

# Plants and Productivity in International Trade

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# Overview

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## Aim of the paper

A model of **International Trade** to analyze the **Producer Level**  
Three Crucial Elements:

- Heterogeneity of Plants
- Coexistence of exporters and purely domestic producers
- Imperfect Competition with variable markups

# Literature

- Empirical literature examining international trade at the level of individual producers
- Alternative to Melitz (2003) theoretical model
- **Ricardian model** → Dornbusch, Fischer, Samuelson (1977)
- **Extension to N countries** → Eaton and Kortum (2002)

⇒ **Imperfect Competition**

## Exporter Facts

- 14% of US manufacturing production is exported
- Only 21% of all plants report exports
- Even exporting plants sell mostly at home
- On average exporting plants are much bigger

## Exporter Facts continued

- Exporting not an industry phenomenon
- Large productivity differences within industries
- Higher Productivity among exporters
- Factor intensity even less informative about the productivity advantage of exporters than industry

## Basic Setup

- N countries
- continuum of goods  $j \in [0, 1]$
- Constant elasticity of substitution  $\sigma > 0$

# Demand

Expenditure on good  $j$  in country  $n$ :

$$X_n(j) = x_n \left( \frac{P_n(j)}{p_n} \right)^{1-\sigma} \quad (1)$$

where

- $P_n(j)$  is the price of good  $j$  in country  $n$
- $x_n$  total expenditure
- $p_n = \left[ \int_0^1 P_n(j)^{1-\sigma} \right]^{\frac{1}{1-\sigma}}$  price index for country  $n$

## Production and Transportation

- The  $k$ 'th most efficient producer of good  $j$  in country  $i$  can convert one bundle of input into a quantity  $Z_{ki}(j)$
- Iceberg assumption on transportation costs:  $d_{ni} \geq 1$

Triangle Inequality on geographic barrier parameters:

$$d_{ni} \leq d_{nk}d_{ki}, \forall k \quad (2)$$

## Production and Transportation continued

- Inputs are mobile within countries, but not between countries
- $w_i$  is the cost of an input bundle in country  $i$

The  $k$ 'th most efficient producer of good  $j$  in country  $i$  can export one unit of output to country  $n$  at cost:

$$C_{kni}(j) = \left( \frac{w_i}{Z_{ki}(j)} \right) d_{ni} \quad (3)$$

Under perfect competition:

$$C_{1n}(j) = \min_i \{ C_{1ni}(j) \} \quad (4)$$

# Bertrand Competition

- Each market is served by the lowest cost supplier of each good  $j$
- Constrained not to charge more than the second-lowest cost of supplying the market

$$C_{2n}(j) = \min_i \left\{ C_{2ni^*}(j), \min_{i \neq i^*} C_{1ni}(j) \right\} \quad (5)$$

The price of good  $j$  in market  $n$ :

$$P_n(j) = \min \{ C_{2n}(j), \bar{m} C_{1n}(j) \} \quad (6)$$

# A Probabilistic Formulation

Need to know  $Z_{1i}(j)$  and  $Z_{2i}(j) \Rightarrow$  random variables drawn from probability distributions (eg Frechet)

Joint distribution of  $Z_{1i}(j)$  and  $Z_{2i}(j)$ :

$$F_i(z_1, z_2) = Pr[Z_{1i} \leq z_1, Z_{2i} \leq z_2] = [1 + T_i(z_2^{-\theta} - z_1^{-\theta})]e^{-T_i z_2^{-\theta}} \quad (7)$$

for  $0 \leq z_2 \leq z_1$

- $\theta > 1$ , governs gains from trade due to comparative advantage
- $T_i$  governs absolute advantage

## Probabilistic Formulation continued

The joint distribution of the lowest cost  $C_{1n}$  and second lowest cost  $C_{2n}$

$$G_n(c_1, c_2) = Pr[C_{1n} \leq c_1, C_{2n} \leq c_2] = 1 - e^{-\Phi_n c_1^\theta} - \Phi_n c_1^\theta e^{-\Phi_n c_2^\theta} \quad (8)$$

for  $c_1 \leq c_2$ , where the cost parameter  $\Phi_n$ :

$$\Phi_n = \sum_{i=1}^N T_i (w_i d_{ni})^{-\theta} \quad (9)$$

# Analytic Results

- The probability  $\pi_{ni}$  that country  $i$  is the low cost supplier to  $n$  for any particular good is just  $i$ 's contribution to the cost parameter  $\Phi_n$ :

$$\pi_{ni} = T_i(w_i d_{ni})^{-\theta} / \Phi_n \quad (10)$$

- The distribution  $G_n(c_1, c_2)$  applies not only to the first- and second-lowest costs of supplying a good to country  $n$  regardless of source, but also to those costs conditional on the nationality of the low-cost supplier

