | 3.1 | 2.0 | 4.77 | 5.59 | 3.1 | 2.79 | 4.03 | 6.74 | 3.82 | 4.23 | 3.78 | 4.69 | 12.91 | 3.92 | 3.57 | 8.62 | . 0 |
| 15 Coruna | 1.00 | 10.16 | 2.7 | 2.1 | 8.31 | 62 | 4.13 | 5.63 | 96 | 11.14 | 67 | 9.48 | 0.74 | . 58 | 6.89 | 3.05 | 2.19 | 2.59 | 8.10 | 3.92 | 6.70 | 3.65 | 3.67 | . 50 | 2.58 | 4.03 | 11.3 | 1.09 |
| 16 C | 1.0 | 7.78 | 6.02 | 3.92 | 5.65 | 7.97 | 1.64 | 7.29 | 2.87 | 5.24 | 2.48 | . 01 | 15.07 | . 65 | 10.45 | 8.25 | 2.53 | 8.40 | . 32 | 3.27 | 3.41 | 3.47 | 3.7 | 5.19 | 9.18 | 6.51 | 45.77 | 25 |
| 17 | 1.02 | 5.87 | 93 | 2.26 | 41 | 32 | 96 | 14 | 48 | 33 | 15 | 5.77 | . 40 | 2.40 | 6.85 | 2.76 | 1.92 | 2.36 | 3.28 | 2.57 | 7.34 | 3.10 | 3.42 | 3.53 | 2.6 | 4.77 | 5.42 | 1.38 |
| 18 Granada | 1.00 | 17.10 | 13 | 2.98 | 6.07 | 3.70 | 16 | 2.63 | 4.21 | 39 | 3.90 | 21.21 | 6.00 | 2.17 | 6.53 | 2.74 | 2.58 | 3.12 | 5.00 | 4.56 | 7.48 | 4.33 | 4.39 | 8.00 | 3.81 | 4.11 | 10.20 | 1.19 |
| 19 Guadalajara | 1.01 | 7.41 | 3.45 | 2.06 | 07 | 6.41 | 1.54 | 4.06 | 58 | 2.99 | 2.12 | 6.45 | 13.96 | 2.23 | 5.54 | 3.87 | 1.53 | 2.63 | 3.19 | 2.04 | 5.34 | 1.75 | 2.35 | 3.96 | 2.77 | 3.07 | 9.99 | 1.24 |
| 20 Guipuzca | 1.00 | 6.87 | 2.60 | 2.32 | 3.66 | 2.15 | 5.21 | 3.10 | 39 | 2.93 | 38 | . 29 | 13.88 | . 84 | 3.32 | 1.99 | 1.82 | 1.74 | 4.10 | 1.79 | 3.44 | 2.55 | 2.06 | 4.83 | 2.59 | 3.28 | 7.67 | 10 |
| 21 H | 1.0 | 5.67 | 3.44 | 3.06 | 5.57 | 5.27 | 2.62 | 6.62 | 3.07 | 5.85 | 3.39 | 61 | 4.69 | 3.76 | 99 | 3.22 | 2.57 | 2.97 | 12.6 | 5.61 | 12.0 | 4.2 | . 29 | . 13 | 3.86 | 3.74 | 21.21 | 20 |
| 22 H | 1.0 | 5.97 | 5.18 | 3.10 | 4.74 | 3.75 | 1.78 | 3.52 | 2.80 | 3.61 | 2.57 | 8.54 | 5.60 | 2.81 | 14.1 | 3.38 | 3.09 | 3.84 | 6.52 | 2.7 | 6.32 | 3.71 | 2.51 | 5.02 | 3.69 | 9.2 | 15.33 | 1.26 |
| 23 Jaen | 1.00 | 15.96 | 3.45 | 16 | 14.92 | 67 | 2.33 | 3.23 | 46 | 3.46 | 4.19 | 9.56 | 7.47 | 2.99 | 4.51 | 4.28 | 3.30 | 6.37 | 16.76 | 2.89 | 6.57 | 4.77 | 5.43 | 19.51 | 8.97 | 3.84 | 10.9 | . 09 |
| 24 Leon | 1.00 | 44 | 3.18 | 95 | 8.98 | 08 | 3.05 | 5.27 | 6.78 | 5.36 | 3.36 | 9.12 | 18.52 | 2.61 | 7.33 | 1.93 | 2.30 | 2.86 | 11.12 | 3.73 | 5.56 | 3.10 | 3.07 | 7.50 | 2.52 | 4.52 | 26.76 | . 14 |
| 25 L | 1.01 | 4.40 | 7.64 | 2.14 | 3.40 | 7.30 | 1.57 | 1.95 | 10.17 | 2.72 | 84 | 4.07 | 3.17 | 2.15 | 4.49 | 3.64 | 1.83 | 3.14 | 6.04 | 3.0 | 5.61 | 3.3 | 2.5 | 3.82 | . 17 | 3.7 | 5.56 | 31 |
| 26 R | 1.0 | 2.73 | 2.43 | 1.92 | 9.44 | 6.07 | 1.87 | 3.46 | 5.66 | 3.96 | 2.84 | 3.34 | 4.06 | 2.08 | 2.18 | 2.2 | 1.98 | 2.0 | 21.91 | 2.23 | 3.82 | 7.57 | 2.46 | 7.59 | 2.5 | 2.7 | 3.6 | 1.28 |
| 27 Lugo | 1.00 | 33.17 | 4.36 | 2.79 | 38.92 | 84 | 3.36 | 9.48 | 8.32 | 18.27 | 4.40 | 9.29 | 21.93 | 2.92 | 6.68 | 2.70 | 2.42 | 2.85 | 14.94 | 4.53 | 6.60 | 9.75 | 3.20 | 4.11 | 3.11 | 5.93 | 11.24 | 1.11 |
| 28 Madrid | 1.01 | 02 | 36 | 1.95 | 2.35 | 1.78 | 2.71 | 2.18 | 2.31 | 3.18 | 2.90 | 5.88 | 14.04 | 1.52 | 2.71 | 2.00 | 1.46 | 1.58 | 2.37 | 2.02 | 2.19 | 1.54 | 2.45 | 2.62 | 2.18 | 3.63 | 14.09 | 1.24 |
| 29 Malaga | 1.0 | 2.84 | 3.30 | 2.47 | 14 | 2.90 | 2.38 | 4.83 | 2.31 | 4.87 | 1.94 | 4.14 | 7.48 | 1.77 | 3.97 | 2.51 | 1.90 | 2.5 | 2.63 | 5.13 | 2.24 | 2.48 | 3.43 | 2.43 | 2.25 | 3.19 | 8.05 | 1.16 |
| 30 N | 1.01 | 4.83 | 4.08 | 2.60 | 6.54 | 4.96 | 2.72 | 3.52 | 3.45 | 6.33 | 2.72 | 7.67 | 11.47 | 2.20 | 2.22 | 2.68 | 2.12 | 2.92 | 4.66 | 1.94 | 15. | 5.19 | 3.28 | 5.46 | 3.24 | 2.86 | 39.31 | \% |
| 31 N | 1.0 | 2.58 | 6.29 | 1.97 | 3.29 | 2.45 | 2.05 | 2.83 | 2.74 | 5.51 | 4.45 | 5.26 | 4.04 | 2.10 | 3.23 | 2.1 | 1.77 | 2.4 | 3.1 | 2.0 | 4.74 | 2.15 | 2. | 5.7 | 2.4 | 2.98 | 14.28 | . 20 |
| 32 Ourense | 1.00 | 11.28 | 5.21 | 2.82 | 9.37 | 3.03 | 3.39 | 8.42 | 8.37 | 10.79 | 9.64 | 10.23 | 8.28 | 2.26 | 6.16 | 2.80 | 2.43 | 3.23 | 12.54 | 5.28 | 6.47 | 5.44 | 3.00 | 12.30 | 2.31 | 5.17 | 32.36 | 1.12 |
| 33 Asturias | 1.0 | 4.30 | 2.48 | 2.08 | 8.56 | 2.36 | 2.28 | 3.34 | 3.41 | 4.19 | 3.16 | 5.07 | 6.09 | 1.93 | 3.88 | 1.78 | 2.30 | 2.16 | 4.14 | 3.61 | 3.00 | 2.97 | 2.84 | 4.60 | 2.34 | 2.52 | 14.05 | 1.08 |
| 34 P | 1.0 | 2.31 | 2.74 | 2.50 | 5.32 | 11.4 | 3.17 | 4.29 | 15.24 | 15.86 | 4.01 | 113.95 | 9.47 | 3.17 | 10.5 | 2.46 | 1.95 | 4.21 | 13.51 | 2.12 | 3.46 | 2.87 | 3.25 | 35.86 | 7.78 | 3.5 | 3.2 | 1.13 |
| 35 P | 1.0 | 6.71 | 3.84 | 4.06 | 4.38 | 4.57 | 8.82 | 3.97 | 4.61 | 6.02 | 4.66 | 4.26 | 6.90 | 2.33 | 14 | 2.7 | 3.02 | 2.2 | 3.76 | 3.42 | 7.82 | 3.0 | 6.08 | 3.96 | 1.88 | 5.32 | 38.22 | 1.28 |
| 36 Pontevedra | 1.00 | 0. 43 | 3.12 | 2.00 | 18.42 | 2.16 | 97 | . 31 | 7.67 | 9.34 | 6.66 | 6.15 | 69 | . 94 | 12.84 | 2.4 | 37 | 3.1 | 4.99 | . 69 | 3.83 | 4.36 | 3.7 | 2.74 | 2.3 | 5.75 | 9.65 | 1.12 |
| 37 Salamanca | 1.00 | 22 | 26 | 3.06 | 7.20 | 11.31 | 4.20 | 4.26 | 4.83 | 20.04 | 49 | 5.45 | 29.86 | 4.11 | 3.49 | 2.66 | 2.45 | 3.78 | 5.07 | 6.77 | 5.90 | 3.06 | 22.89 | 10.06 | 3.66 | 3.18 | 33.5 | 1.22 |
| 38 SantaCruz | 1.01 | 23 | 6.97 | 62 | 6.27 | 3.74 | 4.97 | 12.43 | 9.86 | 7.72 | . 35 | 7.55 | 17.91 | 2.82 | 5.01 | 3.85 | 3.85 | 2.55 | 4.62 | 5.12 | 5.76 | 2.82 | 3.32 | 4.18 | 1.70 | 18.85 | 69.3 | 1.37 |
| 39 Cantabria | 1.00 | 15.42 | 13 | 89 | 19.95 | 3.94 | 1.90 | 2.75 | 2.59 | 5.54 | 3.43 | 4.47 | 6.40 | 2.06 | 4.96 | 1.91 | 1.73 | 1.81 | 2.94 | 2.8 | 2.35 | 2.64 | 2.3 | 5.3 | 2.22 | 3.2 | 5.7 | 1.12 |
| 40 Segovia | 1.0 | 1.68 | 5.41 | 6.12 | 2.59 | 13.08 | 4.01 | 17.18 | 5.92 | 15 | . 25 | 29.29 | 14.86 | . 77 | 52 | 3.4 | 1.87 | 7.07 | 6.74 | 2.54 | 11.2 | 2.15 | 2.7 | 7.47 | 5.11 | 5.50 | 43.68 | . 24 |
| 41 Sevilla | 1.0 | 9.94 | 3.44 | 2.84 | 5.28 | 3.84 | 3.96 | 2.73 | 3.33 | 7.55 | 2.14 | 6.33 | 18.14 | . 41 | 4.77 | 2.44 | 2.01 | 2.5 | 5.58 | 5.6 | 4.7 | 3.12 | 10. | 6.8 | 2.8 | 4.72 | 14.76 | 1.10 |
| 42 S | 1.00 | 2.36 | 5.06 | 3.66 | 5.66 | 45 | 48 | 70 | 28 | 4.14 | 67 | 9.43 | 4.80 | . 27 | 2.38 | 2.2 | 2.89 | 2.90 | 17.65 | 1.86 | 6.00 | 2.3 | 2.4 | 19.71 | 2.82 | 3.1 | 22. | 1.1 |
| 43 Tarragona | 1.01 | 3.74 | 72 | 2.24 | 3.31 | 2.65 | 2.14 | 3.99 | 3.19 | 2.53 | 1.88 | 18.30 | 16.13 | 2.16 | 3.54 | 2.95 | 1.74 | 2.42 | 2.84 | 2.52 | 3.64 | 1.98 | 7.63 | 3.63 | 2.73 | 2.45 | 7.25 | 1.32 |
| 44 Teruel | 1.00 | 14.59 | 5.58 | 4.77 | 10.57 | 4.99 | 1.67 | 78.89 | 5.49 | 4.66 | 2.05 | 42.62 | 28.67 | 9.20 | 24.46 | 4.77 | 3.98 | 6.71 | 26.62 | 5.10 | 19.67 | 2.92 | 4.16 | 43.86 | 15.93 | 4.76 | 12.11 | 1.39 |
| 45 Toledo | 1.0 | . 1 | 3.49 | 2.7 | 3.69 | 3.20 | 1.80 | 9.00 | 5.16 | 6.11 | 11 | 10.55 | 25.01 | 2.81 | 5.98 | 3.3 | 2.04 | 3.6 | 4.32 | 2.04 | 6.1 | 3.45 | 2.9 | 12.98 | 4.2 | 4.41 | 31.52 | 1.2 |
| 46 Valencia | 1.00 | 5.27 | 2.48 | 1.85 | 3.45 | 3.83 | 1.96 | 2.15 | 2.36 | 2.14 | 2.35 | 4.15 | 5.00 | 1.62 | 2.59 | 2.07 | 1.64 | 1.69 | 4.19 | 2.60 | 3.27 | 2.31 | 2.75 | 2.64 | 2.10 | 2.21 | 4.46 | 1.17 |
| 47 Valladolid | 1.00 | 3.32 | 3.69 | 3.23 | 6.42 | 3.44 | 2.73 | 5.62 | 4.10 | 4.49 | 3.13 | 15.68 | 6.00 | 2.47 | 3.20 | 1.75 | 1.87 | 2.54 | 5.94 | 2.72 | 4.31 | 3.32 | 2.27 | 54.53 | 2.86 | 2.83 | 9.69 | 1.12 |
| 48 Vizcaya | 1.00 | 10.02 | 2.87 | 2.08 | 7.14 | 3.65 | 2.52 | 3.95 | 5.51 | 3.69 | 2.56 | 7.93 | 13.70 | 2.01 | 2.05 | 1.76 | 1.67 | 1.86 | 2.98 | 2.52 | 1.79 | 2.36 | 2.76 | 5.56 | 2.17 | 3.45 | 5.26 | 1.09 |
| 49 Zamora | 1.0 | 67 | 4.40 | 11.89 | 17.35 | 3.70 | . 14 | 16.05 | 12.64 | 11.98 | . 13 | 35.42 | 150.78 | . 86 | . 81 | 2.9 | 3.3 | 6.11 | 9.75 | 10.87 | 6.16 | 4.9 | 3.70 | 10.52 | 6.8 | 5.31 | 1.20 | 1.15 |
| 50 Zaragoza | 1.00 | 10.00 | 2.38 | 1.68 | 9.33 | 2.84 | 1.79 | 2.25 | 2.38 | 3.33 | 3.34 | 2.83 | 3.35 | 2.43 | 3.25 | 1.82 | 1.54 | 2.37 | 2.83 | 1.96 | 6.40 | 2.30 | 2.25 | 4.84 | 1.73 | 2.42 | 36.04 | 1.21 |
| Spain | . 01 | 7.98 | 7.4 | 5.45 | 6.41 | 6.42 | 3.9 | 12.23 | 5.91 | 7.55 | 4.67 | 12.04 | 14.92 | 2.90 | 4.43 | 2.85 | 2.33 | 4.12 | 4.13 | 3.79 | 5.10 | 3.81 | 4.92 | 6.10 | 4.11 | 5.64 | 8.9 | 1.4 |

