Universidad Carlos III de Madrid <u>ECONOMETRICS</u> Academic year 2009/10 FINAL EXAM May 17, 2010

DURATION: 2 HOURS

- 1. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3:
 - (a) The effect of education is not statistically different from zero.
 - (b) The effect of education does not vary over time.
 - (c) The effect of education is more negative in 1984 than in 1972.
- 2. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the year does not affect the number of children:
 - (a) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8$.
 - (b) The null hypothesis is $H_0: \delta_5 = \delta_6 = 0.$
 - (c) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8 = 0.$
- 3. Comparing the models (I) and (II):
 - (a) None of the other statements are correct.
 - (b) Model (I) is more restrictive, because it imposes that in year 1972 education does not have an impact on the number of children.
 - (c) Model (II) is less restrictive, because it allows for a given race, age and education, that fertility rates change differently over time.
- 4. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the variance of the dependent variable (rounding to two decimals), conditional on the explanatory variables is:
 - (a) 1.60.
 - (b) 2.79.
 - (c) 2.56.
- 5. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5
 - (b) Estimating by OLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5B.
 - (c) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the instruments MEDUC and <u>FEDUC</u>.

Exam Type: $\begin{bmatrix} FEDUC \\ 1 \end{bmatrix}$

- 6. If education was an endogenous variable, in order to test whether two instruments, father's and mother's education, are valid instruments, we would have to:
 - (a) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these two instruments are individually significant.
 - (b) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these last two variables are jointly significant.
 - (c) Test the hypothesis that the residual of the reduced form (the linear projection of EDUC on the exogenous variables and both instruments) has a significant effect on education.
- 7. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education for a women observed in 1978 is the same than the one observed in 1984, the null hypothesis would be:
 - (a) $\delta_4 = \delta_7 = \delta_8.$
 - (b) $\delta_7 = \delta_8 = 0.$
 - (c) $\delta_7 = \delta_8$.
- 8. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients (and rounding to two decimals), for a 20 year old white woman with 10 years of education:
 - (a) The mean number of children is approximately 6.24.
 - (b) The mean number of children was approximately 0.19 in 1972.
 - (c) There is not enough information to predict the mean number of children in 1972.
- 9. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the effect of education on the number of children does not depend on the year, the null hypothesis is:
 - (a) The null hypothesis is $H_0: \delta_7 = \delta_8 = 0.$
 - (b) The null hypothesis is $H_0: \delta_7 = \delta_8$.
 - (c) The null hypothesis is $H_0: \delta_4 = \delta_7 + \delta_8$.
- 10. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results (rounding to one decimal):
 - (a) The test statistic is approximately t = 3.9.
 - (b) The test statistic is approximately t = -1.2.
 - (c) The test statistic is approximately t = -1.9.
- 11. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the unconditional variance of the dependent variable is:
 - (a) 1.60.
 - (b) 2.79.
 - (c) 2.56.

- 12. Assume that model (I) verifies the assumptions of the classical regression model. If the variable KIDS was measured with error, estimates in the Output 1 will be in general:
 - (a) None of the other statements are correct.
 - (b) Consistent.
 - (c) Less efficient that the ones obtained if the variable KIDS was not measured with error.
- 13. Comparing the models (II) and (III), indicate which of the following statements is FALSE:
 - (a) When estimating model (III) by OLS, we see that education does not longer have a significant effect on fertility.
 - (b) Model (II) is more restrictive, because it imposes that the effect of education does not depend on time (the year).
 - (c) At the 5% significance level we would choose Model (II).
- 14. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) None of the other statements are correct.
 - (b) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5B as an instrument for education.
 - (c) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5 as an instrument for education.
- 15. If you only had information about the number of children, the best prediction you can give about the value of this variable (rounding up to two decimals) is:
 - (a) 2.20.
 - (b) 2.67.
 - (c) 1.67.
- 16. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, the mean difference in the number of children between two women with the same characteristics but one in 1972 and the other in 1978 is:
 - (a) The question cannot be answered with the information provided in Output 2.
 - (b) Significantly different from zero.
 - (c) Statistically equal to zero.
- 17. Assume that model (I) verifies the assumptions of the classical regression model. Under the evidence of Output 1, the effect of age on the number of children is:

(a) Positive, but marginally decreasing in age for women who are younger than 40.

- (b) Constant.
- (c) Negative for women older than 35 years old.
- 18. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3, and taking into account only women younger than 40 years old, indicate which of the following statements is FALSE:
 - (a) The casual effect of education is the same for all women considered.
 - (b) In general, women with lower educational level have on average more children.

(c) <u>Older women have on average more children</u>.

Exam Type: 1

- 19. If we are certain that all the explanatory variables of model (II), except *EDUC*, are exogenous, and we would have estimated model (II) by 2SLS but using only *MEDUC* as an instrument for *EDUC*, the estimates obtained for the parameters of model (II):
 - (a) We cannot obtain consistent 2SLS estimates if we only have one instrument.
 - (b) Would be inconsistent.
 - (c) Would be less efficient than the 2SLS estimates in Output 4.
- 20. Assume that model (II) verifies the assumptions of the classical regression model. If the education variable (EDUC) was measured with error, the inconsistency bias of the estimates of the affected coefficients would be larger:
 - (a) The larger the expected value of education.
 - (b) The larger the variance of the measurement error with respect to the education variance.
 - (c) The larger the education variance with respect to the variance of the measurement error.
- 21. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education on women observed in 1978 is the same as on women observed in 1984, the test statistic (rounding to one decimal) would be:
 - (a) 0.6.
 - (b) -1.6.
 - (c) -2.4.
- 22. Let's focus on model (II):
 - (a) None of the other statements are correct.
 - (b) The model is misspecified, as it omits the variable Y72.
 - (c) Model (I) is a particular case of model (II).
- 23. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that education does not affect fertility:
 - (a) The null hypothesis would be $H_0: \delta_4 \delta_7 \delta_8 = 0$.
 - (b) The null hypothesis would be $H_0: \delta_4 = 0$.
 - (c) The null hypothesis would be $H_0: \delta_4 = \delta_7 = \delta_8 = 0.$
- 24. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1, we can say that fertility rates:
 - (a) We do not have enough information to conclude anything.
 - (b) Have remained constant over time.
 - (c) Have decreased over time.
- 25. If education was an endogenous variable, given the available information, we can say that
 - (a) It would be possible to obtain consistent estimates of the parameters by using only the father's education as instrument.
 - (b) Only the father's education (*FEDUC*) is a valid instrument for *EDUC*.
 - (c) Only the mother's education (*MEDUC*) is a valid instrument for *EDUC*.