## Analytic Results continued

- The markup  $M_n(j) = P_n(j)/C_{1n}(j)$  is the realization of a random variable  $M_n$  drawn from a Pareto distribution truncated at the monopoly markup:

$$H_n(m) = Pr[M_n \leq m] = \begin{cases} 1 - m^{-\theta} & 1 \leq m < \bar{m} \\ 1 & m \geq \bar{m} \end{cases} \quad (11)$$

- Assuming  $\sigma < 1 + \theta$ , the exact price index in country  $n$  implied by (1) is:

$$p_n = \gamma \Phi_n^{-1/\theta} \quad (12)$$

## Analytic Results continued

- The share that country  $n$  spends on goods from country  $i$  is also the fraction of goods it purchases from there:

$$\frac{X_{ni}}{X_n} = \pi_{ni} \quad (13)$$

This relationship provides the link between the model and data on aggregate bilateral trade

- The share of variable costs in aggregate revenues is  $\theta/(1 + \theta)$ . This share applies to the set of active producers in any source country  $i$

# Efficiency and Measured Productivity

- Comparisons of measured productivity across plants reflect only differences in their markups
- conditional on a level of efficiency  $z_1$ , the distribution of the markup is:

$$H_n(m|z_1) = Pr[M_n \leq m|z_1] = \begin{cases} 1 - e^{-\Phi_n w_1^{-\theta} (m^\theta - 1)} & 1 \leq m < \bar{m} \\ 1 & m \geq \bar{m} \end{cases}$$

- A plant with a higher efficiency is likely to have a higher markup as well

# Efficiency and Exporting

Consider the best potential producer of good  $j$  from country  $i$ :

- In order to sell **at home**,  $Z_{1i}(j)$  must satisfy:

$$Z_{1i}(j) \geq Z_{1k}(j) \frac{w_i}{w_k d_{ik}} \forall k \neq i$$

- But to sell in some **other market n**:

$$Z_{1i}(j) \geq Z_{1k}(j) \frac{w_i d_{ni}}{w_k d_{nk}} \forall k \neq i$$

⇒ Variation in underlying efficiency explains the coexistence of exporting plants and plants that sell only to the domestic market

## Efficiency and Size

Exporting plants tend to have higher domestic sales than plants that don't export:

- Greater efficiency raises the probability of exporting **and** it will likely result in a lower domestic price
- for  $\sigma > 1$  lower prices translate into more spending

## Quantification

- Fitting the model to bilateral trade among the US and 46 major trade partners
- Simulation Approach
- Reformulation of the model as an algorithm, which uses data on aggregate trade shares and expenditures to simulate plant level statistics
- Estimation of the two heterogeneity parameters  $\theta$  and  $\sigma$  to make the simulated data match the actual productivity advantage of exporters
- Report how well the other moments of the simulated data line up with the remaining facts discussed in section 1

# General Equilibrium

- Assume that there is a tradable nonmanufactured good produced in each country  $n$  competitively with labor productivity  $W_n$  which serves as numeraire
- The manufacturing sector in country  $n$  thus faces an elastic labor supply at wage  $W_n$
- Given wages, manufacturing price levels in different countries are connected through trade in intermediates

# Counterfactuals

Consider two aggregate shocks to the world trading regime:

- 1 A 5% world-wide decline in geographic barriers
  - Productivity measure increases by 4.7%
  - Over 3% of US plants exit
  - Net job loss is 1.3%
- 2 A 10% exogenous appreciation of the US wage relative to wages in other countries
  - measured US manufacturing productivity rises by 4.2%
  - Together substitution, reallocation and exit generate a 13% fall in manufacturing employment

# Criticism

- Distribution of markups invariant to country characteristics and geographic barriers (Melitz and Ottaviano)
- No international trade barriers
- Homogeneous labor
- No industry specific parameters
- No dynamics

## Possible Extensions

- Trade policies
- Exports vs FDI (Helpman, Melitz, Yeaple)
- Productivity growth of exporters vs purely domestic producers (Bernard, Jensen)
- Export destinations (Eaton, Kortum, Kamarz)
- Small Economy Case

# Conclusion

- Combination of Micro and Macro level data
- Explains the coexistence of exporters and purely domestic producers
- Many extensions possible

## Questions, Comments, Criticism?

## Reference

Bernard, Eaton Kortum 'Plants and Productivity in International Trade' American Economic Review, September 2003