Table 6: Normalized segregation index in Spain as of January 2009 for $\alpha=0.00$ (normalized homophily index) and a neighborhood radius of 400 meters.

| Province | E | BU | F | I | O | P | RU | R | UC | AR | MA | NI | SE | A | BO | B | CO | CU | CH | EC | PA | PE | RD | UR | VE | C | PA | $\bar{\sigma}(C, 0.50)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 Alava | 1.00 | 57 | 1.92 | 1.91 | 30 | 1.96 | 77 | 2.02 | 11 | 57 | 71 | 2.31 | 67 | . 67 | . 75 | 1.32 | 1.37 | 12 | 22 | 1.50 | . 74 | 3.17 | 27 | 5.27 | 77 | 27 | 2.33 | 1.06 |
| 02 | 1.00 | 3.01 | 2.71 | 2.12 | 7.69 | 4.96 | 2.60 | 3.41 | 7.91 | 3.23 | 3.41 | 9.36 | 4.75 | 2.33 | 3.42 | 2.19 | 1.61 | 2.88 | 4.95 | 3.08 | 1.67 | 3.06 | 2.51 | 3.70 | 3.44 | 4.75 | 6.49 | 1.16 |
| 03 Alicante | 1.01 | 3.65 | 4.11 | 35 | 3.54 | 79 | 25 | 99 | 3.75 | 2.99 | 2.75 | 13.07 | . 55 | 1.96 | . 43 | 3.92 | 1.91 | 2.42 | 4.00 | 2.06 | 3.13 | 2.5 | 3.3 | 2.4 | 3.66 | 3.6 | 11.21 | 1.29 |
| 04 Almeria | 1.02 | 3.66 | 4.13 | 3.56 | 4.40 | 3.24 | 2.68 | 2.89 | 4.02 | 6.93 | 4.00 | 16.45 | 8.19 | 1.79 | 7.69 | 3.17 | 2.22 | 3.83 | 5.49 | 4.24 | 14.53 | 5.09 | 5.87 | 6.84 | 3.67 | 4.21 | 11.99 | 1.49 |
| 05 Avila | 1.00 | . 64 | 27 | 4.76 | 3.62 | 3.74 | 2.08 | 16.00 | 6.18 | 5.99 | 3.59 | 5.22 | 57.39 | 6.09 | 6.95 | 3.06 | 2.28 | 6.54 | 10.25 | 2.74 | 18.03 | 4.15 | 2.54 | 6.83 | 10.39 | 3.56 | 84.63 | 1.21 |
| 06 Badajoz | 1.00 | 18.85 | 5.49 | 4.71 | 13.34 | 4.01 | 5.25 | 12 | 7.86 | 6.74 | 2.69 | 12.00 | 19.62 | 4.32 | 5.66 | 2.50 | 2.71 | 5.29 | 16.40 | 3.65 | 9.08 | 6.93 | 5.99 | 16.60 | 10.6 | 4.7 | 20.8 | 1.12 |
| 07 Baleares | 1.01 | 2.68 | 2.68 | 1.79 | 2.94 | 2.64 | 2.43 | 3.41 | 2.71 | 2.59 | 72 | . 61 | 72 | 1.43 | 70 | 1.92 | . 68 | . 71 | 08 | . 12 | . 67 | 2.05 | 2.0 | 2.24 | 2.05 | 3.44 | 16.42 | . 26 |
| 08 Barcelona | 1.01 | 3.83 | 3.55 | 2.32 | 4.09 | 2.06 | 2.28 | 1.97 | 2.84 | 3.17 | 2.81 | 11.43 | 9.65 | 1.64 | 2.62 | 2.01 | 1.40 | 1.61 | 1.89 | 2.35 | 4.81 | 2.09 | 2.90 | 2.67 | 1.70 | 3.69 | 8.55 | 1.25 |
| 09 Burgos | 1.00 | 3.28 | 2.94 | 2.92 | 3.87 | 3.61 | 1.92 | 5.77 | 6.81 | 2.38 | 2.23 | 4.02 | 4.59 | 3.24 | 3.74 | 1.92 | 2.03 | 3.53 | 5.25 | 1.88 | 3.31 | 3.06 | 2.36 | 19.85 | 2.46 | 3.01 | 5.84 | 1.15 |
| 10 Caceres | 1.00 | 20.38 | 76 | 33 | 11.32 | 6.68 | 4.96 | 11.50 | 15.31 | 9.60 | 10.82 | 59.10 | 12.13 | 5.23 | 5.76 | 3.11 | 2.76 | 6.48 | 15.34 | 3.84 | 6.83 | 5.15 | 7.51 | 19.64 | 6.92 | 4.48 | 67.34 | 1.24 |
| 11 | 1.00 | 14.65 | 3.62 | 3.99 | 5.11 | 5.45 | 12.9 | 6.40 | 4.97 | 6.70 | 4.41 | 10.61 | 0. 3 | 13 | 4.57 | 3.46 | 2.58 | 3.20 | 5.95 | 3.87 | 7.14 | 3.57 | 3.2 | 12.21 | 3.71 | 3.52 | 2.25 | 11 |
| 12 Castello | 1.01 | 6.03 | 4.53 | 72 | 3.88 | 18 | 1.36 | 6.40 | 4.27 | 2.21 | 2.07 | 3.78 | 05 | . 86 | 16.24 | 5.00 | . 52 | 2.02 | 3.68 | . 42 | . 77 | 2.69 | 3.08 | 5.8 | 2.8 | 2.3 | 4.43 | 19 |
| 13 Ciudad Rea | 1.00 | 24 | 50 | 3.57 | 6.14 | 4.67 | 2.15 | 11.71 | 3.71 | 6.07 | 2.33 | 24.93 | 32.56 | 4.23 | 3.83 | 3.71 | 2.37 | 5.61 | 9.95 | 3.69 | 3.15 | 3.75 | 3.89 | 11.99 | 5.24 | 3.88 | 26.05 | 1.17 |
| 14 Cordoba | 1.00 | 18.01 | 73 | 2.54 | 10.53 | 3.53 | 3.15 | 4.19 | 6.99 | 7.79 | 2.31 | 12.64 | 11.82 | 4.74 | 5.37 | 3.10 | 2.75 | 3.92 | 6.31 | 3.70 | 4.06 | 3.68 | 4.60 | 12.68 | 3.89 | 3.39 | 8.42 | 1.08 |
| 15 Coruna | 1.00 | 92 | 77 | 10 | 8.29 | 61 | 11 | 5.51 | 90 | 10.82 | 64 | 9.30 | 10.38 | 2.55 | 6.39 | 3.03 | 2.17 | 2.56 | 8.05 | 3.74 | 6.40 | 3.60 | 3.52 | 3.45 | 2.57 | 3.94 | 11.47 | 1.09 |
| 16 C | 1.0 | 7.77 | 6.01 | 3.95 | 5.64 | 7.94 | 1.64 | 7.29 | 85 | 5.08 | 48 | 28.97 | 15.02 | . 63 | 10.45 | 8.24 | 2.53 | 8.42 | . 31 | 3.27 | 3.41 | 3.44 | 3.7 | 55.16 | 9.17 | 6.11 | 45.8 | . 25 |
| 17 | 1.02 | 5.86 | 93 | 2.26 | 41 | 32 | 1.96 | 6.13 | 47 | 28 | 15 | 5.72 | 5.39 | 2.40 | 6.85 | 2.76 | 1.91 | 2.36 | 3.28 | 2.56 | 7.35 | 3.09 | 3.42 | 3.53 | 2.66 | 4.78 | 5.38 | 1.38 |
| 18 Granada | 00 | 17.08 | 11 | 95 | 99 | 69 | 5.16 | 2.60 | 11 | 5.34 | . 85 | 20.55 | . 76 | 2.17 | 6.48 | 2.72 | 2.56 | 3.08 | 4.93 | 4.54 | 7.37 | 4.25 | 4.3 | 7.9 | 3.7 | 3.9 | 0.06 | 1.19 |
| 19 Guadalajara | 1.01 | 7.40 | 3.44 | 2.06 | 3.06 | 6.40 | 54 | 98 | 53 | 98 | 2.11 | 6.44 | 13.88 | 2.22 | 5.50 | 3.86 | 1.53 | 2.62 | 3.18 | 2.02 | 5.34 | 1.74 | 2.32 | 3.90 | 2.75 | 3.05 | 9.84 | 1.24 |
| 20 Guipuzca | 1.00 | 6.84 | 59 | 2.29 | 52 | 2.14 | 5.18 | . 01 | 2.36 | 2.88 | 2.38 | 9.08 | 13.62 | . 83 | 3.29 | 1.96 | 1.79 | 1.73 | 4.08 | 1.78 | 3.35 | 2.50 | 2.04 | 4.76 | 2.50 | 3.21 | 7.71 | 1.10 |
| 21 H | 1.0 | 5.65 | 3.42 | 3.05 | 5.48 | 5.27 | 2.62 | 6.56 | 3.03 | 5.75 | 31 | 9.44 | 4.51 | 70 | 95 | . 15 | 2.54 | 2.93 | 12.58 | 5.50 | 12.0 | 4.2 | 4.99 | 11.25 | 3.8 | 3.60 | 1.37 | 20 |
| 22 H | 1.0 | 5.97 | 5.17 | 3.10 | 73 | 3.76 | 1.78 | 3.50 | 2.80 | 3.53 | 2.56 | 8.67 | 56 | .82 | 14.17 | 3.3 | 3.09 | 3.83 | 6.34 | 2.7 | 6.29 | 3.7 | 2.4 | 5.0 | 3.6 | 19.2 | 5.2 | . 26 |
| 23 Jaen | 1.00 | 15.88 | 3.42 | 08 | 14.77 | 61 | 2.32 | 3.17 | 9.46 | 3.41 | 4.14 | 8.95 | 7.49 | 2.93 | 4.48 | 4.14 | 3.21 | 6.34 | 16.32 | 2.85 | 6.50 | 4.65 | 5.36 | 19.15 | 8.92 | 3.69 | 10.60 | 1.08 |
| 24 Leon | 1.00 | . 43 | 3.17 | 91 | 8.94 | 4.08 | 3.05 | 5.23 | 6.79 | 5.35 | 3.31 | 9.10 | 18.31 | 2.60 | 7.21 | 1.93 | 2.27 | 2.85 | 11.43 | 3.65 | 5.53 | 3.05 | 3.02 | 7.29 | 2.50 | 4.39 | 26.70 | 1.14 |
| 25 L | 1.01 | 4.39 | 7.64 | 2.13 | 3.38 | 7.30 | 1.57 | 1.93 | 10.17 | 2.65 | 82 | 3.93 | 16 | 12 | 45 | 3.63 | 1.83 | 3.14 | . 03 | 2.99 | 5.54 | 3.37 | 2.5 | 3.80 | 4.1 | 3.7 | 5.30 | 1.31 |