- 26. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, for a 20 year old black woman with 5 years of education, between 1978 and 1984, the mean number of children has decreased (rounding to two decimals) by:
 - (a) 0.68.
 - (b) 0.48.
 - (c) 0.58.
- 27. The information provided in Output 6 allow us to know whether:
 - (a) None of the other statements are correct.
 - (b) We can reject the null hypothesis that education is exogenous.
 - (c) We can reject the null hypothesis that the instruments are valid.
- 28. Comparing the models (I) and (II), model (II) can be expressed as model (I) with the following restriction:
 - (a) $\delta_6 = 6\delta_5.$

(b)
$$\delta_5 = \delta_6.$$

(c)
$$\delta_6 = 2\delta_5$$

- 29. If we want to test whether both father's and mother's education are valid instruments, the value of the test statistic would be
 - (a) 154.9.
 - (b) 190.4.
 - (c) 26.8.
- 30. Using KIDS as dependent variable, consider the models that include a constant, AGE, AGE^2 , BLACK and EDUC. Indicate which of the following statements is FALSE:
 - (a) If we would also include YEAR and Y78 as explanatory variables , the model would be more general than model (I), but it would not be comparable to model (II), because the models impose different restrictions.
 - (b) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the R^2 would coincide with the one of Output 2.
 - (c) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the estimated coefficients of AGE, AGE^2 , BLACK and EDUC would coincide with those of Output 2.
- 31. Assume that model (I) verifies the assumptions of the classical regression model. If the variable KIDS was measured with some error, and that error was correlated with some of the explanatory variables, estimations in Output 1 would be:
 - (a) None of the other statements are correct.
 - (b) Inconsistent.
 - (c) As efficient as the ones obtained if the variable *KIDS* was not measured with error.
- 32. Given the results in Output 6:
 - (a) We do not reject that the correlation of the instruments with the error of model (II) is zero.
 - (b) We do not reject that EDUC is exogenous.
- (c) We do not reject that the correlation between the instruments and *EDUC* is zero.

- 33. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients and for a given race, age and education:
 - (a) A woman in 1984 has 58% less children than a woman in 1972.
 - (b) For every 100 women, there are around 58 less children in 1984 than in 1972.
 - (c) A woman in 1978 has 10% more children than a woman in 1972.
- 34. Assuming that models (I) and (II) verify the assumptions of the classical regression model, assume that the variable years of education (EDUC) is measured with error. Then
 - (a) Output 1 and Output 2 will provide consistent estimates for the parameters of models (I) and (II), respectively.
 - (b) Output 1 will provide consistent estimates for the parameters of model (I).
 - (c) Output 2 will provide inconsistent estimates for the parameters of model (II).
- 35. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results obtained:
 - (a) We cannot reject the above statement at the 10% significance level.
 - (b) At the 1% significance level, we can reject the above statement.
 - (c) We can reject the above statement at the 10% significance level, but we cannot at the 5% significance level.
- 36. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the null hypothesis that the effect of education on women observed in 1978 is the same as on women observed in 1984, we can conclude that:
 - (a) We do not reject the null hypothesis at the 10% significance level.
 - (b) We reject the null hypothesis at the 5% significance level.
 - (c) We reject the null hypothesis at the 10%, but we do not reject it at the 5% significance level.
- 37. Assume the error in the model (II) verifies $E(\varepsilon_2 | AGE, BLACK, EDUC, Y78, Y84) = 0$ for any combinations of the values of the explanatory variables, but the homoskedasticity assumption does not hold. Then:
 - (a) The Gauss-Markov Theorem is verified.
 - (b) The estimated OLS coefficients are inconsistent.
 - (c) The estimated OLS coefficients are unbiased.
- 38. Comparing the models (I) and (II):
 - (a) Model (I) imposes the restriction that the coefficient of Y84 is exactly the double of the coefficient of Y78.
 - (b) The models (I) and (II) are different models because none of them is a particular case of the other.
 - (c) Model (I) imposes the restriction that the coefficients of Y78 and Y84 are both equal to zero.

- 39. Suppose that we are interested in model (II). Consider the following conjecture: "For a given race and educational level, the decrease in the fertility rate is constant over time". Indicate which of the following statements is false:
 - We do not have enough information to evaluate the above conjecture. (a)
 - (b) If the conjecture is true, model (II) could be represented as model (I).
 - (c)At the 5% significance level, we cannot reject the above conjecture.
- 40. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the hypothesis that the year does not affect the number of children:
 - (a) The question cannot be answered with the provided information.
 - It is not rejected, as the p-value of the corresponding statistic is equal to zero. (b)
 - It is rejected given the value of the corresponding statistic obtained when comparing (c)the unrestricted model and the model that imposes the restriction.
- 41. In model (II), if you wanted to test that the effect of age on the number of children is constant, the null hypothesis would be
 - $H_0: \delta_1 + \delta_2 = 0.$ (a)
 - (b) $H_0: \delta_1 = \delta_2 = 0.$
 - $H_0: \delta_2 = 0.$ (c)
- 42. In model (II), if you wanted to test whether the mean number of children for a black woman in 1972 with 10 years of education is the same than a white woman in 1972 with the same age but with 12 years of education:
 - The null hypothesis would be $H_0: 2\delta_4 + \delta_3 = 0.$ (a)
 - The null hypothesis would be $H_0: 2\delta_4 \delta_3 = 0.$ (b)
 - The null hypothesis would be $H_0: 12\delta_4 \delta_3 = 0.$ (c)
- 43. Assume that model (I) verifies the assumptions of the classical regression model. Consider two women interviewed in the same year, both of them are white and have the same level of education, but one is 40 years old and the other one is 30 years old. The first one will have on average (rounding to the closest integer number):
 - (a)
 - 1 child more than the second woman.
 - (b) 5 children more than the second woman.
 - The same number of children as the second woman. (c)
- 44. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, in the year 1972, the mean difference in the number of children between a black woman and a white woman with the same age but with 5 years less of education than the first one is (rounding to one decimal):
 - 1.1 more children. (a)
 - 0.4 more children. (b)
 - 0.3 less children. (c)

- 45. If education was an endogenous variable, then:
 - (a) None of the other statements are correct.
 - (b) The estimated coefficients in Output 1 would be inconsistent for model (I), but those of Output 2 would not be inconsistent for model (II).
 - (c) The estimated coefficients in Output 2 would be inconsistent for model (II), but those of Output 3 would not be inconsistent for model (III).
- 46. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1 and keeping all the other factors constant, which of the following statements is FALSE:
 - (a) A woman in 1978 had on average 0.29 more children than a woman in 1984.
 - (b) A woman in 1978 had on average 0.29 less children than a woman in 1972.
 - (c) A woman in 1978 had on average 0.05 less children than a woman in 1972.

