2. Consider an exchange economy that operates over an infinite number of consecutive dates. There is a single perishable consumption good. Every date t, N_t individuals are born. Individuals live only two dates. Thus, every date t only the consumers born at t - 1 (the elderly), and those born at t (the young) interact. The preferences of individuals for consumption when young, x, and old, y, are represented by the utility function u(x, y) = xy, and their endowments are $\bar{x} = 10$ and $\bar{y} = 4$.

(a) Discuss why even if there is a credit market there is no trade is the unique competitive equilibrium. (Note that only the young can borrow or lend.) Verify that the equilibrium allocation is not Pareto optimal.

(b) Suppose now that there is a stock of money held initially by the elderly at date 1. Specifically, at date 1 each elder owns $\in 8$. Money must be accepted as a mean of exchange, i.e., every date t there is a competitive market in which the good is exchanged for money at a price of p_t (euros per unit). Write the budget constraints of a consumer. (Use the notation $\rho_t = p_t/p_{t+1}$, and note that young consumers have no money.) Calculate the set of stationary equilibrium prices (i.e., those in which ρ_t is constant over time), and identify the price ρ^* supporting the Golden Rule, assuming that: (i) $N_t = 2N_{t-1}$; (ii) $N_t = N_{t-1}$; (iii) $N_t = N_{t-1}/2$.



IF THE YOUNG OF EACH GENERATION DONATED 2 UNITS OF GASUMPTION TO THE OLD AND THESE DONDTION ARE SHARED EQUALY BY THE OLD, THEN THE CONSUMPTION STREAMS ARE: DATE : 1 2 3 --t. _ - - -0LD X X 8 --- X ---YOUNG 8 8 8 ----8 (X) 4+2 (2) NOTE THAT THERE DRE TWICE AS MANY YOUNC INDIVIDUALS THAN OLD INDIVIDUALS (20) THE CONSUMPTION STREAM OF BENERATION t=0 is (10,8). ALL THE OTHER BENATIONS' CONSUMPTION STREAM IS (8,8). TILLS SCHEME IS NOT A MARKET OUTCOME BUT IT CON BE THE RESULT OF & CULTUREL TROIT BY WINCH EACH MOTHER RECIEVES 2 UNITS OF CONSUMPTION FROM EACH OF HER TWO DAVENTERS WHAT IF THE POPULATION IS STUNKING ?

(6) MONEY (NEWN OF TRANSACTION, DEPOST OF VALVE) SUPPOSE THE STOCK OF MONEY IS GIVEN TO THE OLD PRESENT IT

E=1. Normaly, THESE AGENTS WILL USE MOMEY TO BEY AS HUCH

OF THE CONSUMPTION GOOD AS THEY CAN, A YOUNG AGENT

SCLUNG SOME OF ITS ENDOWINGNE AF TIME & CAN HOLD

ON THE MONEY HE'S RECEIVES TO BY GOOD THE NEXT

DATE, JIMS, HER BUDGET CONSTRAINT IS

 $P_{b}(x - \overline{x}) + P_{k+1}(y - \overline{y}) = 0$ (1)

OBVIOUSLY, IN EQUILIBRIUM PLZO, YE. HENCE (1)

MAJ BE WRITEN AS

, ____



ILN ACENT BORN AT É CINOOSE (X, X) TO SOLUE

$$mex \qquad xy$$
s.t.
$$P_{k} x + y = loP_{k} + y$$

THE SOWNON SOLVES THE SEISTEM

HENCE, MARKET CLEARING ACQUIRES

$$N_{t-1}(2 + SP_{t-1}) + N_{t}(S + \frac{2}{P_{t}}) = N_{t-1}(4) + N_{t}(10)$$

 $(\dot{c}) N_{c} = 2 N_{t-1}$

$$SP + \frac{4}{0} = 12$$

A STATIONARY CE (1.E., Pt=P, HE) SATISFIES

$$SP^{2} - 12p + 4 = 0 \iff P = \frac{12 + \sqrt{12^{2} - 8_{2}}}{10} = \frac{12 + 8}{10} = \frac{12}{10}$$



IN MIS CE THERE IS NO TROOF!

For
$$p=2$$
, $x(z) = 6$, $y(z) = 12$. $h^* = 12$

(ii)
$$N_{t-1} = N_t$$
: MARKET CLEANING: 2+5P+5+ $\frac{2}{P}$ -4+10

(iii) $N_{e-1} = 2N_{e}$. M_{c} : $4 + 10P + S + \frac{2}{P} = 2(4) + 10$