| 26 R | 1.0 | 2.70 | 2.43 | 1.92 | 9.42 | 6.06 | 1.87 | 3.44 | 5.65 | 3.95 | 2.81 | 3.21 | 3.94 | 2.07 | 2.16 | 2.2 | 1.98 | 2.0 | . 9 | 2.21 | 3.78 | 7.5 | 2.47 | 7.55 | 2.4 | 2. | 3.48 | 1.28 |
| 27 Lugo | 1.00 | 33.15 | 4.34 | 2.78 | 38.77 | 1.84 | 3.31 | 9.35 | 8.34 | 17.64 | 4.38 | 8.92 | 21.76 | 2.91 | 6.65 | 2.70 | 2.43 | 2.79 | 14.95 | 4.50 | 6.36 | 9.73 | 3.18 | 4.02 | 3.06 | 5.67 | 10.82 | 1.11 |
| 28 Madrid | 1.01 | 2.99 | 29 | 1.93 | 2.32 | 1.77 | 2.70 | 2.13 | 2.29 | 3.04 | 2.87 | 5.78 | 13.03 | 1.50 | 2.68 | 1.97 | 1.45 | 1.56 | 2.33 | 2.00 | 2.15 | 1.53 | 2.40 | 2.55 | 2.16 | 3.48 | 13.95 | 1.23 |
| 29 Malaga | 1.0 | 2.82 | 3.29 | 2.45 | 4.11 | 2.88 | 2.35 | 4.81 | 2.28 | 4.82 | 1.93 | 4.04 | 26 | 1.76 | 3.95 | 2.48 | 1.89 | 2.54 | 2.59 | 5.14 | 2.20 | 2.47 | 3.39 | 2.42 | 2.24 | 3.14 | 7.80 | 1.16 |
| 30 N | 1.0 | 4.77 | 4.07 | 2.58 | 6.50 | 4.95 | 2.70 | 3.48 | 3.40 | 6.31 | 2.67 | 7.39 | 11.37 | 2.17 | 2.18 | 2.67 | 2.11 | 2.8 | 4.63 | 1.94 | 15. | 5. | 3.18 | 5.35 | 3.19 | 2.79 | 98 | 1.29 |
| 31 N | 1.0 | 2.57 | 6.28 | 1.96 | 3.27 | 2.44 | 2.05 | 2.78 | 2.69 | 5.46 | 4.45 | 5.12 | 3.95 | 2.0 | 3.18 | 2.1 | 1.76 | 2.4 | 3.1 | 1.99 | 4.61 |  | 2.54 | 5.6 | . | , | 23 | 1.20 |
| 32 Ourense | 1.00 | 11.23 | 5.21 | 2.81 | 9.35 | 3.02 | 3.35 | 8.20 | 8.36 | 10.50 | 9.63 | 10.08 | 7.94 | 2.25 | 6.00 | 2.79 | 2.42 | 3.22 | 12.48 | 4.95 | 6.41 | 5.45 | 2.94 | 12.29 | 2.30 | 5.01 | 32.88 | 1.12 |
| 33 Asturias | 1.0 | 4.22 | 2.45 | 2.05 | 8.55 | 2.35 | 2.28 | 3.26 | 3.34 | 4.07 | 3.15 | 4.93 | 5.88 | 1.91 | 3.77 | 1.78 | 2.29 | 2.12 | 4.03 | 3.49 | 2.96 | 2.85 | 2.82 | 4.59 | 2.31 | 2.43 | 12.70 | 1.08 |
| 34 P | 1.0 | 2.30 | 2.74 | 2.47 | 5.30 | 11.40 | 3.18 | 4.30 | 15.19 | 15.79 | 4.00 | 113.98 | 9.26 | 3.16 | 10.54 | 2.46 | 1.92 | 4.25 | 13.57 | 2.11 | 3.46 | 2.81 | 3.19 | 34.95 | 7.7 | 3.4 | 53.27 | 1.13 |
| 35 P | 1.01 | 6.71 | 83 | 4.05 | 4.35 | 4.56 | 8.80 | 94 | . 53 | 5.95 | 64 | 4.16 | 6.77 | 33 | 4.11 | 2.7 | . 01 | 2.24 | .74 | . 3 | . 76 | 3.04 | 5.9 | 3.9 | 1.8 | 5.15 | 38.06 | 1.28 |
| 36 Pontevedra | 1.00 | 30.30 | 3.10 | 1.98 | 16.93 | 2.16 | 92 | 5.23 | 7.56 | 29.22 | . 62 | 5.88 | 9.04 | . 93 | 12.02 | 2.37 | 2.34 | 3.05 | 4.89 | 7.03 | 3.75 | 4.31 | 3.75 | 2.7 | 2.3 | 5.68 | 8.56 | 1.11 |
| 37 Salamanca | 1.00 | 7.21 | 4.24 | 3.03 | 7.15 | 11.30 | 4.21 | 4.20 | 4.74 | 18.70 | 2.47 | 5.36 | 29.84 | 4.09 | 3.44 | 2.65 | 2.43 | 3.76 | 5.04 | 6.75 | 5.76 | 3.01 | 22.89 | 9.97 | 3.63 | 3.09 | 33.34 | 1.22 |
| 38 SantaCruz | 1.01 | 7.22 | 97 | 62 | 6.26 | 3.74 | 4.96 | 12.43 | 9.85 | 7.71 | 7.35 | 7.51 | 17.90 | 2.82 | 4.86 | 3.82 | 3.85 | 2.54 | 4.59 | 5.11 | 5.59 | 2.80 | 3.30 | 4.18 | 1.69 | 18.83 | 69.31 | 1.37 |
| 39 Cantabria | 1.00 | 15.41 | 13 | 1.89 | 19.94 | 3.93 | 1.89 | 2.75 | 2.56 | 5.34 | 3.38 | 4.44 | 6.38 | 2.05 | 4.63 | 1.90 | 1.72 | 1.81 | 2.91 | 2.85 | 2.30 | 2.62 | 2.34 | 5.26 | 2.20 | 3.18 | 5.79 | 1.12 |
| 40 Segovia | 1.01 | 1.68 | 5.42 | 10 | 58 | 13.08 | 00 | 17.16 | 5.90 | 08 | 2.24 | 29.19 | 15.05 | . 69 | 46 | 3.41 | 1.88 | 7.06 | 6.72 | 2.52 | 11.18 | 2.14 | 2.78 | 7.43 | 5.01 | 5.42 | 3.63 | 1.24 |
| 41 Sevilla | 1.0 | 9.45 | 37 | 2.78 | 5.19 | 3.68 | 3.93 | 2.66 | 3.29 | 7.49 | 2.11 | 6.19 | 17.96 | 2.37 | 4.62 | 2.41 | 1.97 | 2.46 | 5.38 | 5.46 | 4.59 | 3.02 | 10.75 | 6.76 | 2.78 | 4.57 | 14.23 | 1.10 |
| 42 Soria | 1.00 | 2.35 | , | 3.64 | 5.65 | 3.45 | 2.48 | 6.66 | 8.29 | 4.08 | 2.66 | 9.52 | 4.91 | 2.29 | 2.33 | 2.24 | 2.88 | 2.90 | 17.63 | 1.85 | 5.98 | 2.28 | 2.49 | 19.65 | 2.80 | 2.89 | 22.74 | 1.16 |
| 43 Tarragona | 1.01 | 3.74 | 3.72 | 2.23 | 3.30 | 2.64 | 2.13 | 3.98 | 3.19 | 2.50 | 1.87 | 18.18 | 16.12 | 2.16 | 3.44 | 2.94 | 1.72 | 2.42 | 2.82 | 2.50 | 3.60 | 1.97 | 7.63 | 3.62 | 2.71 | 2.43 | 7.14 | 1.32 |
| 44 Teruel | 1.00 | 14.57 | 5.54 | 4.75 | 10.57 | 4.98 | 1.67 | 78.91 | 5.48 | 4.51 | 2.05 | 42.62 | 28.67 | 9.19 | 24.46 | 4.76 | 3.95 | 6.66 | 26.62 | 5.10 | 19.63 | 2.91 | 4.12 | 43.84 | 15.91 | 4.60 | 12.08 | 1.39 |
| 45 Toledo | 1.00 | 3.28 | 48 | 2.73 | . 69 | 3.18 | 1.80 | 8.96 | 5.15 | 6.09 | 2.11 | 10.54 | 24.84 | 2.80 | 5.95 | 3.37 | 2.04 | 3.69 | 4.30 | 2.03 | 6.10 | 3.45 | 2.98 | 12.96 | 4.19 | 4.38 | 31.52 | 1.20 |
| 46 Valencia | 1.00 | 5.22 | 2.46 | 1.82 | 3.42 | 3.81 | 1.94 | 2.10 | 2.33 | 2.08 | 2.30 | 3.96 | 4.79 | 1.60 | 2.55 | 2.05 | 1.63 | 1.67 | 4.11 | 2.54 | 3.18 | 2.25 | 2.69 | 2.61 | 2.07 | 2.14 | 4.26 | 1.17 |
| 47 Valladolid | 1.00 | 3.31 | 3.65 | 3.20 | 6.41 | 3.43 | 2.73 | 5.61 | 4.04 | 4.39 | 3.00 | 15.31 | 5.70 | 2.43 | 3.11 | 1.74 | 1.86 | 2.50 | 5.76 | 2.66 | 4.16 | 3.29 | 2.22 | 54.53 | 2.86 | 2.77 | 9.63 | 1.12 |
| 48 Vizcaya | 1.00 | 9.92 | 2.80 | 2.03 | 7.07 | 3.63 | 2.50 | 3.86 | 5.48 | 3.48 | 2.47 | 7.44 | 13.17 | 2.00 | 1.99 | 1.74 | 1.64 | 1.81 | 2.92 | 2.46 | 1.76 | 2.32 | 2.72 | 5.45 | 2.14 | 3.30 | 5.07 | 1.09 |
| 49 Zamora | 1.00 | 2.67 | 37 | 11.87 | 14.62 | 3.70 | 5.14 | 15.96 | 12.64 | 11.93 | 7.10 | 35.47 | 150.76 | 4.85 | 7.72 | 2.97 | 3.34 | 6.08 | 9.30 | 10.85 | 6.12 | 4.94 | 3.67 | 10.45 | 6.58 | 5.15 | 11.06 | 1.15 |
| 50 Zaragoza | 1.00 | 9.99 | 2.35 | 1.66 | 9.33 | 2.83 | 1.78 | 2.22 | 2.38 | 3.22 | 3.28 | 2.72 | 3.22 | 2.41 | 3.20 | 1.78 | 1.53 | 2.36 | 2.79 | 1.92 | 6.32 | 2.28 | 2.23 | 4.80 | 1.72 | 2.36 | 36.01 | 1.21 |
| Spain | 1.01 | 7.93 | 7.37 | 5.42 | 6.36 | 6.39 | 3.95 | 12.17 | 5.86 | 7.41 | 4.61 | 11.48 | 14.67 | 2.89 | 4.37 | 2.82 | 2.31 | 4.10 | 4.10 | 3.75 | 5.04 | 3.77 | 4.82 | 6.07 | 4.08 | 5.46 | 27.27 | 1.40 |