Universidad Carlos III de Madrid <u>ECONOMETRICS</u> Academic year 2009/10 FINAL EXAM May 17, 2010

DURATION: 2 HOURS

- 1. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education on women observed in 1978 is the same as on women observed in 1984, the test statistic (rounding to one decimal) would be:
 - (a) -2.4.
 - (b) −1.6.
 - (c) 0.6.
- 2. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the null hypothesis that the effect of education on women observed in 1978 is the same as on women observed in 1984, we can conclude that:
 - (a) We reject the null hypothesis at the 10%, but we do not reject it at the 5% significance level.
 - (b) We reject the null hypothesis at the 5% significance level.
 - (c) We do not reject the null hypothesis at the 10% significance level.
- 3. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that education does not affect fertility:
 - (a) The null hypothesis would be $H_0: \delta_4 = \delta_7 = \delta_8 = 0.$
 - (b) The null hypothesis would be $H_0: \delta_4 = 0.$
 - (c) The null hypothesis would be $H_0: \delta_4 \delta_7 \delta_8 = 0.$
- 4. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the unconditional variance of the dependent variable is:
 - (a) 2.56.
 - (b) 2.79.
 - (c) 1.60.
- 5. Comparing the models (II) and (III), indicate which of the following statements is FALSE:
 - (a) At the 5% significance level we would choose Model (II).
 - (b) Model (II) is more restrictive, because it imposes that the effect of education does not depend on time (the year).
 - (c) When estimating model (III) by OLS, we see that education does not longer have a significant effect on fertility.

- 6. Assume that model (I) verifies the assumptions of the classical regression model. Under the evidence of Output 1, the effect of age on the number of children is:
 - (a) Negative for women older than 35 years old.
 - (b) Constant.
 - (c) Positive, but marginally decreasing in age for women who are younger than 40.
- 7. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education for a women observed in 1978 is the same than the one observed in 1984, the null hypothesis would be:

(a)
$$\delta_7 = \delta_8.$$

(b)
$$\delta_7 = \delta_8 = 0.$$

- (c) $\delta_4 = \delta_7 = \delta_8.$
- 8. If education was an endogenous variable, given the available information, we can say that
 - (a) Only the mother's education (*MEDUC*) is a valid instrument for *EDUC*.
 - (b) Only the father's education (*FEDUC*) is a valid instrument for *EDUC*.
 - (c) It would be possible to obtain consistent estimates of the parameters by using only the father's education as instrument.
- 9. Assume that model (I) verifies the assumptions of the classical regression model. Consider two women interviewed in the same year, both of them are white and have the same level of education, but one is 40 years old and the other one is 30 years old. The first one will have on average (rounding to the closest integer number):
 - (a) The same number of children as the second woman.
 - (b) 5 children more than the second woman.
 - (c) 1 child more than the second woman.
- 10. In model (II), if you wanted to test whether the mean number of children for a black woman in 1972 with 10 years of education is the same than a white woman in 1972 with the same age but with 12 years of education:
 - (a) The null hypothesis would be $H_0: 12\delta_4 \delta_3 = 0$.
 - (b) The null hypothesis would be $H_0: 2\delta_4 \delta_3 = 0$.
 - (c) The null hypothesis would be $H_0: 2\delta_4 + \delta_3 = 0$.
- 11. Comparing the models (I) and (II):
 - (a) Model (II) is less restrictive, because it allows for a given race, age and education, that fertility rates change differently over time.
 - (b) Model (I) is more restrictive, because it imposes that in year 1972 education does not have an impact on the number of children.
 - (c) None of the other statements are correct.
- 12. In model (II), if you wanted to test that the effect of age on the number of children is constant, the null hypothesis would be
 - (a) $H_0: \delta_2 = 0.$ (b) $H_0: \delta_1 = \delta_2 = 0.$
 - (c) $H_0: \delta_1 = \delta_2 = 0.$ (c) $H_0: \delta_1 + \delta_2 = 0.$
- Exam Type: 2

- 13. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, for a 20 year old black woman with 5 years of education, between 1978 and 1984, the mean number of children has decreased (rounding to two decimals) by:
 - (a) 0.58.
 - (b) 0.48.
 - (c) 0.68.
- 14. The information provided in Output 6 allow us to know whether:
 - (a) We can reject the null hypothesis that the instruments are valid.
 - (b) We can reject the null hypothesis that education is exogenous.
 - (c) None of the other statements are correct.
- 15. If you only had information about the number of children, the best prediction you can give about the value of this variable (rounding up to two decimals) is:
 - (a) 1.67.
 - (b) 2.67.
 - (c) 2.20.
- 16. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1 and keeping all the other factors constant, which of the following statements is FALSE:
 - (a) A woman in 1978 had on average 0.05 less children than a woman in 1972.
 - (b) A woman in 1978 had on average 0.29 less children than a woman in 1972.
 - (c) A woman in 1978 had on average 0.29 more children than a woman in 1984.
- 17. Let's focus on model (II):
 - (a) Model (I) is a particular case of model (II).
 - (b) The model is misspecified, as it omits the variable Y72.
 - (c) None of the other statements are correct.
- 18. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results (rounding to one decimal):
 - (a) The test statistic is approximately t = -1.9.
 - (b) The test statistic is approximately t = -1.2.
 - (c) The test statistic is approximately t = 3.9.
- 19. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the variance of the dependent variable (rounding to two decimals), conditional on the explanatory variables is:
 - (a) 2.56.
 - (b) 2.79.
 - (c) 1.60.

- 20. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, in the year 1972, the mean difference in the number of children between a black woman and a white woman with the same age but with 5 years less of education than the first one is (rounding to one decimal):
 - (a) 0.3 less children.
 - (b) 0.4 more children.
 - (c) 1.1 more children.
- 21. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the year does not affect the number of children:
 - (a) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8 = 0.$
 - (b) The null hypothesis is $H_0: \delta_5 = \delta_6 = 0$.
 - (c) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8$.
- 22. Comparing the models (I) and (II), model (II) can be expressed as model (I) with the following restriction:

(a)
$$\delta_6 = 2\delta_5.$$

(b)
$$\delta_5 = \delta_6$$
.

- (c) $\delta_6 = 6\delta_5.$
- 23. If we are certain that all the explanatory variables of model (II), except *EDUC*, are exogenous, and we would have estimated model (II) by 2SLS but using only *MEDUC* as an instrument for *EDUC*, the estimates obtained for the parameters of model (II):
 - (a) Would be less efficient than the 2SLS estimates in Output 4.
 - (b) Would be inconsistent.
 - (c) We cannot obtain consistent 2SLS estimates if we only have one instrument.
- 24. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5 as an instrument for education.
 - (b) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5B as an instrument for education.
 - (c) None of the other statements are correct.
- 25. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the hypothesis that the year does not affect the number of children:
 - (a) It is rejected given the value of the corresponding statistic obtained when comparing the unrestricted model and the model that imposes the restriction.
 - (b) It is not rejected, as the p-value of the corresponding statistic is equal to zero.
 - (c) The question cannot be answered with the provided information.