Table 7: Normalized segregation index in Spain as of January 2009 for $\alpha=0.50$ and a neighborhood radius of 400 meters.

| Province | E | BU | F | I | PO | P | RU | R | UC | AR | MA | NI | SE | A | BO | B | CO | CU | CH | EC | PA | PE | RD | UR | VE | C | PA | $\bar{\sigma}(C, 0.85)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 Alava | 1.00 | 14 | 1.84 | 1.85 | 3.10 | . 93 | 1.75 | 1.85 | 1.98 | 50 | 1.60 | 2.08 | 34 | . 60 | 68 | 1.29 | . 36 | 2.07 | . 08 | 1.47 | 1.67 | . 12 | 2.15 | 4.78 | 1.69 | . 13 | 2.24 | 1.06 |
| 02 Albacete | 1.00 | 2.96 | 2.66 | 2.01 | 7.52 | 4.97 | 2.59 | 3.37 | 7.76 | 3.10 | 3.38 | 8.90 | 4.46 | 2.24 | 3.33 | 2.08 | 1.58 | 2.83 | 4.41 | 3.05 | 1.64 | 2.79 | 2.42 | 3.54 | 3.38 | 4.47 | 5.6 | 1.16 |
| 03 Alicante | 1.01 | 3.60 | 4.09 | 2.32 | 3.51 | 2.75 | 2.22 | 6.91 | 3.64 | 2.82 | 2.69 | 11.92 | 8.12 | 1.94 | 4.35 | 3.83 | 1.88 | 2.39 | 3.91 | 2.02 | 2.93 | 2.38 | 3.14 | 2.41 | 3.61 | 3.49 | 10.30 | 1.28 |
| 04 Almer | 1.02 | 3.61 | 4.13 | 3.55 | 4.39 | . 22 | 2.67 | 2.88 | 00 | 6.91 | 3.94 | 16.33 | 8.11 | 1.76 | 7.67 | . 12 | 2.1 | .76 | 5.46 | 4.22 | 14. | 5.08 | 5.84 | 6.77 | 62 | 15 | . 89 | 1.49 |
| 05 Avila | 1.00 | 7.64 | 5.25 | 4.75 | 3.63 | 3.73 | 2.07 | .95 | 6.10 | 5.53 | 3.59 | 5.22 | 56.9 | 6.09 | 6.95 | . 05 | 2.26 | . 47 | 10.23 | 2.74 | 18.03 | 4.14 | 2.51 | 81 | 0.3 | . 39 | 84.63 | 1.20 |
| 06 Badajoz | . 00 | 18.66 | 5.38 | 4.60 | 13.11 | 3.98 | 5.21 | 12.40 | 7.52 | 6.31 | 2.62 | 11.21 | 18.86 | 4.20 | 5.39 | 2.43 | 2.60 | 5.04 | 16.20 | 3.41 | 8.51 | 6.75 | 5.85 | 16.09 | 10.46 | 4.54 | 18.80 | 1.12 |
| 07 Baleares | 1.01 | 2.65 | 64 | 1.77 | 2.92 | 2.61 | 2.40 | 3.37 | 66 | . 51 | 2.69 | 8.61 | 6.48 | 1.42 | 3.4 | . 90 | 1.6 | . 70 | 2.06 | 2.11 | 3.59 | 2.02 | 1.97 | 2.23 | 2.0 | 3.16 | 16. | 1.25 |
| 08 Barcelona | 1.0 | 3.69 | 3.43 | 2.26 | 4.01 | 1.9 | 2.23 | 1.90 | 2.77 | 2.93 | 2.6 | 10.89 | 9.02 | 1.61 | 2.4 | 1.91 | 1.38 | 1.5 | 1.84 | 2. | 4.68 | 2.03 | 73 | 2.61 | 1.65 | . 35 | 7.25 | 1.23 |
| 09 Burgos | 1.00 | 3.26 | 2.90 | 2.84 | 3.76 | 3.46 | 1.90 | . 57 | 6.70 | 2.25 | 2.19 | 3.68 | 3.61 | 3.19 | 3.71 | 1.86 | 2.01 | 3.35 | 5.07 | 1.8 | 3.1 | . 03 | . 28 | 19.6 | 2.43 | 2.77 | 5.80 | 1.15 |
| 10 Caceres | 1.00 | 19.8 | 9.73 | 8.26 | 11.22 | 6.68 | 4.96 | 11.27 | 15.05 | 9.42 | 10.80 | 58.86 | 11.74 | 5.15 | 5.27 | 3.06 | 2.7 | 6.27 | 15.07 | 3.7 | 6.6 | 5.09 | 7.44 | 9.1 | 6.78 | 4.14 | 4.84 | 1.24 |
| 11 Cadiz | 1.00 | 14.04 | 3.51 | 3.86 | . 88 | 5.32 | 12.84 | 6.18 | 4.66 | 6.05 | 4.29 | 10.09 | 9.39 | 4.00 | 4.2 | 3.37 | 2.50 | 3.04 | 5.27 | 3.73 | 6.72 | 3.27 | 2.96 | 11.96 | 3.52 | 3.20 | 26.62 | . 10 |
| 12 Castellon | 1.01 | 5.99 | 4.52 | 2.71 | . 83 | 3.14 | 1.35 | 6.35 | . 19 | 2.13 | 2.05 | 3.39 | 4.71 | 1.85 | 16.16 | 4.98 | 1.50 | 1.97 | 3.62 | 4.38 | 4.64 | 2.65 | 2.93 | 5.81 | 2.83 | 2.21 | . 1. | 1.18 |
| 13 Ciudad Rea | 1.00 | 7.21 | 4.48 | 3.47 | 6.08 | 4.59 | 2.14 | 11.27 | 3.67 | 5.84 | 2.31 | 22.73 | 32.39 | 4.13 | 3.81 | 3.62 | 2.36 | 5.50 | 9.46 | 3.63 | 3.12 | 3.47 | 3.77 | 11.35 | 5.20 | 3.78 | 23.92 | 1.16 |
| 14 Cordoba | 1.00 | 17.03 | 3.54 | 2.36 | 91 | 3.41 | 3.10 | 93 | 6.81 | 7.58 | 2.23 | 1.50 | 0.34 | 4.67 | 4.87 | 2.94 | 2.67 | 3.69 | 5.56 | 3.39 | 3.58 | 3.34 | 4.18 | 11.74 | 3.65 | 3.05 | 7.75 | 1.07 |
| 15 Coruna | 1.00 | 9.45 | 2.71 | 2.06 | 8.22 | 2.58 | 4.06 | 30 | 8.66 | 10.16 | 9.55 | 8.88 | 9.35 | 2.48 | 5.38 | 2.9 | 2.14 | 2.50 | 7.96 | 3.38 | 5.70 | 3.50 | 3.29 | 3.34 | 2.53 | 3.69 | 11.0 | 1.08 |
| 16 Cuenca | 1.0 | 7.76 | 5.99 | 3.95 | . 62 | 7.87 | . 64 | . 25 | 2.80 | 4.82 | 2.47 | 28.89 | 14.79 | 3.60 | 10.44 | 8.22 | 2.52 | 8.38 | 9.20 | 3.26 | 3.40 | 3.36 | 3.68 | 55.08 | 9.11 | 5.43 | 45.79 | 1.25 |
| 17 Girona | 1.0 | 5.82 | 5.93 | 2.25 | 3.40 | 3.32 | 1.96 | 13 | 2.45 | 4.18 | 2.13 | 15.30 | 5.33 | 2.39 | 6.84 | 2.74 | 1.90 | 2.34 | 3.27 | 2.53 | 7.34 | 3.05 | . 40 | . 51 | . 63 | 4.77 | 5.27 | 1.38 |
| 18 Granada | 1.00 | 17.02 | 3.04 | 2.88 | 5.82 | 3.64 | 5.15 | 53 | 3.92 | 5.18 | 3.74 | 8.83 | 26 | 2.1 | 6.40 | 2.66 | 2.51 | 3.00 | 4.75 | 4.4 | 7.0 | 4.07 | 4.21 | 7.84 | . 6 | 3.72 | 9.17 | 1.18 |
| 19 Guadalajar | 1.01 | 7.40 | 3.44 | 2.06 | 3.04 | 6.39 | 1.54 | 3.81 | 5.43 | 2.89 | 2.08 | 6.41 | 13.58 | 2.20 | 5.42 | 3.85 | 1.5 | 2.59 | 3.12 | 2.00 | 5.33 | 1.71 | 2.26 | 3.77 | 2.71 | 2.97 | 9.08 | 1.24 |
| 20 Guipuzca | 1.00 | 6.72 | 2.55 | 21 | . 16 | 2.09 | 5.14 | 2.83 | 2.28 | 2.77 | 2.35 | 8.53 | 13.28 | 1.78 | 3.22 | 1.88 | 1.73 | 1.69 | 4.01 | 1.75 | 3.14 | 2.41 | 1.98 | 4.49 | 2.3 | 2.98 | 7.68 | 1.0 |
| 21 Huelva | 1.00 | 5.63 | 3.39 | 3.01 | 5.33 | 5.26 | 2.60 | 6.46 | 2.95 | 5.56 | 3.18 | 7.25 | 4.11 | 3.57 | 3.81 | 3.04 | 2.47 | 2.86 | 12.28 | 5.28 | 11.94 | 4.11 | 4.40 | 11.28 | 3.69 | 3.29 | 21.15 | 1.19 |
| 22 Huesca | 1.0 | 5.96 | 5.17 | 3.09 | 4.70 | 3.75 | 1.78 | 45 | 2.79 | 3.40 | 2.53 | . 84 | 5.41 | 2.81 | 14.14 | 3.23 | 3.09 | 3.80 | 5.92 | 2.70 | 6.21 | 3.67 | 2.44 | . 99 | 3.57 | 19.13 | 15.22 | 1.26 |
| 23 J | 1.00 | 15.70 | 3.29 | 3.91 | 48 | 4.45 | 2.29 | 2.98 | 9.22 | 3.30 | 3.92 | 52 | 7.15 | 2.80 | 4.34 | . 87 | 3.00 | 6.21 | 15.54 | 2.76 | 6.26 | 4.40 | 5.17 | 8.1 | . 73 | 3.31 | 8.98 | 1.08 |
| 24 Leon | 1.0 | 41 | 3.14 | 2.82 | 8.81 | 4.07 | 2.91 | 12 | 6.65 | 4.95 | 3.14 | 41 | 17.86 | 2.56 | 7.03 | 1.91 | 2.22 | 2.81 | 11.36 | 3.48 | 5.44 | 2.92 | 2.89 | 6.83 | 2.41 | 4.14 | 26.45 | 1.14 |
| 25 Lleida | 1.0 | 4.36 | 7.63 | 2.11 | 3.34 | 7.29 | 1.56 | 1.90 | 10.15 | 2.52 | 1.78 | 3.69 | 3.13 | 2.07 | 4.33 | 3.60 | 1.82 | 3.12 | 5.99 | 2.98 | 5.36 | 3.36 | 2.51 | 3.74 | 4.08 | 3.62 | 4.65 | 1.30 |
| 26 Rioja | 1.00 | 2.66 | 2.40 | 1.90 | 9.39 | 6.06 | 87 | 3.39 | 5.61 | 3.93 | 2.75 | 2.87 | 3.53 | 2.05 | 2.10 | 2.15 | 1.98 | 2.03 | 21.95 | 2.16 | 3.61 | 7.52 | 2.46 | 7.44 | 2.40 | 2.60 | 3.1 | . 27 |
| 27 L | 1.00 | 33 | 4.30 | 2.75 | 38.5 | 1.84 | 3.22 | 8.97 | 8.04 | 16.71 | 4.32 | 7.95 | 21.43 | 2.85 | 6.35 | 2.68 | 2.4 | 2.68 | 14.9 | 4. | 5.90 | 9.68 | 3.15 | 3.85 | 2.95 | 5.20 | 9.60 | 1.10 |
| 28 Madrid | 1.00 | 2.94 | 7.13 | 1.87 | 2.26 | 1.73 | 2.67 | 2.01 | 2.21 | 2.69 | 2.80 | 5.54 | 10.78 | 1.47 | 2.5 | 1.88 | 1.4 | 1. | 2.2 | 1.9 | 2.0 | 1.4 | 2.2 | 2.42 | 2.12 | 17 | 13.11 | 1.22 |
| 29 Malaga | 1.0 | 2.74 | 3.25 | 2.39 | 4.03 | 2.82 | 2.30 | 4.78 | 2.20 | 4.65 | 1.89 | 3.74 | 6.77 | 1.73 | 3.87 | 2.43 | 1.87 | 2.48 | 2.49 | 5.12 | 2.13 | 2.41 | 3.28 | 2.36 | 2.20 | 3.01 | 7.15 | 1.15 |
| 30 Murcia | 1.01 | 4.66 | 4.05 | 2.53 | 6.41 | 4.91 | 2.68 | 3.41 | 3.28 | 6.26 | 2.59 | 6.77 | 11.16 | 2.12 | 2.12 | 2.63 | 2.09 | 2.78 | 4.48 | 1.91 | 14.99 | 5.07 | 2.99 | 5.14 | 3.07 | 2.64 | 39.10 | 1.28 |
| 31 Navarı | 1.00 | 2.54 | 6.26 | 1.91 | 3.21 | 2.44 | 03 | 68 | 2.60 | 38 | 4.44 | 4.89 | 78 | 2.04 | 3.04 | 2.11 | 1.7 | 2.40 | 3.06 | 1.95 | 4.36 | 2.09 | 2.49 | 5.42 | 2.39 | 2.83 | 14.0 | 1.19 |
| 32 | 1.00 | 11.14 | 5.21 | 2.79 | 9.26 | 3.02 | 3.27 | 7.21 | 8.19 | 9.94 | 9.60 | 9.77 | 6.86 | 2.23 | 5.4 | 2.7 | 2.3 | 3. | 12.2 | 4.38 | 6.30 | 5.3 | 2.83 | 12.23 | 2.26 | 4.67 | 32.90 | 1.12 |
| 33 Asturias | 1.0 | 4.04 | 2.37 | 1.99 | 8.51 | 2.30 | 2.25 | . 04 | 3.21 | 3.78 | 3.10 | 4.52 | 5.29 | 1.87 | 3.52 | 1.75 | 2.2 | 2.06 | 3.83 | 3.2 | 2.8 | 2.6 | 2.76 | 4.51 | 2.25 | 2.27 | 40 | 1.07 |
| 34 Palencia | 1.00 | 2.28 | 2.72 | . 40 | 5.25 | 11.39 | 3.17 | 10 | 15.07 | 15.59 | 3.97 | 113.73 | 8.26 | 3.11 | 10.48 | 2.43 | 1.84 | 4.06 | 13.39 | 2.06 | 3.43 | 2.71 | 3.01 | 33.16 | 7.58 | 3.40 | 53.2 | 1.13 |
| 35 Palmas | 1.01 | 6.68 | 3.82 | 4.04 | 4.29 | 55 | . 75 | 85 | 36 | 5.79 | 4.59 | 96 | 6.47 | 2.32 | 3.9 | 2.62 | 2.99 | 2.21 | 3.69 | 3.33 | 7.60 | 2.99 | 5.8 | 3.9 | 1.81 | 4.86 | 37. | 1.2 |
| 36 Pontevedra | 1.0 | 29.96 | 7 | 1. | 13.88 | 2.15 | 5.83 | 5.00 | 27 | 29.0 | 6.56 | 5.30 | 7.78 | 1.9 | 9.9 | 2.30 | 2.2 | 2.9 | 4.5 | 5.7 | 3.4 | 4.1 | 3.6 | 2.6 | 2.3 | 5.3 | 14. | 1.11 |
| 37 Salamanca | 1.00 | 7.20 | 4.21 | 2.95 | 7.06 | 11.30 | 4.19 | 4.07 | 4.57 | 15.98 | 2.45 | 5.13 | 29.80 | 4.04 | 3.33 | 2.60 | 2.38 | 3.70 | 4.94 | 6.69 | 5.4 | 2.90 | 22.85 | 9.69 | 3.52 | 2.93 | 32.39 | 1.22 |
| 38 SantaCruz | 1.0 | 7. 19 | 6.96 | 4.61 | 6.26 | 3.73 | 4.95 | 12.42 | 9.82 | 7.67 | 7.34 | 7.45 | 17.87 | 2.80 | 4.50 | 3.78 | 3.85 | 2.52 | 4.55 | 5.07 | 5.15 | 2.73 | 3.20 | 4.16 | 1.68 | 18.78 | 69.30 | 1.37 |
| 39 Cantabria | 1.0 | 15.40 | . 11 | 87 | 19.87 | 3.92 | 1.87 | 2.72 | 2.50 | 4.83 | 3.26 | 4.25 | 6.14 | 2.03 | 4.02 | 1.88 | 1.71 | 1.79 | 2.78 | 2.77 | 2.20 | 2.56 | 2.30 | 5.18 | 2.15 | 2.97 | 5.63 | 1.11 |
| 40 Segovia | 1.01 | 1.66 | 39 | 6.03 | 56 | 13.07 | 4.00 | 17.09 | 5.84 | 7.84 | 2.22 | 28.62 | 14.81 | 5.55 | 8.36 | 3.39 | 1.88 | 6.99 | 6.60 | 2.46 | 11.00 | 2.09 | 2.74 | 7.35 | 4.79 | 5.29 | 43.40 | 1.24 |
| 41 Sevilla | 1.00 | 8.41 | 3.17 | 2.62 | 4.95 | 3.43 | 3.85 | 2.50 | 3.13 | 7.21 | 2.01 | 5.69 | 17.44 | 2.26 | 4.20 | 2.34 | 1.88 | 2.30 | 4.87 | 4.93 | 4.18 | 2.80 | 9.95 | 6.43 | 2.60 | 4.25 | 11.34 | 1.09 |
| 42 Soria | 1.0 | 2.34 | 5.04 | 3.56 | 5.63 | 3.45 | 2.47 | 6.53 | 8.29 | 3.95 | 2.64 | 9.48 | 4.74 | 2.28 | 2.2 | 2.23 | 2.8 | 2.88 | 17.60 | 1.8 | 5.9 | 2.22 | 2.48 | 19.55 | 2.76 | 2.57 | 22.3 | 1.16 |
| 43 Tarragona | 1.0 | 3.73 | 3.71 | 2.22 | 3.27 | 2.62 | 2.12 | 3.95 | 3.18 | 2.42 | 1.83 | 17.95 | 16.10 | 2.15 | 3.17 | 2.92 | 1.70 | 2.41 | 2.78 | 2.48 | 3.50 | 1.94 | 7.61 | 3.59 | 2.66 | 2.38 | 6.89 | 1.31 |
| 44 Teruel | 1.00 | 14.52 | 5.47 | 4.69 | 10.56 | 4.96 | 1.66 | 78.90 | 5.45 | 4.23 | 2.04 | 42.62 | 28.65 | 9.14 | 24.44 | 4.74 | 3.90 | 6.60 | 26.57 | 5.08 | 19.55 | 2.88 | 4.08 | 43.80 | 15.80 | 4.29 | 11.98 | 1.39 |
| 45 Toledo | 1.00 | 3.22 | 3.45 | 2.70 | 3.67 | 3.16 | 1.80 | 8.87 | 5.13 | 5.98 | 2.11 | 10.53 | 24.30 | 2.77 | 5.90 | 3.36 | 2.04 | 3.68 | 4.21 | 2.01 | 5.90 | 3.43 | 2.96 | 12.93 | 4.13 | 4.30 | 31.51 | 1.19 |
| 46 Valencia | 1.0 | 5.12 | 2.40 | 1.76 | 3.36 | 3.75 | 1.90 | 1.98 | 2.27 | 1.97 | 2.20 | 3.57 | 4.36 | 1.57 | 2.4 | 2.01 | 1.59 | 1.6 | 3.94 | 2.4 | 2.95 | 2.10 | 2.52 | 2.54 | 1.99 | 1.99 | 3.81 | 1.16 |
| 47 Valladolid | 1.00 | 3.29 | 3.57 | 3.13 | 6.28 | 3.41 | 2.70 | 5.52 | 3.90 | 4.00 | 2.78 | 4.64 | 5.10 | 2.3 | 2.9 | 1.70 | 1.84 | 2.42 | 5.1 | 2.50 | 3.81 | 3.2 | 2.1 | 54.51 | 2.78 | 2.6 | 9.0 | 1.1 |
| 48 Vizcaya | 1.00 | 9.64 | 2.60 | 1.92 | 6.82 | 3.60 | 2.48 | 3.54 | 5.29 | 3.02 | 2.26 | 6.25 | 12.05 | 1.96 | 1.85 | 1.70 | 1.59 | 1.71 | 2.77 | 2.35 | 1.69 | 2.23 | 2.59 | 5.22 | 2.05 | 2.93 | 4.54 | 1.08 |
| 49 Zamora | 1.00 | 2.66 | 4.32 | 11.83 | 10.64 | 3.69 | 5.14 | 15.71 | 12.62 | 11.77 | 7.03 | 31.93 | 149.34 | 4.82 | 7.54 | 2.92 | 3.33 | 6.03 | 8.58 | 10.81 | 5.94 | 4.92 | 3.61 | 10.31 | 6.19 | 4.69 | 9.08 | 1.14 |
| 50 Zaragoza | 1.00 | 9.96 | 2.30 | 1.62 | 9.31 | 2.81 | 1.77 | 2.14 | 2.34 | 3.02 | 3.16 | 2.45 | 2.89 | 2.38 | 3.07 | 1.71 | 1.50 | 2.31 | 2.68 | 1.83 | 6.04 | 2.23 | 2.18 | 4.69 | 1.67 | 2.23 | 35.88 | 1.20 |
| Spain | 1.01 | 7.83 | 7.28 | 5.36 | 25 | 6.34 | 3.91 | 12.05 | 5.73 | 09 | . 49 | 30 | 14.11 | 85 | 20 | 75 | 2.28 | 4.03 | 4.00 | 3.65 | 4.88 | 68 | 4.60 | 5.99 | 4.02 | 5.06 | 3.5 | 1.39 |