- 26. Using KIDS as dependent variable, consider the models that include a constant, AGE, AGE^2 , BLACK and EDUC. Indicate which of the following statements is FALSE:
 - (a) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the estimated coefficients of AGE, AGE^2 , BLACK and EDUC would coincide with those of Output 2.
 - (b) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the R^2 would coincide with the one of Output 2.
 - (c) If we would also include *YEAR* and *Y*78 as explanatory variables , the model would be more general than model (I), but it would not be comparable to model (II), because the models impose different restrictions.
- 27. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1, we can say that fertility rates:
 - (a) Have decreased over time.
 - (b) Have remained constant over time.
 - (c) We do not have enough information to conclude anything.
- 28. Suppose that we are interested in model (II). Consider the following conjecture: "For a given race and educational level, the decrease in the fertility rate is constant over time". Indicate which of the following statements is false:
 - (a) At the 5% significance level, we cannot reject the above conjecture.
 - (b) If the conjecture is true, model (II) could be represented as model (I).
 - (c) We do not have enough information to evaluate the above conjecture.
- 29. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3:
 - (a) The effect of education is more negative in 1984 than in 1972.
 - (b) The effect of education does not vary over time.
 - (c) The effect of education is not statistically different from zero.
- 30. Assuming that models (I) and (II) verify the assumptions of the classical regression model, assume that the variable years of education (EDUC) is measured with error. Then
 - (a) Output 2 will provide inconsistent estimates for the parameters of model (II).
 - (b) Output 1 will provide consistent estimates for the parameters of model (I).
 - (c) Output 1 and Output 2 will provide consistent estimates for the parameters of models
 (I) and (II), respectively.
- 31. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results obtained:
 - (a) We can reject the above statement at the 10% significance level, but we cannot at the 5% significance level.
 - (b) At the 1% significance level, we can reject the above statement.
 - (c) We cannot reject the above statement at the 10% significance level.

- 32. Assume the error in the model (II) verifies $E(\varepsilon_2 | AGE, BLACK, EDUC, Y78, Y84) = 0$ for any combinations of the values of the explanatory variables, but the homoskedasticity assumption does not hold. Then:
 - (a) The estimated OLS coefficients are unbiased.
 - (b) The estimated OLS coefficients are inconsistent.
 - (c) The Gauss-Markov Theorem is verified.
- 33. If education was an endogenous variable, in order to test whether two instruments, father's and mother's education, are valid instruments, we would have to:
 - (a) Test the hypothesis that the residual of the reduced form (the linear projection of EDUC on the exogenous variables and both instruments) has a significant effect on education.
 - (b) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these last two variables are jointly significant.
 - (c) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these two instruments are individually significant.
- 34. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the instruments MEDUC and FEDUC.
 - (b) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5B.
 - $\begin{array}{c|c} \hline (c) & \text{Estimating by OLS a model with $KIDS$ as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5 \\ \end{array}$
- 35. Given the results in Output 6:
 - (a) We do not reject that the correlation between the instruments and *EDUC* is zero.
 - (b) We do not reject that EDUC is exogenous.
 - (c) We do not reject that the correlation of the instruments with the error of model (II) is zero.
- 36. Comparing the models (I) and (II):
 - (a) Model (I) imposes the restriction that the coefficients of Y78 and Y84 are both equal to zero.
 - (b) The models (I) and (II) are different models because none of them is a particular case of the other.
 - (c) Model (I) imposes the restriction that the coefficient of Y84 is exactly the double of the coefficient of Y78.
- 37. If we want to test whether both father's and mother's education are valid instruments, the value of the test statistic would be
 - (a) 26.8.
 - (b) 190.4.
 - (c) 154.9.

- 38. Assume that model (I) verifies the assumptions of the classical regression model. If the variable KIDS was measured with some error, and that error was correlated with some of the explanatory variables, estimations in Output 1 would be:
 - (a) As efficient as the ones obtained if the variable *KIDS* was not measured with error.
 - (b) Inconsistent.
 - (c) None of the other statements are correct.
- 39. Assume that model (II) verifies the assumptions of the classical regression model. If the education variable (EDUC) was measured with error, the inconsistency bias of the estimates of the affected coefficients would be larger:
 - (a) The larger the education variance with respect to the variance of the measurement error.
 - (b) The larger the variance of the measurement error with respect to the education variance.
 - (c) The larger the expected value of education.
- 40. If education was an endogenous variable, then:
 - (a) The estimated coefficients in Output 2 would be inconsistent for model (II), but those of Output 3 would not be inconsistent for model (III).
 - (b) The estimated coefficients in Output 1 would be inconsistent for model (I), but those of Output 2 would not be inconsistent for model (II).
 - (c) None of the other statements are correct.
- 41. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients and for a given race, age and education:
 - (a) A woman in 1978 has 10% more children than a woman in 1972.
 - (b) For every 100 women, there are around 58 less children in 1984 than in 1972.
 - (c) A woman in 1984 has 58% less children than a woman in 1972.
- 42. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the effect of education on the number of children does not depend on the year, the null hypothesis is:
 - (a) The null hypothesis is $H_0: \delta_4 = \delta_7 + \delta_8$.
 - (b) The null hypothesis is $H_0: \delta_7 = \delta_8$.
 - (c) The null hypothesis is $H_0: \delta_7 = \delta_8 = 0$.
- 43. Assume that model (I) verifies the assumptions of the classical regression model. If the variable *KIDS* was measured with error, estimates in the Output 1 will be in general:
 - (a) Less efficient that the ones obtained if the variable KIDS was not measured with error.
 - (b) Consistent.
 - (c) None of the other statements are correct.

- 44. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, the mean difference in the number of children between two women with the same characteristics but one in 1972 and the other in 1978 is:
 - (a) Statistically equal to zero.
 - (b) Significantly different from zero.
 - (c) The question cannot be answered with the information provided in Output 2.
- 45. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3, and taking into account only women younger than 40 years old, indicate which of the following statements is FALSE:
 - (a) Older women have on average more children.
 - (b) In general, women with lower educational level have on average more children.
 - (c) The casual effect of education is the same for all women considered.
- 46. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients (and rounding to two decimals), for a 20 year old white woman with 10 years of education:
 - (a) There is not enough information to predict the mean number of children in 1972.
 - (b) The mean number of children was approximately 0.19 in 1972.
 - (c) The mean number of children is approximately 6.24.