Table 8: Normalized segregation index in Spain as of January 2009 for $\alpha=0.85$ and a neighborhood radius of 400 meters

| nce | E | BU | F | I | PO | P | U | R | UC | R | IA | NI | E | A | 3 O | B | CO | CU | CH | EC | PA | PE | RD | UR | VE | C | PA | $\bar{\sigma}(C, 0.99)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 Alava | 1.00 | 3.24 | 1.72 | . 74 | 89 | 1.86 | 1.72 | . 63 | 1.77 | 1.40 | 1.46 | 1.73 | 1.88 | 1.49 | 1.57 | 1.27 | . 34 | 1.98 | . 86 | 1.41 | 1.54 | 3.08 | 2.02 | . 0 | 1.6 | 1.87 | 2.01 | 1.04 |
| 02 Albacete | 1.00 | 2.90 | 2.58 | 1.82 | 7.23 | 4.95 | 2.57 | 3.27 | 7.66 | 2.88 | 3.33 | 8.06 | 3.96 | 2.09 | 3.15 | 1.86 | 1.55 | 2.77 | 3.57 | 3.02 | 1.61 | 2.30 | 2.2 | 3.3 | 3.2 | 4.0 | 4.48 | 1.15 |
| 03 A | 1.01 | 3.54 | 4.06 | 2.28 | 3.47 | 2.70 | 2.17 | 6.81 | 3.50 | 2.47 | 2.57 | 7.11 | 6.43 | 1.89 | 4.24 | 3.70 | 1.8 | 2.34 | 3.81 | 1.94 | 2.51 | 2.25 | 2.93 | 2.33 | 3.54 | 3.35 | 9.43 | 1.26 |
| 04 A | 1.02 | 3.53 | 4.12 | 3.54 | 4.38 | 3.20 | 2.66 | 2.86 | 3.98 | 6.89 | 3.84 | 6. 24 | 8.05 | . 72 | 7.66 | 3.05 | 2.10 | 68 | . 42 | 4.19 | 14.45 | 5.06 | 5.82 | 6.66 | 3.54 | 4.06 | . 7.5 | 48 |
| 05 Avila | 1.00 | 7.63 | 5.24 | 4.75 | 3.62 | 3.72 | 2.05 | 15.89 | 6.05 | 4.38 | 3.58 | 5.08 | 56.36 | 6.08 | 6.94 | 3.03 | 2.21 | 6.40 | 10.20 | 2.73 | 18.03 | 4.1 | 2.49 | 6.7 | 10.3 | 3.2 | 4.63 | . 20 |
| 06 Badajoz | 1.00 | 18.38 | 5.22 | 4.42 | 12.81 | 3.92 | 5.15 | 11.31 | 6.91 | 5.64 | 2.55 | 10.07 | 18.05 | 4.07 | 4.98 | 2.34 | 2.45 | 4.67 | 15.87 | 3.09 | 7.76 | 6.47 | 5.66 | 15.45 | 10.21 | 4.29 | 16.31 | 1.11 |
| 07 Baleares | 1.00 | 61 | 2.58 | 1.7 | 2.89 | 2.57 | 2.3 | 3.30 | 2.59 | 2.37 | 2.63 | 4.23 | 6.1 | . 41 | 2.9 | 1.8 | 1.66 | 1.69 | 2.03 | 2.0 | 3.48 | 1.9 | 1.9 | 2.22 | 1.9 | 2.6 | 15.7 | 1.22 |
| 08 B | 1.00 | 3.44 | 3.08 | 2.02 | 3.89 | 1.75 | 2.15 | 1.78 | 2.66 | 2.32 | 2.31 | 10.11 | 7.95 | 1.54 | 2.13 | 1.70 | 1.34 | 1.49 | . 75 | 2.00 | 4.51 | 1.90 | 2.32 | 2.5 | 1.56 | 2.73 | 4.64 | 1.18 |
| 09 Burgos | 1.00 | 21 | 85 | 2.76 | 3.66 | 3.32 | 1.87 | 5.31 | 6.53 | 2.10 | 2.12 | 3.26 | 2.37 | 3.08 | . 67 | 1.77 | 1.98 | . 15 | . 79 | 1.74 | . 00 | 2.9 | 2.20 | 19.4 | 2.38 | 2.5 | 5.54 | 1.14 |
| 10 Caceres | 1.00 | 19.33 | 9.67 | 8.16 | 10.85 | 6.67 | 4.95 | 11.01 | 14.83 | 9.20 | 10.79 | 58.60 | 11.30 | 5.09 | 4.60 | 2.98 | 2.67 | 5.99 | 14.55 | 3.55 | 6.41 | 5.01 | 7.3 | 18.7 | 6.5 | 3.7 | 62.88 | . 23 |
| 11 Cadiz | 1.00 | . 24 | 37 | 70 | 4.58 | 5.15 | 12.70 | 5.89 | 4.21 | 4.75 | 3.98 | 9.57 | 8.37 | 3.81 | 3.74 | 3.23 | 2.39 | 2.84 | 4.39 | 3.53 | 5.98 | 2.90 | 2.55 | 11.66 | 3.24 | 2.69 | 21.31 | 1.10 |
| 12 Castellon | 1.01 | 93 | 4.51 | 2.6 | 3.75 | 3.08 | 33 | 6.29 | 09 | 2.02 | 2.02 | 2.82 | 4.24 | 1.83 | 16.07 | 4.96 | 1.46 | 1.92 | 3.55 | 4.34 | 4.48 | 2.61 | 2.73 | 5.74 | 2.77 | 2.08 | 3.83 | 1.18 |
| 13 Ciudad Re | 1.00 | 7.17 | 4.46 | 3.36 | 5.99 | 4.4 | 2.1 | 10.75 | 3.63 | 5.35 | 2.30 | 20.80 | 32.11 | 4.03 | 78 | 3.48 | 2.35 | 5.39 | . 05 | 3.55 | 09 | 3.15 | . 66 | 10.7 | 5.09 | 3.61 | 21.81 | 16 |
| 14 Cordoba | 1.00 | 15.88 | 3.24 | 2.09 | 8.55 | 3.21 | 3.03 | 48 | 6.52 | 7.38 | 13 | . 26 | 7.09 | 4.58 | . 86 | 2.72 | 2.59 | 3.31 | . 74 | 2.79 | 2.76 | 2.8 | 3.55 | 10.4 | 3.3 | 2.6 | 6.96 | 1.06 |
| 15 | 1.00 | 8.82 | 2.60 | 1.99 | 8.11 | 2.55 | 3.98 | 5.06 | 8.27 | 9.34 | 9.45 | 8.40 | 6.82 | 2.37 | 4.00 | 2.93 | 2.09 | 2.43 | 7.88 | 2.92 | 4.62 | 3.34 | 3.01 | 3.08 | 2.48 | 3.28 | 10.23 | 88 |
| 16 Cuenc | 1.00 | 7.75 | 5.98 | 3.90 | 5.59 | 7.77 | 1.64 | . 20 | 2.68 | 4.35 | 2.4 | . 7 | 14.40 | 3.57 | 10.41 | 8.18 | 2.47 | 8.24 | 9.07 | 3.24 | 3.38 | 3.2 | 3.36 | 54.9 | 8.98 | 4.45 | 5.7 | 1.24 |
| 17 Girona | 1.02 | 5.77 | 5.93 | 2.24 | 3.38 | 3.30 | 1.95 | 6.12 | 2.42 | 4.04 | 2.06 | 11.74 | . 07 | 2.38 | 6.78 | 2.71 | 1.88 | 2.32 | 3.25 | 2.44 | 7.31 | 2.99 | 3.37 | 3.48 | 2.56 | 4.73 | 5.03 | 1.37 |
| 18 Granada | 1.00 | 16 | 2.91 | 2.76 | 5.62 | 3.57 | 5.14 | 2.46 | 3.71 | 4.89 | 3.50 | . 05 | 15 | . 10 | 32 | 2.55 | 2.39 | 2.90 | . 49 | . 24 | . 70 | 3.85 | 3.82 | 7.5 | 3.4 | 3.18 | 7.03 | 17 |
| 19 Guadalajar | 1.01 | 7.39 | 3.42 | 2.04 | 3.03 | 6.38 | 1.53 | 3.44 | 5.30 | 2.76 | 2.05 | 6.38 | 12.82 | 2.18 | 5.34 | 3.83 | 1.52 | 2.55 | 3.07 | 1.96 | 5.31 | 1.67 | 2.20 | 3.62 | 2.66 | 2.8 | 7.12 | 1.23 |
| 20 Guipuzca | 00 | 58 | . 49 | . 07 | 69 | 1.95 | 5.10 | 2.61 | 2.14 | 2.65 | 2.32 | 7.90 | 13.03 | 1.73 | 3.15 | 1.79 | 1.65 | 1.64 | 3.90 | 1.72 | 2.87 | 2.30 | 1.91 | 4.14 | 2.11 | 2.59 | 7.62 | 1.09 |
| 21 Huelva | 1.0 | 5.61 | 3.33 | 2.97 | 5.21 | 5.25 | 2.59 | 6.36 | 2.81 | 5.33 | 3.03 | 4.02 | 3.55 | 3.40 | 3.40 | 2.89 | 2.33 | 2.79 | 11.87 | 5.00 | 11.84 | 3.81 | 3.83 | 11.24 | 3.43 | 2.76 | 20.64 | 1.19 |
| 22 Huesca | 1.00 | 5.95 | 5.16 | 3.08 | 4.68 | 3.75 | 1.77 | 3.41 | 2.77 | 3.28 | 2.50 | 6.01 | 5.14 | 2.79 | 14.10 | 3.08 | 3.08 | 3.78 | 5.13 | 2.65 | 6.14 | 3.64 | 2.37 | 4.98 | 3.48 | 19.06 | 15.17 | 1.25 |
| 23 J | 1.00 | 15 | 3.09 | 3.70 | 14.15 | 4.24 | 2.25 | 2.74 | 8.82 | 3.16 | 3.59 | 6.11 | 6.47 | 65 | 4.06 | 3.6 | 2.58 | 99 | 14.73 | 2.67 | 5.93 | 4.14 | 4.94 | 17.11 | 8.48 | 2.78 | 5.94 | 1.07 |
| 24 L | 1.0 | 37 | 3.11 | 2.73 | 8.65 | 4.07 | 2.40 | 4.98 | 6.28 | 4.19 | 2.76 | 6.37 | 17.12 | 2.50 | 6.88 | 1.85 | 2.14 | 2.76 | 10.95 | 3.17 | 5.34 | 2.76 | 2.65 | 6.32 | 2.26 | 3.81 | 26.02 | 1.13 |
| 25 Lleida | 1.01 | 32 | 7.62 | 2.08 | 3.29 | 7.28 | 1.54 | 1.83 | 10.13 | 2.34 | 1.74 | 3.47 | 3.10 | 2.02 | 4.10 | 3.55 | 1.81 | 3.10 | 5.93 | 2.95 | 5.14 | 3.33 | 2.38 | 3.62 | 3.97 | 3.47 | 3.66 | 1.30 |
| 26 Rioja | 1.0 | 2.61 | 2.37 | 1.85 | 9.33 | 6.06 | 1.86 | 3.32 | 5.49 | 3.90 | 2.65 | 2.33 | 2.87 | 2.03 | 2.00 | 2.01 | 1.98 | 1.99 | 21.96 | 2.06 | 3.42 | 7.51 | 2.43 | 7.30 | 2.34 | 2.5 | 2.34 | 1.25 |
| 27 L | 1.00 | 32 | 4.25 | 2.67 | 38. | 1.83 | 3.08 | 8.51 | 7.53 | 15.88 | 4.20 | 6.31 | 20.9 | 2.74 | 5.69 | 2.66 | 2.3 | 2.5 | 14.8 | 4.0 | 5.47 | 9.62 | 3.12 | 3.57 | 2.83 | 4.73 | 8.16 | 1.10 |
| 28 M | 1.00 | 2.83 | 6.71 | 1.69 | 2.16 | 1.66 | 2.61 | 1.83 | 2.06 | 2.14 | 2.64 | 5.10 | 5.82 | 1.39 | 2.27 | 1.69 | 1.38 | 1.38 | 2.15 | 1.76 | 1.89 | , | 1.94 | 2.2 | 2.05 | 2. | 1.53 | 1.19 |
| 29 Malaga | 1.00 | 2.58 | 3.20 | 2.30 | 3.93 | 2.76 | 2.22 | 4.71 | 2.02 | 4.34 | 1.82 | 2.88 | 6.11 | 1.69 | 3.72 | 2.36 | 1.83 | 2.38 | 2.37 | 5.09 | 2.01 | 2.32 | 3.13 | 2.26 | 2.13 | 2.74 | 6.17 | 1.14 |
| 30 Murcia | 1.01 | 4.52 | 4.03 | 2.47 | 6.29 | 4.85 | 2.64 | 3.33 | 3.13 | 6.17 | 2.46 | 5.79 | 10.89 | 2.06 | 2.04 | 2.56 | 2.05 | 2.65 | 4.23 | 1.88 | 14.88 | 4.93 | 2.71 | 4.90 | 2.87 | 2.46 | 38.64 | 1.27 |
| 31 Navarra | 1.00 | 2.47 | 6.23 | 1.83 | 3.12 | 2.41 | 1.98 | 2.57 | 2.43 | 5.29 | 4.43 | 4.65 | 3.56 | 1.99 | 2.46 | 2.08 | 1.70 | 2.34 | 2.96 | 1.87 | 4.06 | 2.01 | 2.41 | 5.22 | 2.27 | 2.59 | 13.91 | 1.19 |
| 32 O | 1.00 | 11.02 | 5.19 | 2.75 | 9.13 | 3.02 | 3.14 | 5.76 | 7.84 | 9.21 | 9.54 | 9.21 | 4.54 | 2.19 | 4.58 | 2.70 | 2.3 | 3.1 | 11.8 | 3.59 | 6.12 | 5.0 | 2.65 | 12.0 | 2.15 | 4.22 | 32.30 | 1.11 |
| 33 Astur | 1.00 | 81 | 2.26 | 1.92 | 8.48 | 2.24 | 2.22 | . 81 | 3.09 | 3.23 | 3.02 | 3.72 | 3.91 | . 83 | 3.18 | 1.6 | 2.05 | 2.01 | 3.64 | 2.9 | 2.7 | 2.3 | 2.6 | 4.3 | 2.1 | 2.1 | 5.15 | . 6 |
| 34 Palencia | 1.00 | 2.23 | 2.70 | 2.33 | 5.20 | 11.38 | 3.14 | 3.74 | 14.92 | 15.37 | 3.93 | 113.39 | 6.23 | 3.03 | 10.39 | 2.38 | 1.66 | 3.16 | 12.96 | 1.97 | 3.39 | 2.58 | 2.72 | 31.06 | 7.39 | 3.15 | 53.01 | 1.12 |
| 35 Palmas | 1.01 | 6.64 | 3.76 | 4.01 | 4.20 | 4.53 | 8.68 | 3.68 | 4.15 | 5.54 | 4.49 | 3.72 | 6.06 | 2.28 | 3.67 | 2.44 | 2.97 | 2.17 | 3.59 | 3.24 | 7.40 | 2.92 | 5.66 | 3.91 | 1.74 | 4.49 | 37.37 | 1.27 |
| 36 Pontevedr | 1.0 | 29.47 | 3.03 | 1.88 | 9.47 | 2.14 | 5.70 | 4.58 | 6.78 | 28.97 | 6.51 | 64 | 4.88 | 1.86 | 5.54 | 2.19 | 2.23 | 2.75 | 4.19 | 4.45 | 2.94 | 3.89 | 3.49 | 2.44 | 2.24 | 4.95 | 8.48 | 1.10 |
| 37 Salamanca | 1.00 | 7.18 | 4.18 | 2.80 | 6.98 | 11.29 | 4.17 | 3.95 | 4.39 | 12.22 | 2.41 | 4.85 | 29.75 | 3.97 | . 11 | 2.51 | 2.2 | 3.63 | 4.79 | 6.5 | 5.03 | 2.7 | 22.81 | 9.1 | 3.3 | 2.6 | 30.72 | 1.21 |
| 38 SantaCruz | 1.01 | 7.15 | 6.95 | 4.60 | 6.25 | 3.72 | 4.94 | 12.41 | 9.79 | 7.61 | 7.34 | 7.35 | 17.84 | 2.78 | 3.91 | 3.73 | 3.84 | 2.50 | 4.50 | 5.01 | 4.54 | 2.61 | 3.04 | 4.15 | 1.66 | 18.69 | 69.28 | 1.36 |
| 39 Cantabria | 1.00 | 15.38 | 2.08 | 1.85 | 19.81 | 3.90 | 1.85 | 2.65 | 2.39 | 3.98 | 3.07 | 3.92 | 5.52 | 2.00 | 3.34 | 1.86 | 1.68 | 1.76 | 2.59 | 2.62 | 2.04 | 2.45 | 2.22 | 5.09 | 2.10 | 2.71 | 5.27 | 1.11 |
| 40 Segovia | 1.00 | 64 | 5.26 | 5.90 | 2.52 | 13.05 | 4.00 | 17.00 | 5.77 | 7.55 | 2.21 | 27.79 | 14.19 | 5.39 | 8.27 | 3.37 | 1.89 | 6.91 | 6.47 | 2.37 | 10.65 | 2.01 | 2.67 | 7.29 | 4.54 | 5.05 | 43.11 | 1.24 |
| 41 Sevilla | 1.00 | 6.32 | 2.55 | 2.15 | 4.55 | 3.16 | 3.68 | 2.24 | 2.84 | 6.77 | 1.81 | 4.15 | 16.47 | 2.10 | 3.11 | 2.24 | 1.72 | 2.10 | 4.10 | 3.40 | 3.37 | 2.37 | 8.33 | 5.81 | 2.32 | 3.80 | 6.82 | 1.07 |
| 42 Soria | 1.00 | 2.31 | 5.03 | 3.38 | 5.61 | 3.45 | 2.47 | 6.41 | 8.28 | 3.79 | 2.63 | 8.99 | 3.61 | 2.26 | 2.16 | 2.21 | 2.85 | 2.84 | 17.53 | 1.80 | 5.68 | 2.13 | 2.46 | 19.41 | 2.71 | 2.30 | 21.79 | 1.15 |
| 43 Tarragona | 1.01 | 3.71 | 3.70 | 2.21 | 3.23 | 2.59 | 2.11 | 3.93 | 3.17 | 2.30 | 1.76 | 17.45 | 16.08 | 2.14 | 2.85 | 2.90 | 1.67 | 2.39 | 2.70 | 2.46 | 3.38 | 1.91 | 7.55 | 3.56 | 2.60 | 2.30 | 6.48 | 1.30 |
| 44 Teruel | 1.00 | 14.48 | 5.40 | 4.64 | 10.56 | 4.94 | 1.65 | 78.88 | 5.41 | 3.98 | 2.04 | 42.62 | 28.63 | 9.08 | 24.43 | 4.72 | 3.86 | 6.56 | 26.51 | 5.06 | 19.48 | 2.86 | 4.05 | 43.77 | 15.70 | 4.02 | 11.85 | 1.38 |
| 45 Toledo | 1.00 | 3.14 | 3.42 | 2.67 | 3.66 | 3.13 | 1.79 | 8.78 | 5.10 | 5.79 | 2.10 | 10.52 | 23.67 | 2.74 | 5.85 | 3.35 | 2.04 | 3.67 | 4.03 | 1.99 | 5.61 | 3.40 | 2.93 | 12.86 | 4.07 | 4.14 | 31.51 | 1.19 |
| 46 Valencia | 1.00 | 5.03 | 2.30 | 1.64 | 3.29 | 3.69 | 1.87 | 1.79 | 2.17 | 1.79 | 2.06 | 2.89 | 3.79 | 1.52 | 2.31 | 1.93 | 1.53 | 1.51 | 3.74 | 2.08 | 2.58 | 1.90 | 2.26 | 2.41 | 1.88 | 1.76 | 3.12 | 1.14 |
| 47 Valladolid | 1.00 | 24 | 3.43 | 3.02 | 6.04 | 3.38 | 2.64 | 5.36 | 3.75 | 3.12 | 2.30 | 13.79 | 4.32 | 2.23 | 2.60 | 1.64 | 1.78 | 2.34 | 4.41 | 2.19 | 3.13 | 3.15 | 1.96 | 54.48 | 2.63 | 2.46 | 7.95 | 1.10 |
| 48 Vizcaya | 1.00 | 9.34 | 2.27 | 1.78 | 6.50 | 3.56 | 2.44 | 2.95 | 5.01 | 2.31 | 1.92 | 4.13 | 10.41 | 1.89 | 1.61 | 1.62 | 1.50 | 1.59 | 2.55 | 2.19 | 1.54 | 1.95 | 2.40 | 4.96 | 1.92 | 2.24 | 3.68 | 1.07 |
| 49 Zamora | 1.00 | 2.63 | 4.25 | 11.78 | 5.66 | 3.68 | 5.14 | 15.29 | 12.56 | 11.46 | 6.88 | 12.44 | 146.65 | 4.76 | 7.30 | 2.78 | 3.32 | 5.95 | 8.00 | 10.77 | 5.67 | 4.86 | 3.51 | 10.14 | 5.85 | 3.82 | 6.50 | 1.14 |
| 50 Zaragoza | 1.00 | 9.92 | 2.21 | 1.57 | 9.27 | 2.74 | 1.74 | 2.02 | 2.29 | 2.67 | 2.90 | 1.94 | 2.20 | 2.32 | 2.84 | 1.64 | 1.45 | 2.23 | 2.50 | 1.67 | 5.70 | 2.10 | 2.04 | 4.56 | 1.61 | 2.02 | 35.69 | 1.18 |
| Spain | 1.00 | 7.69 | 7.06 | 5.18 | 6.11 | 6.27 | 3.86 | 11.87 | 5.53 | 6.56 | 4.26 | 8.31 | 13.09 | 2.78 | 3.78 | 2.61 | 2.23 | 3.94 | 3.85 | 3.40 | 4.57 | 3.49 | 4.06 | 5.87 | 3.92 | 4.24 | 16.13 | 1.35 |