Universidad Carlos III de Madrid <u>ECONOMETRICS</u> Academic year 2009/10 FINAL EXAM May 17, 2010

DURATION: 2 HOURS

- 1. Assume that model (II) verifies the assumptions of the classical regression model. If the education variable (EDUC) was measured with error, the inconsistency bias of the estimates of the affected coefficients would be larger:
 - (a) The larger the variance of the measurement error with respect to the education variance.
 - (b) The larger the expected value of education.
 - (c) The larger the education variance with respect to the variance of the measurement error.
- 2. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the variance of the dependent variable (rounding to two decimals), conditional on the explanatory variables is:
 - (a) 2.79.
 - (b) 1.60.
 - (c) 2.56.
- 3. If education was an endogenous variable, then:
 - (a) The estimated coefficients in Output 1 would be inconsistent for model (I), but those of Output 2 would not be inconsistent for model (II).
 - (b) None of the other statements are correct.
 - (c) The estimated coefficients in Output 2 would be inconsistent for model (II), but those of Output 3 would not be inconsistent for model (III).
- 4. In model (II), if you wanted to test that the effect of age on the number of children is constant, the null hypothesis would be
 - (a) $H_0: \delta_1 = \delta_2 = 0.$
 - (b) $H_0: \delta_1 + \delta_2 = 0.$
 - (c) $H_0: \delta_2 = 0.$
- 5. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, in the year 1972, the mean difference in the number of children between a black woman and a white woman with the same age but with 5 years less of education than the first one is (rounding to one decimal):
 - (a) 0.4 more children.
 - (b) 1.1 more children.

(c) 0.3 less children.

- 6. Using KIDS as dependent variable, consider the models that include a constant, AGE, AGE^2 , BLACK and EDUC. Indicate which of the following statements is FALSE:
 - (a) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the R^2 would coincide with the one of Output 2.
 - (b) If we would also include *YEAR* and *Y*78 as explanatory variables , the model would be more general than model (I), but it would not be comparable to model (II), because the models impose different restrictions.
 - (c) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the estimated coefficients of AGE, AGE^2 , BLACK and EDUC would coincide with those of Output 2.
- 7. Comparing the models (I) and (II), model (II) can be expressed as model (I) with the following restriction:
 - (a) $\delta_5 = \delta_6$.
 - (b) $\delta_6 = 6\delta_5.$

(c)
$$\delta_6 = 2\delta_5$$
.

- 8. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, for a 20 year old black woman with 5 years of education, between 1978 and 1984, the mean number of children has decreased (rounding to two decimals) by:
 - (a) 0.48.
 - (b) 0.68.
 - (c) 0.58.
- 9. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education for a women observed in 1978 is the same than the one observed in 1984, the null hypothesis would be:
 - (a) $\delta_7 = \delta_8 = 0.$
 - (b) $\delta_4 = \delta_7 = \delta_8.$
 - (c) $\delta_7 = \delta_8$.
- 10. Assume that model (I) verifies the assumptions of the classical regression model. Under the evidence of Output 1, the effect of age on the number of children is:
 - (a) Constant.
 - (b) Positive, but marginally decreasing in age for women who are younger than 40.
 - $\overline{(c)}$ Negative for women older than 35 years old.
- 11. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3:
 - (a) The effect of education does not vary over time.
 - (b) The effect of education is not statistically different from zero.
 - (c) The effect of education is more negative in 1984 than in 1972.

- 12. Assume that model (I) verifies the assumptions of the classical regression model. If the variable KIDS was measured with some error, and that error was correlated with some of the explanatory variables, estimations in Output 1 would be:
 - (a) Inconsistent.
 - (b) None of the other statements are correct.
 - (c) As efficient as the ones obtained if the variable *KIDS* was not measured with error.
- 13. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the null hypothesis that the effect of education on women observed in 1978 is the same as on women observed in 1984, we can conclude that:
 - (a) We reject the null hypothesis at the 5% significance level.
 - (b) We do not reject the null hypothesis at the 10% significance level.
 - (c) We reject the null hypothesis at the 10%, but we do not reject it at the 5% significance level.
- 14. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1, we can say that fertility rates:
 - (a) Have remained constant over time.
 - (b) We do not have enough information to conclude anything.
 - (c) Have decreased over time.
- 15. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5B as an instrument for education.
 - (b) None of the other statements are correct.
 - (c) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5 as an instrument for education.
- 16. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3, and taking into account only women younger than 40 years old, indicate which of the following statements is FALSE:
 - (a) In general, women with lower educational level have on average more children.
 - (b) The casual effect of education is the same for all women considered.
 - (c) Older women have on average more children.
- 17. Given the results in Output 6:



- We do not reject that EDUC is exogenous.
- (b) We do not reject that the correlation of the instruments with the error of model (II) is zero.
- (c) We do not reject that the correlation between the instruments and *EDUC* is zero.

- 18. Suppose that we are interested in model (II). Consider the following conjecture: "For a given race and educational level, the decrease in the fertility rate is constant over time". Indicate which of the following statements is false:
 - (a) If the conjecture is true, model (II) could be represented as model (I).
 - (b) We do not have enough information to evaluate the above conjecture.
 - (c) At the 5% significance level, we cannot reject the above conjecture.
- 19. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the effect of education on the number of children does not depend on the year, the null hypothesis is:
 - (a) The null hypothesis is $H_0: \delta_7 = \delta_8$.
 - (b) The null hypothesis is $H_0: \delta_7 = \delta_8 = 0$.
 - (c) The null hypothesis is $H_0: \delta_4 = \delta_7 + \delta_8$.
- 20. Assuming that models (I) and (II) verify the assumptions of the classical regression model, assume that the variable years of education (EDUC) is measured with error. Then
 - (a) Output 1 will provide consistent estimates for the parameters of model (I).
 - (b) Output 1 and Output 2 will provide consistent estimates for the parameters of models (I) and (II), respectively.
 - (c) Output 2 will provide inconsistent estimates for the parameters of model (II).
- 21. If we want to test whether both father's and mother's education are valid instruments, the value of the test statistic would be
 - (a) 190.4.
 - (b) 154.9.
 - (c) 26.8.
- 22. Comparing the models (II) and (III), indicate which of the following statements is FALSE:
 - (a) Model (II) is more restrictive, because it imposes that the effect of education does not depend on time (the year).
 - (b) When estimating model (III) by OLS, we see that education does not longer have a significant effect on fertility.
 - (c) At the 5% significance level we would choose Model (II).
- 23. In model (II), if you wanted to test whether the mean number of children for a black woman in 1972 with 10 years of education is the same than a white woman in 1972 with the same age but with 12 years of education:
 - (a) The null hypothesis would be $H_0: 2\delta_4 \delta_3 = 0.$
 - (b) The null hypothesis would be $H_0: 2\delta_4 + \delta_3 = 0$.
 - (c) The null hypothesis would be $H_0: 12\delta_4 \delta_3 = 0.$