Table 9: Normalized segregation index in Spain as of January 2009 for $\alpha=0.99$ and a neighborhood radius of 400 meters.


[^0]:    *We are very grateful to Antonio Cabrales, Matthew Jackson, Alfonso Rosa and Yves Zenou for very fruitful discussions. Two anonymous referees helped us to improve the paper significantly. We also thank the seminar/conference participants at ASSET (Alicante), IMEBE (Bilbao), FEDEA, Alicante, Bilbao, Lisbon, Murcia, Saarbrücken, and Valencia for many very helpful comments. It would have been impossible to conduct the empirical analysis without the financial support of FEDEA.
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[^1]:    ${ }^{1}$ See, among others, Benabou (1993), Borjas (1995), Boeri et al. (2012), Card and Rothstein (2007), Cutler and Glaeser (1997), Edin et al. (2003), Kling et al. (2007) and Zenou (2009).

[^2]:    ${ }^{2}$ People randomly meet friends, friends of friends, or higher-order acquaintances. Also, socioeconomic relationships are usually recursive, self-enforcing, and with feedback effects. For example, Jackson and Rogers (2007) show for several situations that a random link formation process matches empirical networks very well.
    ${ }^{3}$ Since both individuals are chosen at random, the measure is controlling for group sizes. It is also robust to the number of census tracts, the definition of the boundaries of census tracts, and the population size. We nevertheless also define the group-size-dependent measure $\sigma_{g}$ according to which a randomly chosen individual will meet any individual from the same group when the random walk terminates. All our theoretical results hold for both the group-size-dependent and the normalized measure.

[^3]:    ${ }^{4}$ We also formally relate the segregation index to the dimension of evenness by showing that the normalized isolation index is minimized if the individuals of a group are equally distributed over all nodes (Proposition 4). However, uneven distributions can lead to even lower levels of segregation as soon as the network is introduced.

[^4]:    ${ }^{5}$ There is no need to assume that the graph is symmetric. Asymmetric graphs occur, for instance, when $\mathbf{A}$ represents a social communication structure. Also, friendship networks are not necessarily symmetric. Finally, the mobility between two different social strata could be more sticky depending on the direction of movement.

[^5]:    ${ }^{6}$ To see this, note that since every node has an out-link $\left(a_{i}>0\right)$, the expected length of a walk is independent of its origin. Now, take any initial node $\omega_{0}$. The random-walk continues with probability one to $\omega_{1}$. But the random-walk starting at $\omega_{1}$ has, due to the independence of the origin, an expected length of $\alpha$ times $l(\alpha)$. Hence, $\mathbb{E}(l)=1+\alpha \mathbb{E}(l)$.
    ${ }^{7}$ It is important to note that the model parameter $\alpha$ gives raise not just to a single measure but to a family of measures, one for each $\alpha$. This allows us to analyze the phenomenon of segregation as a function of the spatial mobility. In particular, it will become clear in the empirical analysis that a comparison of the degree of the segregation for different $\alpha$ uncovers group clustering (network effects).

[^6]:    ${ }^{8}$ In the literature on social networks, clustering refers to the probability that two neighbors of a given individual have a direct link between themselves. The two concepts have to be carefully distinguished.

[^7]:    ${ }^{9}$ They write on page 293: "..., suppose we have two urban areas with the same number of minority members, who comprise the same proportion of the total population. In each place, no minority member shares a common residential area with a majority member, all minority areas are located the same average distance from the central business district, and all areas are of the same geographic size. In this case, both urban areas would display identical measures of evenness, exposure, concentration, and centralization. However, if all minority areas in one of the urban areas were contiguous to one another, but in the other area they were separated from one another, then we would probably consider the former urban area to be more segregated, since all minority members live within one single homogeneous ghetto, compared to the latter area, where they reside in minority neighborhoods that are scattered throughout the urban area."

[^8]:    ${ }^{10}$ See Wasserman and Faust (1994) for an excellent overview of centrality measures.

[^9]:    ${ }^{11}$ There is a vast literature that recognizes the importance of centrality in determining socioeconomic outcomes. Examples include eduction (Calvo-Armengol et al. 2009), criminal behavior (Haynie 2001), worker's performance (Mehra et al. 2001), power in organizations (Brass 1984), and the formation and performance of R\&D networks (Boje and Whetten 1981, Powell et al. 1996 and Uzzi 1997).

[^10]:    ${ }^{12}$ Section 4 shows that the Spectral Segregation Index $(S S I)$ does not relate directly to the dimension of centralization because it only considers the network of within-group interactions. In the example, it misses that the blacks are connected to a more central square than the whites.
    ${ }^{13}$ Note that $\mathbf{P}$ is a sparse matrix meaning that the number of non-zero entries in each row is negligible. Thus, for large datasets (over 5,000 nodes), it is key to work with special data structures representing sparse matrices (sparse function in Matlab and SparseArray function in Mathematica). Otherwise, one spends a considerable amount of memory space to store zeroes that do not affect matrix multiplications. Also, in order to compute $\sigma_{g}$, it is not necessary to determine all connected components even though the measure is component-separable by definition. Finally, $\sigma_{g}$ has a computational advantage over the $S S I$ : The asymptotic convergence rates of the $S S I$ can be very low compared to those of $\sigma_{g}$, which are bounded if $\alpha$ is well below 1 .

[^11]:    ${ }^{14}$ The next section presents an extension of the $S S I$ to a setting with multiple inhabitants in the same node.
    ${ }^{15}$ For the sake of simplicity, given any such matrix $\mathbf{P}^{g}$, we will also use $\mathbf{P}^{g}$ to refer to the network corresponding to $\mathbf{P}^{g}$. Formally, the subgraph $\mathbf{P}^{g, \gamma}$ is said to be a strongly connected component of the network represented by $\mathbf{P}^{g}$ if $\mathbf{P}^{g, \gamma}$ is a network of maximal size such that there is a path between any pair of its nodes.
    ${ }^{16}$ Proposition 13 in Echenique and Fryer (2007) shows that the $S S I$ is approximately proportional to the probability that two individuals from the same social group meet without leaving the subgroup network. Hence, the $S S I$ is also related to a probability but, at the same time, differs substantially from the segregation index. Indeed, for $\sigma_{g}$ it does not matter whether $i$ meets somebody from a different group on his way to $j$, yet the walks undertaken are restricted to within group interactions according to the $S S I$. This important distinction can lead to substantial differences in applications; i.e., our empirical analysis in the next section shows that the correlation between the segregation index and the $S S I$ can be rather low.

[^12]:    ${ }^{17}$ However, we also note that problems still arise when $\mathbf{P}^{g}$ is connected but near disconnectedness. In that case, the $S S I$ can still display very unstable behavior.
    ${ }^{18}$ Note that Proposition 5 on page 475 indicates continuity of $S S I\left(\mathbf{P}^{g}\right)$ in the entire network $\mathbf{P}^{g}$, which is not true. Indeed, $S S I\left(\mathbf{P}^{g}\right)$ is continuous as long as $\mathbf{P}^{g}$ is connected.

[^13]:    ${ }^{19}$ Our analysis excludes immigrants from Britain and Germany who amount to more than $1 \%$ of the Spanish population because these groups can be expected to be less of a "social problem" than poor migrants from Africa. Many of them are pensioners who bought second homes in the coastal area of the Mediterranean Sea and it is not clear how much time they actually spend in these residences. We are very grateful to an anonymous referee for pointing out this effect.

[^14]:    ${ }^{20}$ Even though the network is constructed from geographical positioning data, we nevertheless proxy true social interactions. This is so because geographical proximity is correlated to close relationships, despite the fact that the new era of information has made weak social links less dependent on physical distance (see, Goldenberg and Levy 2009 and Mok et al. 2010). Also, our qualitative results remain identical for radii of 1,000 and 1,500 meters.
    ${ }^{21}$ The numerical results for $\alpha \in\{0.00 ; 0.50 ; 0.85 ; 0.99\}$ and the normalized isolation index are detailed for all groups and all provinces in Appendix B. Setting the continuation probability $\alpha$ equal to 0.85 is a prominent choice in applications related to PageRank because in this way, relevant network effects are introduced, and the analysis is not compromised with computation inefficiencies or ill-conditioned problems that can appear if $\alpha$ grows closer to 1 .

[^15]:    ${ }^{22}$ The British and the Germans that were excluded from our study because of the before mentioned reasons show a very similar residence pattern to that of the Russians. They live highly segregated in few areas, in particular in Alicante and the Balearic Islands (province 07), so that their network effect is rather small. Actually, the British and the Germans are two most segregated groups if $\alpha=0.85$ (the Pakistanis remain to be the most segregated group if the normalized segregation index is applied).

[^16]:    ${ }^{23}$ Modelling citation patterns using transition matrices is standard in the literature. See, for instance, Palacios-Huerta and Volij (2004), and impact measures like Eigenfactor ${ }^{\mathrm{TM}}$, Article Influence ${ }^{\mathrm{TM}}$ and SCImago Journal Rank.

[^17]:    ${ }^{24}$ http://www.cefage.uevora.pt/en/links/revistas_cientificas_rankings.

[^18]:    ${ }^{25}$ Alternatively, one could also follow an axiomatic approach to rationalize the measure. See, Palacios-Huerta and Volij (2004) and Frankel and Volij (2010) for related examples.

[^19]:    ${ }^{26}$ The latter equations can be verified with the help of the proof of Theorem 1.