- 24. If education was an endogenous variable, in order to test whether two instruments, father's and mother's education, are valid instruments, we would have to:
 - (a) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these last two variables are jointly significant.
 - (b) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these two instruments are individually significant.
 - (c) Test the hypothesis that the residual of the reduced form (the linear projection of EDUC on the exogenous variables and both instruments) has a significant effect on education.
- 25. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the unconditional variance of the dependent variable is:
 - (a) 2.79.
 - (b) 1.60.
 - (c) 2.56.
- 26. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that education does not affect fertility:
 - (a) The null hypothesis would be $H_0: \delta_4 = 0$.
 - (b) The null hypothesis would be $H_0: \delta_4 \delta_7 \delta_8 = 0.$
 - (c) The null hypothesis would be $H_0: \delta_4 = \delta_7 = \delta_8 = 0.$
- 27. If you only had information about the number of children, the best prediction you can give about the value of this variable (rounding up to two decimals) is:
 - (a) 2.67.
 - (b) 2.20.
 - (c) 1.67.
- 28. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education on women observed in 1978 is the same as on women observed in 1984, the test statistic (rounding to one decimal) would be:
 - $\begin{array}{ccc} (a) & -1.6. \\ \hline (b) & 0.6. \\ \hline (c) & -2.4. \end{array}$
- 29. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the year does not affect the number of children:
 - (a) The null hypothesis is $H_0: \delta_5 = \delta_6 = 0.$
 - (b) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8$.
 - (c) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8 = 0.$
- 30. If education was an endogenous variable, given the available information, we can say that
 - (a) Only the father's education (*FEDUC*) is a valid instrument for *EDUC*.
 - (b) It would be possible to obtain consistent estimates of the parameters by using only the father's education as instrument.
 - (c) Only the mother's education (*MEDUC*) is a valid instrument for *EDUC*.

- 31. Comparing the models (I) and (II):
 - (a) The models (I) and (II) are different models because none of them is a particular case of the other.
 - (b) Model (I) imposes the restriction that the coefficient of Y84 is exactly the double of the coefficient of Y78.
 - (c) Model (I) imposes the restriction that the coefficients of Y78 and Y84 are both equal to zero.
- 32. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients (and rounding to two decimals), for a 20 year old white woman with 10 years of education:
 - (a) The mean number of children was approximately 0.19 in 1972.
 - (b) The mean number of children is approximately 6.24.
 - (c) There is not enough information to predict the mean number of children in 1972.
- 33. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1 and keeping all the other factors constant, which of the following statements is FALSE:
 - (a) A woman in 1978 had on average 0.29 less children than a woman in 1972.
 - (b) A woman in 1978 had on average 0.29 more children than a woman in 1984.
 - (c) A woman in 1978 had on average 0.05 less children than a woman in 1972.
- 34. The information provided in Output 6 allow us to know whether:
 - (a) We can reject the null hypothesis that education is exogenous.
 - (b) None of the other statements are correct.
 - (c) We can reject the null hypothesis that the instruments are valid.
- 35. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results (rounding to one decimal):
 - (a) The test statistic is approximately t = -1.2.
 - (b) The test statistic is approximately t = 3.9.
 - (c) The test statistic is approximately t = -1.9.
- 36. Assume that model (I) verifies the assumptions of the classical regression model. If the variable *KIDS* was measured with error, estimates in the Output 1 will be in general:
 - (a) Consistent.
 - (b) None of the other statements are correct.
 - (c) Less efficient that the ones obtained if the variable KIDS was not measured with error.
- 37. Assume the error in the model (II) verifies $E(\varepsilon_2 | AGE, BLACK, EDUC, Y78, Y84) = 0$ for any combinations of the values of the explanatory variables, but the homoskedasticity assumption does not hold. Then:
 - (a) The estimated OLS coefficients are inconsistent.
 - (b) The Gauss-Markov Theorem is verified.
 - (c) The estimated OLS coefficients are unbiased.

- 38. Comparing the models (I) and (II):
 - (a) Model (I) is more restrictive, because it imposes that in year 1972 education does not have an impact on the number of children.
 - (b) None of the other statements are correct.
 - (c) Model (II) is less restrictive, because it allows for a given race, age and education, that fertility rates change differently over time.
- 39. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by OLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5B.
 - (b) Estimating by OLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5
 - (c) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the instruments MEDUC and FEDUC.
- 40. If we are certain that all the explanatory variables of model (II), except *EDUC*, are exogenous, and we would have estimated model (II) by 2SLS but using only *MEDUC* as an instrument for *EDUC*, the estimates obtained for the parameters of model (II):
 - (a) Would be inconsistent.
 - (b) We cannot obtain consistent 2SLS estimates if we only have one instrument.
 - (c) Would be less efficient than the 2SLS estimates in Output 4.
- 41. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the hypothesis that the year does not affect the number of children:
 - (a) It is not rejected, as the p-value of the corresponding statistic is equal to zero.
 - (b) The question cannot be answered with the provided information.
 - (c) It is rejected given the value of the corresponding statistic obtained when comparing the unrestricted model and the model that imposes the restriction.
- 42. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results obtained:
 - (a) At the 1% significance level, we can reject the above statement.
 - (b) We cannot reject the above statement at the 10% significance level.
 - (c) We can reject the above statement at the 10% significance level, but we cannot at the 5% significance level.
- 43. Assume that model (I) verifies the assumptions of the classical regression model. Consider two women interviewed in the same year, both of them are white and have the same level of education, but one is 40 years old and the other one is 30 years old. The first one will have on average (rounding to the closest integer number):
 - (a)
- 5 children more than the second woman.
- (b) 1 child more than the second woman.
- (c) The same number of children as the second woman.

- 44. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients and for a given race, age and education:
 - (a) For every 100 women, there are around 58 less children in 1984 than in 1972.
 - (b) A woman in 1984 has 58% less children than a woman in 1972.
 - (c) A woman in 1978 has 10% more children than a woman in 1972.
- 45. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, the mean difference in the number of children between two women with the same characteristics but one in 1972 and the other in 1978 is:
 - (a) Significantly different from zero.
 - (b) The question cannot be answered with the information provided in Output 2.
 - (c) Statistically equal to zero.
- 46. Let's focus on model (II):
 - (a) The model is misspecified, as it omits the variable Y72.
 - (b) None of the other statements are correct.
 - (c) Model (I) is a particular case of model (II).

Universidad Carlos III de Madrid <u>ECONOMETRICS</u> Academic year 2009/10 FINAL EXAM May 17, 2010

DURATION: 2 HOURS

- 1. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients and for a given race, age and education:
 - (a) A woman in 1978 has 10% more children than a woman in 1972.
 - (b) A woman in 1984 has 58% less children than a woman in 1972.
 - (c) For every 100 women, there are around 58 less children in 1984 than in 1972.
- 2. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that education does not affect fertility:
 - (a) The null hypothesis would be $H_0: \delta_4 = \delta_7 = \delta_8 = 0$.
 - (b) The null hypothesis would be $H_0: \delta_4 \delta_7 \delta_8 = 0.$
 - (c) The null hypothesis would be $H_0: \delta_4 = 0$.
- 3. Comparing the models (I) and (II), model (II) can be expressed as model (I) with the following restriction:

(a)
$$\delta_6 = 2\delta_5.$$

(b)
$$\delta_6 = 6\delta_5.$$

- (c) $\delta_5 = \delta_6.$
- 4. Let's focus on model (II):
 - (a) Model (I) is a particular case of model (II).
 - (b) None of the other statements are correct.
 - (c) The model is misspecified, as it omits the variable Y72.
- 5. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the effect of education on the number of children does not depend on the year, the null hypothesis is:
 - (a) The null hypothesis is $H_0: \delta_4 = \delta_7 + \delta_8$.
 - (b) The null hypothesis is $H_0: \delta_7 = \delta_8 = 0.$
 - (c) The null hypothesis is $H_0: \delta_7 = \delta_8$.

- 6. Using KIDS as dependent variable, consider the models that include a constant, AGE, AGE^2 , BLACK and EDUC. Indicate which of the following statements is FALSE:
 - (a) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the estimated coefficients of AGE, AGE^2 , BLACK and EDUC would coincide with those of Output 2.
 - (b) If we would also include *YEAR* and *Y*78 as explanatory variables , the model would be more general than model (I), but it would not be comparable to model (II), because the models impose different restrictions.
 - (c) If we would also include YEAR and Y78 as explanatory variables and we would estimate by OLS, the R^2 would coincide with the one of Output 2.
- 7. If you only had information about the number of children, the best prediction you can give about the value of this variable (rounding up to two decimals) is:
 - (a) 1.67.
 - (b) 2.20.
 - (c) 2.67.
- 8. Assume that model (I) verifies the assumptions of the classical regression model. If the variable KIDS was measured with some error, and that error was correlated with some of the explanatory variables, estimations in Output 1 would be:
 - (a) As efficient as the ones obtained if the variable *KIDS* was not measured with error.
 - (b) None of the other statements are correct.
 - (c) Inconsistent.
- 9. In model (II), if you wanted to test whether the mean number of children for a black woman in 1972 with 10 years of education is the same than a white woman in 1972 with the same age but with 12 years of education:
 - (a) The null hypothesis would be $H_0: 12\delta_4 \delta_3 = 0$.
 - (b) The null hypothesis would be $H_0: 2\delta_4 + \delta_3 = 0.$
 - (c) The null hypothesis would be $H_0: 2\delta_4 \delta_3 = 0.$
- 10. Comparing the models (II) and (III), indicate which of the following statements is FALSE:



- At the 5% significance level we would choose Model (II).
- (b) When estimating model (III) by OLS, we see that education does not longer have a significant effect on fertility.
- (c) Model (II) is more restrictive, because it imposes that the effect of education does not depend on time (the year).
- 11. Assume that model (I) verifies the assumptions of the classical regression model. Consider two women interviewed in the same year, both of them are white and have the same level of education, but one is 40 years old and the other one is 30 years old. The first one will have on average (rounding to the closest integer number):
 - (a) The same number of children as the second woman.
 - (b) 1 child more than the second woman.
 - (c) 5 children more than the second woman.

- 12. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, in the year 1972, the mean difference in the number of children between a black woman and a white woman with the same age but with 5 years less of education than the first one is (rounding to one decimal):
 - (a) 0.3 less children.
 - (b) 1.1 more children.
 - (c) 0.4 more children.
- 13. Assume that model (I) verifies the assumptions of the classical regression model. Under the evidence of Output 1, the effect of age on the number of children is:
 - (a) Negative for women older than 35 years old.
 - (b) Positive, but marginally decreasing in age for women who are younger than 40.
 - (c) Constant.
- 14. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3, and taking into account only women younger than 40 years old, indicate which of the following statements is FALSE:
 - (a) Older women have on average more children.
 - (b) The casual effect of education is the same for all women considered.
 - (c) In general, women with lower educational level have on average more children.
- 15. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients (and rounding to two decimals), for a 20 year old white woman with 10 years of education:
 - (a) There is not enough information to predict the mean number of children in 1972.
 - (b) The mean number of children is approximately 6.24.
 - (c) The mean number of children was approximately 0.19 in 1972.
- 16. In model (II), if you wanted to test that the effect of age on the number of children is constant, the null hypothesis would be
 - (a) $H_0: \delta_2 = 0.$
 - (b) $H_0: \delta_1 + \delta_2 = 0.$
 - (c) $H_0: \delta_1 = \delta_2 = 0.$
- 17. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1 and keeping all the other factors constant, which of the following statements is FALSE:
 - (a) A woman in 1978 had on average 0.05 less children than a woman in 1972.
 - (b) A woman in 1978 had on average 0.29 more children than a woman in 1984.
 - (c) A woman in 1978 had on average 0.29 less children than a woman in 1972.
- 18. Comparing the models (I) and (II):
 - (a) Model (I) imposes the restriction that the coefficients of Y78 and Y84 are both equal to zero.
 - (b) Model (I) imposes the restriction that the coefficient of Y84 is exactly the double of the coefficient of Y78.
- (c) The models (I) and (II) are different models because none of them is a particular case of the other.
 Exam Type: 4

- 19. Comparing the models (I) and (II):
 - (a) Model (II) is less restrictive, because it allows for a given race, age and education, that fertility rates change differently over time.
 - (b) None of the other statements are correct.
 - (c) Model (I) is more restrictive, because it imposes that in year 1972 education does not have an impact on the number of children.
- 20. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the null hypothesis that the effect of education on women observed in 1978 is the same as on women observed in 1984, we can conclude that:
 - (a) We reject the null hypothesis at the 10%, but we do not reject it at the 5% significance level.
 - (b) We do not reject the null hypothesis at the 10% significance level.
 - (c) We reject the null hypothesis at the 5% significance level.
- 21. If education was an endogenous variable, in order to test whether two instruments, father's and mother's education, are valid instruments, we would have to:
 - (a) Test the hypothesis that the residual of the reduced form (the linear projection of EDUC on the exogenous variables and both instruments) has a significant effect on education.
 - (b) In a regression of *EDUC* on the exogenous variables of the model and on both instruments, test that these two instruments are individually significant.
 - $\begin{array}{c|c} \hline (c) & \text{In a regression of } EDUC \text{ on the exogenous variables of the model and on both instruments, test that these last two variables are jointly significant.} \end{array}$
- 22. Suppose that we are interested in model (II). Consider the following conjecture: "For a given race and educational level, the decrease in the fertility rate is constant over time". Indicate which of the following statements is false:
 - (a) At the 5% significance level, we cannot reject the above conjecture.
 - (b) We do not have enough information to evaluate the above conjecture.
 - (c) If the conjecture is true, model (II) could be represented as model (I).
- 23. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education for a women observed in 1978 is the same than the one observed in 1984, the null hypothesis would be:

(a)
$$\delta_7 = \delta_8$$
.

(b)
$$\delta_4 = \delta_7 = \delta_8.$$

(c)
$$\delta_7 = \delta_8 = 0$$

- 24. Assume that model (II) verifies the assumptions of the classical regression model. If the education variable (EDUC) was measured with error, the inconsistency bias of the estimates of the affected coefficients would be larger:
 - (a) The larger the education variance with respect to the variance of the measurement error.
 - (b) The larger the expected value of education.
 - (c) The larger the variance of the measurement error with respect to the education variance.

- 25. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test the hypothesis that the year does not affect the number of children:
 - (a) It is rejected given the value of the corresponding statistic obtained when comparing the unrestricted model and the model that imposes the restriction.
 - (b) The question cannot be answered with the provided information.
 - (c) It is not rejected, as the p-value of the corresponding statistic is equal to zero.
- 26. If we want to test whether both father's and mother's education are valid instruments, the value of the test statistic would be
 - (a) 26.8.
 - (b) 154.9.
 - (c) 190.4.
- 27. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, for a 20 year old black woman with 5 years of education, between 1978 and 1984, the mean number of children has decreased (rounding to two decimals) by:
 - (a) 0.58.
 - $(b) \quad 0.68.$
 - (c) 0.48.
- 28. Assume that model (II) verifies the assumptions of the classical regression model. Given the estimated coefficients, the mean difference in the number of children between two women with the same characteristics but one in 1972 and the other in 1978 is:
 - (a) Statistically equal to zero.
 - (b) The question cannot be answered with the information provided in Output 2.
 - (c) Significantly different from zero.
- 29. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the unconditional variance of the dependent variable is:
 - (a) 2.56.
 - (b) 1.60.
 - (c) 2.79.
- 30. Assume that model (III) verifies the assumptions of the classical regression model. Given the results in Output 3:
 - (a) The effect of education is more negative in 1984 than in 1972.
 - (b) The effect of education is not statistically different from zero.
 - (c) The effect of education does not vary over time.
- 31. If we are certain that all the explanatory variables of model (II), except *EDUC*, are exogenous, and we would have estimated model (II) by 2SLS but using only *MEDUC* as an instrument for *EDUC*, the estimates obtained for the parameters of model (II):
 - (a) Would be less efficient than the 2SLS estimates in Output 4.
 - (b) We cannot obtain consistent 2SLS estimates if we only have one instrument.
 - (c) Would be inconsistent.

- 32. If education was an endogenous variable, then:
 - (a) The estimated coefficients in Output 2 would be inconsistent for model (II), but those of Output 3 would not be inconsistent for model (III).
 - (b) None of the other statements are correct.
 - (c) The estimated coefficients in Output 1 would be inconsistent for model (I), but those of Output 2 would not be inconsistent for model (II).
- 33. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5 as an instrument for education.
 - (b) None of the other statements are correct.
 - (c) Estimating by 2SLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the education, using a prediction based on the estimations in Output 5B as an instrument for education.
- 34. Assume that model (I) verifies the assumptions of the classical regression model. An appropriate estimation of the variance of the dependent variable (rounding to two decimals), conditional on the explanatory variables is:
 - (a) 2.56.
 - (b) 1.60.
 - (c) 2.79.
- 35. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test that the year does not affect the number of children:
 - (a) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8 = 0.$
 - (b) The null hypothesis is $H_0: \delta_5 = \delta_6 = \delta_7 = \delta_8$.
 - (c) The null hypothesis is $H_0: \delta_5 = \delta_6 = 0$.
- 36. Assuming that models (I) and (II) verify the assumptions of the classical regression model, assume that the variable years of education (EDUC) is measured with error. Then
 - (a) Output 2 will provide inconsistent estimates for the parameters of model (II).
 - (b) Output 1 and Output 2 will provide consistent estimates for the parameters of models (I) and (II), respectively.
 - (c) Output 1 will provide consistent estimates for the parameters of model (I).
- 37. Given the results in Output 6:
 - (a) We do not reject that the correlation between the instruments and *EDUC* is zero.
 - (b) We do not reject that the correlation of the instruments with the error of model (II) is zero.
 - (c) We do not reject that EDUC is exogenous.

- 38. The 2SLS estimated coefficients in Output 4 could have been obtained in an equivalent way:
 - (a) Estimating by OLS a model with KIDS as the dependent variable and including as regressors all the exogenous explanatory variables and the instruments MEDUC and FEDUC.
 - (b) Estimating by OLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5
 - (c) Estimating by OLS a model with *KIDS* as the dependent variable and including as regressors all the exogenous explanatory variables and the prediction of education based on the estimations in Output 5B.
- 39. The information provided in Output 6 allow us to know whether:
 - (a) We can reject the null hypothesis that the instruments are valid.
 - (b) None of the other statements are correct.
 - (c) We can reject the null hypothesis that education is exogenous.
- 40. If education was an endogenous variable, given the available information, we can say that
 - (a) Only the mother's education (*MEDUC*) is a valid instrument for *EDUC*.
 - (b) It would be possible to obtain consistent estimates of the parameters by using only the father's education as instrument.
 - (c) Only the father's education (*FEDUC*) is a valid instrument for *EDUC*.
- 41. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results (rounding to one decimal):
 - (a) The test statistic is approximately t = -1.9.
 - (b) The test statistic is approximately t = 3.9.
 - (c) The test statistic is approximately t = -1.2.
- 42. Suppose that we are interested in model (II). Consider the following statement: "In 1972, the fertility rate of a 30 year old black woman is equal to the fertility rate of a white woman of the same age but with 8 years less of education". Given the results obtained:
 - (a)

We can reject the above statement at the 10% significance level, but we cannot at the 5% significance level.

- (b) We cannot reject the above statement at the 10% significance level.
- (c) At the 1% significance level, we can reject the above statement.
- 43. Assume the error in the model (II) verifies $E(\varepsilon_2 | AGE, BLACK, EDUC, Y78, Y84) = 0$ for any combinations of the values of the explanatory variables, but the homoskedasticity assumption does not hold. Then:
 - (a) The estimated OLS coefficients are unbiased.
 - (b) The Gauss-Markov Theorem is verified.
 - (c) The estimated OLS coefficients are inconsistent.

- 44. Assume that model (III) verifies the assumptions of the classical regression model. If we wanted to test whether the effect of education on women observed in 1978 is the same as on women observed in 1984, the test statistic (rounding to one decimal) would be:
 - (a) -2.4.(b) 0.6.
 - (c) -1.6.
- 45. Assume that model (I) verifies the assumptions of the classical regression model. Given the results in Output 1, we can say that fertility rates:
 - (a) Have decreased over time.
 - (b) We do not have enough information to conclude anything.
 - (c) Have remained constant over time.
- 46. Assume that model (I) verifies the assumptions of the classical regression model. If the variable *KIDS* was measured with error, estimates in the Output 1 will be in general:
 - (a) Less efficient that the ones obtained if the variable KIDS was not measured with error.
 - (b) None of the other statements are correct.
 - (c) Consistent.